

$$P(\mathcal{D} | a, \beta) = \prod_{d=1}^M \int p(\vartheta_d | a) \left(\prod_{n=1}^{N_d} \sum_z p(z | \vartheta_d) p(w_n | z, \beta) \right) d\vartheta$$