

Hashing

Preliminary Slides

IntegerSet ADT interface

- Let's implement

```
public interface IntegerSet {  
    void add(Integer value);  
    boolean contains(Integer value);  
    void clear();  
    boolean isEmpty();  
    void remove(Integer value);  
    int size();  
}
```

add, contains, remove should be $O(1)$

→ Add and search quickly

Implementing HashSet using hash table and linear probing

```
public class HashSet implements IntegerSet {
    private Integer[] elements;
    private int size;

    // constructs new empty set
    public HashSet() {
        elements = new Integer[10];
        size = 0;
    }

    // hash function maps values to indexes
    private int hash(Integer value) {
        return Math.abs(value.hashCode()) % elements.length;
    }
    ...
}
```

The add operation

- Use the hash function to find the proper bucket index.
 - If we see a `null` (empty bucket) → put it there.
 - If not, move forward until we find an empty (`null`) index to store it.
 - If the value is already in the table
- do NOT re-add it (WHY?)
- `set.add(54);` `// client code`
 - `set.add(14);`

<i>index</i>	0	1	2	3	4	5	6	7	8	9
<i>value</i>		11			24	54	14	37		49
<i>size</i>	6									

The contains operation

- Use the hash function to find the proper bucket index.
- Loop forward until the value is found, or an empty index (`null`).
- If the value is found → return `true`
- If 0 is found → return `false`.
 - `set.contains(24)` // `true`
 - `set.contains(14)` // `true`
 - `set.contains(35)` // `false`

<i>index</i>	<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>	<i>8</i>	<i>9</i>
<i>value</i>		11			24	54	14	37		49
<i>size</i>	6									

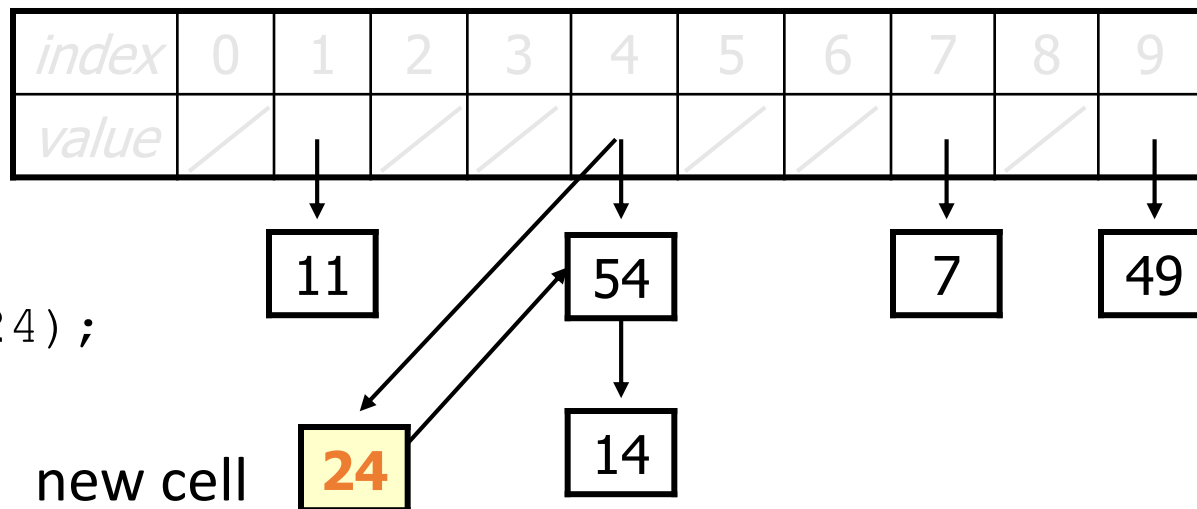
Implementing HashSet using separate chaining

```
public class HashSet implements IntegerSet {
    // array of linked lists;
    // elements[i] = front of list #i (null if empty)
    private Cell[] elements;
    private int size;

    // constructs new empty set
    public HashSet() {
        elements = new Cell[10];
        size = 0;
    }
    // hash function maps values to indexes
    // We do NOT use here the Integer hashCode()
    private int hash(Integer value) {
        return Math.abs(value) % elements.length;
    }
    ...
}
```

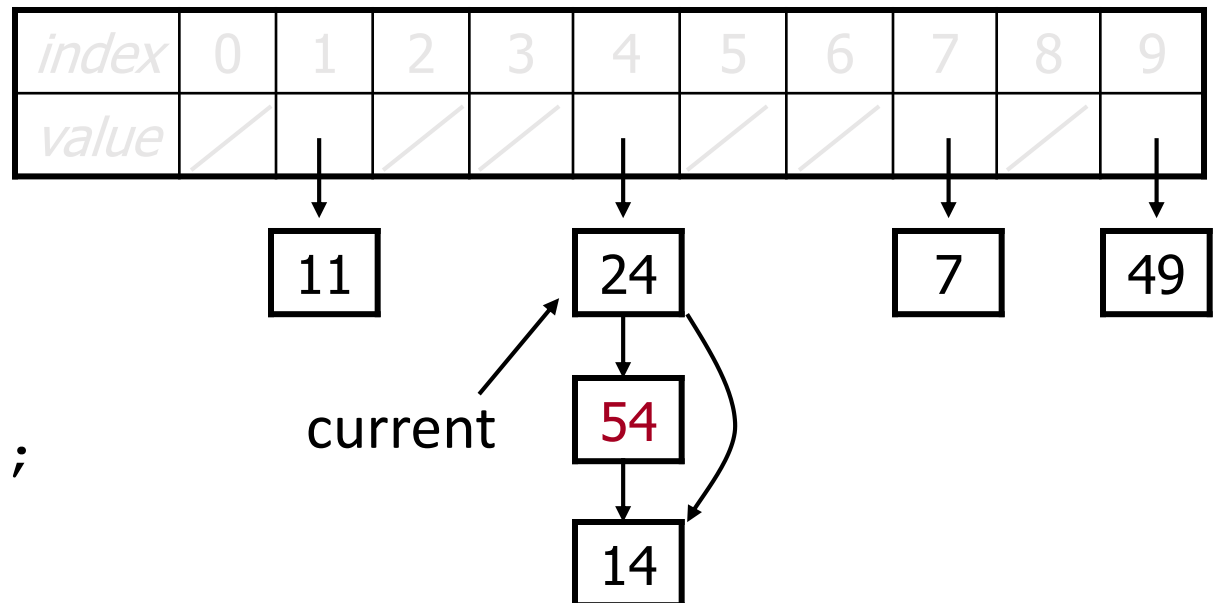
The add operation

- How do we add an element to the hash table?
 - Modification of a linked list change can be done by
 - the list's `head` reference
 - or the `next` field of a node in the list.
 - Where/when should we add the new element?
 - Must make sure to avoid duplicates.



The remove operation

- How do we remove an element from the hash table?
- Cases to consider:
 - head (24),
 - non-head (14),
 - not found (94),
 - null (32)



```
set.remove(54);
```