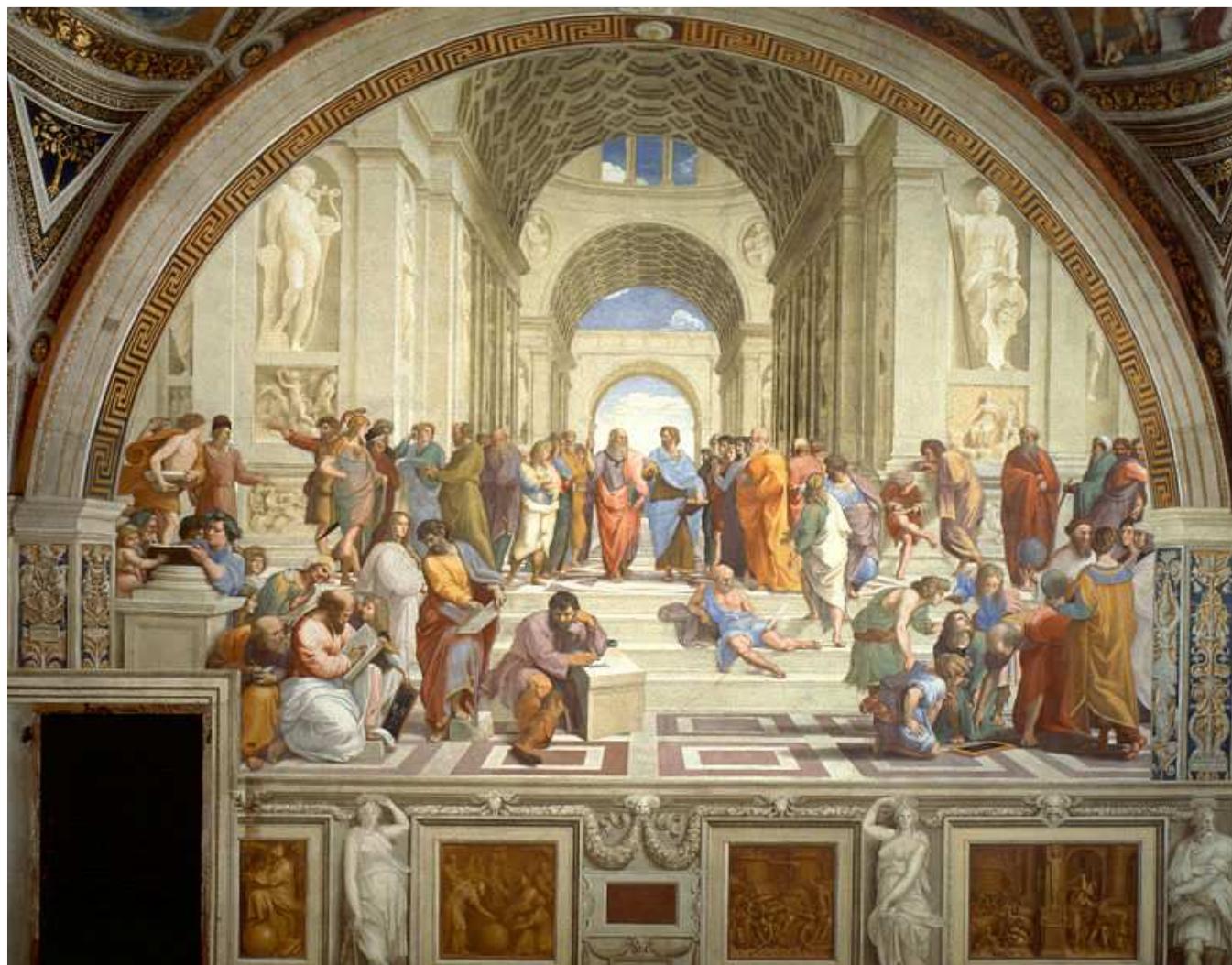


Typed Scheme

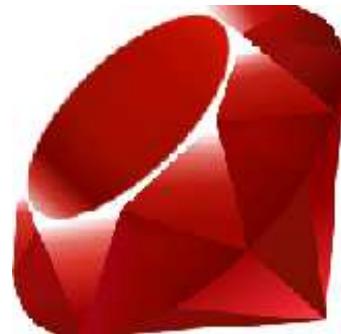
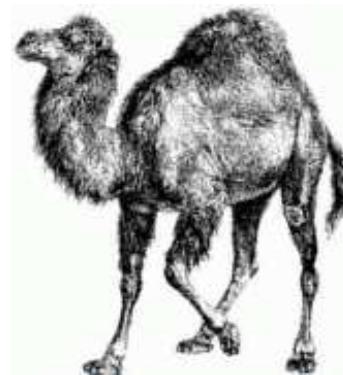
From Scripts to Programs

Sam Tobin-Hochstadt
Northeastern University

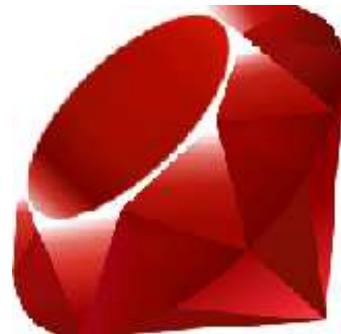
The PL Renaissance



The PL Renaissance



The PL Renaissance



What's good

These languages are

- interactive
- designed for rapid development
- supported by an active community
- modular
- higher-order

And they're exciting!

What's not so good

```
(define (main stx trace-flag super-expr  
         deserialize-id-expr name-id  
         interface-exprs defn-and-exprs))
```

```
(let-values (((this-id) #'this-id)  
           [(the-obj) (datum->syntax (quote-syntax here) (gensym 'self))]  
           [(the-finder) (datum->syntax (quote-syntax here) (gensym 'find-self))])  
(let* ([def-ctx (syntax-local-make-definition-context)]  
       [localized-map (make-bound-identifier-mapping)]  
       [any-localized? #f]  
       [localize/set-flag (lambda (id)  
                            (let ((id2 (localize id)))  
                              (unless (eq? id id2)  
                                (set! any-localized? #t))  
                              id2)))  
       [bind-local-id (lambda (id)  
                      (let ((l (localize/set-flag id)))  
                        (syntax-local-bind-syntaxes (list id) #f def-ctx)  
                        (bound-identifier-mapping-put!  
                         localized-map  
                         id  
                         l)))  
       [lookup-localize (lambda (id)  
                          (bound-identifier-mapping-get  
                           localized-map  
                           id  
                           (lambda ()  
                             ; If internal & external names are distinguished,  
                             ; we need to fall back to localize:  
                             (localize id))))])  
; ----- Expand definitions -----  
(let ([defn-and-exprs (expand-all-forms stx defn-and-exprs def-ctx bind-local-id)])  
  [bad (lambda (msg expr)  
        (raise-syntax-error #f msg stx expr))]  
  [class-name (if name-id  
                 (syntax-e name-id)  
                 (let ((s (syntax-local-infer-name stx)))  
                   (if (syntax? s)  
                       (syntax-e s)  
                       s))))]  
; ----- Basic syntax checks -----  
(for-each (lambda (stx)  
            (syntax-case stx (-init init-rest -field -init-field inherit-field  
                               private public override augrde  
                               public-final override-final augment-final  
                               pubment overment augment  
                               rename-super inherit inherit/super inherit/inner rename-inner  
                               inspect)  
            [(form orig idp ...)  
             (and (identifier? #'form)  
                  (or (free-identifier=? #'form (quote-syntax -init))  
                      (free-identifier=? #'form (quote-syntax -init-field))))])))) )
```

+ 900 lines

What's not so good

; Start here:

```
(define (main stx trace-flag super-expr  
          deserialize-id-expr name-id  
          interface-exprs defn-and-exprs))
```

```
(let-values (((this-id) #'this-id)  
           [(the-obj) (datum->syntax (quote-syntax here) (gensym 'self))]  
           [(the-finder) (datum->syntax (quote-syntax here) (gensym 'find-self))])  
(let* ([def-ctx (syntax-local-make-definition-context)]  
      [localized-map (make-bound-identifier-mapping)]  
      [any-localized? #f]  
      [localize/set-flag (lambda (id)  
                           (let ((id2 (localize id)))  
                             (unless (eq? id id2)  
                               (set! any-localized? #t))  
                             id2)))  
      [bind-local-id (lambda (id)  
                      (let ((l (localize/set-flag id)))  
                        (syntax-local-bind-syntaxes (list id) #f def-ctx)  
                        (bound-identifier-mapping-put!  
                         localized-map  
                         id  
                         l)))  
      [lookup-localize (lambda (id)  
                         (bound-identifier-mapping-get  
                          localized-map  
                          id  
                          (lambda ()  
                            ; If internal & external names are distinguished,  
                            ; we need to fall back to localize:  
                            (localize id))))])  
    ; ----- Expand definitions -----  
    (let ([defn-and-exprs (expand-all-forms stx defn-and-exprs def-ctx bind-local-id)])  
      [bad (lambda (msg expr)  
             (raise-syntax-error #f msg stx expr))]  
      [class-name (if name-id  
                     (syntax-e name-id)  
                     (let ((s (syntax-local-infer-name stx)))  
                       (if (syntax? s)  
                           (syntax-e s)  
                           s))))])  
    ; ----- Basic syntax checks -----  
    (for-each (lambda (stx)  
                (syntax-case stx (-init init-rest -field -init-field inherit-field  
                                         private public override augrde  
                                         public-final override-final augment-final  
                                         pubment overment augment  
                                         rename-super inherit inherit/super inherit/inner rename-inner  
                                         inspect)  
                [(form orig idp ...)  
                 (and (identifier? #'form)  
                      (or (free-identifier=? #'form (quote-syntax -init))  
                          (free-identifier=? #'form (quote-syntax -init-field))))])))) )
```

+ 900 lines

What's not so good

```
; main : stx bool stx           id  id stxs stxs -> stx
(define (main stx trace-flag super-expr
             deserialize-id-expr name-id
             interface-exps defn-and-exprs))
```

```
(let-values (((this-id) #'this-id)
            [(the-obj) (datum->syntax (quote-syntax here) (gensym 'self))]
            [(the-finder) (datum->syntax (quote-syntax here) (gensym 'find-self))])
  (let* ([def-ctx (syntax-local-make-definition-context)]
        [localized-map (make-bound-identifier-mapping)]
        [any-localized? #f]
        [localize/set-flag (lambda (id)
                             (let ((id2 (localize id)))
                               (unless (eq? id id2)
                                   (set! any-localized? #t))
                               id2)))
        [bind-local-id (lambda (id)
                         (let ((l (localize/set-flag id)))
                           (syntax-local-bind-syntaxes (list id) #f def-ctx)
                           (bound-identifier-mapping-put!
                             localized-map
                             id
                             l)))
        [lookup-localize (lambda (id)
                           (bound-identifier-mapping-get
                             localized-map
                             id
                             (lambda ()
                               ; If internal & external names are distinguished,
                               ; we need to fall back to localize:
                               (localize id))))])
    ; ----- Expand definitions -----
    (let ([defn-and-exprs (expand-all-forms stx defn-and-exprs def-ctx bind-local-id)])
      [bad (lambda (msg expr)
             (raise-syntax-error #f msg stx expr))]
      [class-name (if name-id
                     (syntax-e name-id)
                     (let ((s (syntax-local-infer-name stx)))
                       (if (syntax? s)
                           (syntax-e s)
                           s))))]
    ; ----- Basic syntax checks -----
    (for-each (lambda (stx)
                (syntax-case stx (-init init-rest -field -init-field inherit-field
                                         private public override augrde
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                                         pubment overment augment
                                         rename-super inherit inherit/super inherit/inner rename-inner
                                         inspect)
                [(form orig idp ...)
                 (and (identifier? #'form)
                      (or (free-identifier=? #'form (quote-syntax -init))
                          (free-identifier=? #'form (quote-syntax -init-field))))])))) )
```

+ 900 lines

What's not so good

```
; main : stx bool stx (or #f id) id stxs stxs -> stx
(define (main stx trace-flag super-expr
             deserialize-id-expr name-id
             interface-exps defn-and-exprs))
```

```
(let-values (((this-id) #'this-id)
            [(the-obj) (datum->syntax (quote-syntax here) (gensym 'self))]
            [(the-finder) (datum->syntax (quote-syntax here) (gensym 'find-self))])
  (let* ([def-ctx (syntax-local-make-definition-context)]
        [localized-map (make-bound-identifier-mapping)]
        [any-localized? #'f]
        [localize/set-flag (lambda (id)
                             (let ((id2 (localize id)))
                               (unless (eq? id id2)
                                   (set! any-localized? #t))
                               id2)))
        [bind-local-id (lambda (id)
                         (let ((l (localize/set-flag id)))
                           (syntax-local-bind-syntaxes (list id) #f def-ctx)
                           (bound-identifier-mapping-put!
                             localized-map
                             id
                             l)))
        [lookup-localize (lambda (id)
                           (bound-identifier-mapping-get
                             localized-map
                             id
                             (lambda ()
                               ; If internal & external names are distinguished,
                               ; we need to fall back to localize:
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    ; ----- Expand definitions -----
    (let ([defn-and-exprs (expand-all-forms stx defn-and-exprs def-ctx bind-local-id)])
      [bad (lambda (msg expr)
             (raise-syntax-error #'f msg stx expr))]
      [class-name (if name-id
                     (syntax-e name-id)
                     (let ((s (syntax-local-infer-name stx)))
                       (if (syntax? s)
                           (syntax-e s)
                           s))))]
    ; ----- Basic syntax checks -----
    (for-each (lambda (stx)
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                                         private public override augrde
                                         public-final override-final augment-final
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                [(form orig idp ...)
                 (and (identifier? #'form)
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                          (free-identifier=? #'form (quote-syntax -init-field))))])))) )
```

+ 900 lines

What's not so good

```
(: main (Stx Bool Stx (U #f Id) Id Stxs Stxs -> Stx))  
(define (main stx trace-flag super-expr  
           deserialize-id-expr name-id  
           interface-exprs defn-and-exprs))
```

```
(let-values (((this-id) #'this-id)  
           [(the-obj) (datum->syntax (quote-syntax here) (gensym 'self))]  
           [(the-finder) (datum->syntax (quote-syntax here) (gensym 'find-self))])  
(let* ([def-ctx (syntax-local-make-definition-context)]  
       [localized-map (make-bound-identifier-mapping)]  
       [any-localized? #f]  
       [localize/set-flag (lambda (id)  
                           (let ((id2 (localize id)))  
                             (unless (eq? id id2)  
                               (set! any-localized? #t))  
                             id2)))  
       [bind-local-id (lambda (id)  
                       (let ((l (localize/set-flag id)))  
                         (syntax-local-bind-syntaxes (list id) #f def-ctx)  
                         (bound-identifier-mapping-put!  
                          localized-map  
                          id  
                          l)))  
       [lookup-localize (lambda (id)  
                         (bound-identifier-mapping-get  
                           localized-map  
                           id  
                           (lambda ()  
                             ; If internal & external names are distinguished,  
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(let ([defn-and-exprs (expand-all-forms stx defn-and-exprs def-ctx bind-local-id)])  
   [bad (lambda (msg expr)  
          (raise-syntax-error #f msg stx expr))]  
   [class-name (if name-id  
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                  (let ((s (syntax-local-infer-name stx)))  
                    (if (syntax? s)  
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(for-each (lambda (stx)  
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                                pubment overment augment  
                                rename-super inherit inherit/super inherit/inner rename-inner  
                                inspect)  
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             (and (identifier? #'form)  
                  (or (free-identifier=? #'form (quote-syntax -init))  
                      (free-identifier=? #'form (quote-syntax -init-field))))])))) )
```

+ 900 lines

Module-by-module porting of code from an untyped language to a typed sister language allows for an easy transition from untyped scripts to typed programs.

Module-by-module porting of code from an untyped language to a typed sister language allows for an easy transition from untyped scripts to typed programs.

*Module-by-module porting of code from an untyped language to a **typed sister language** allows for an easy transition from untyped scripts to typed programs.*

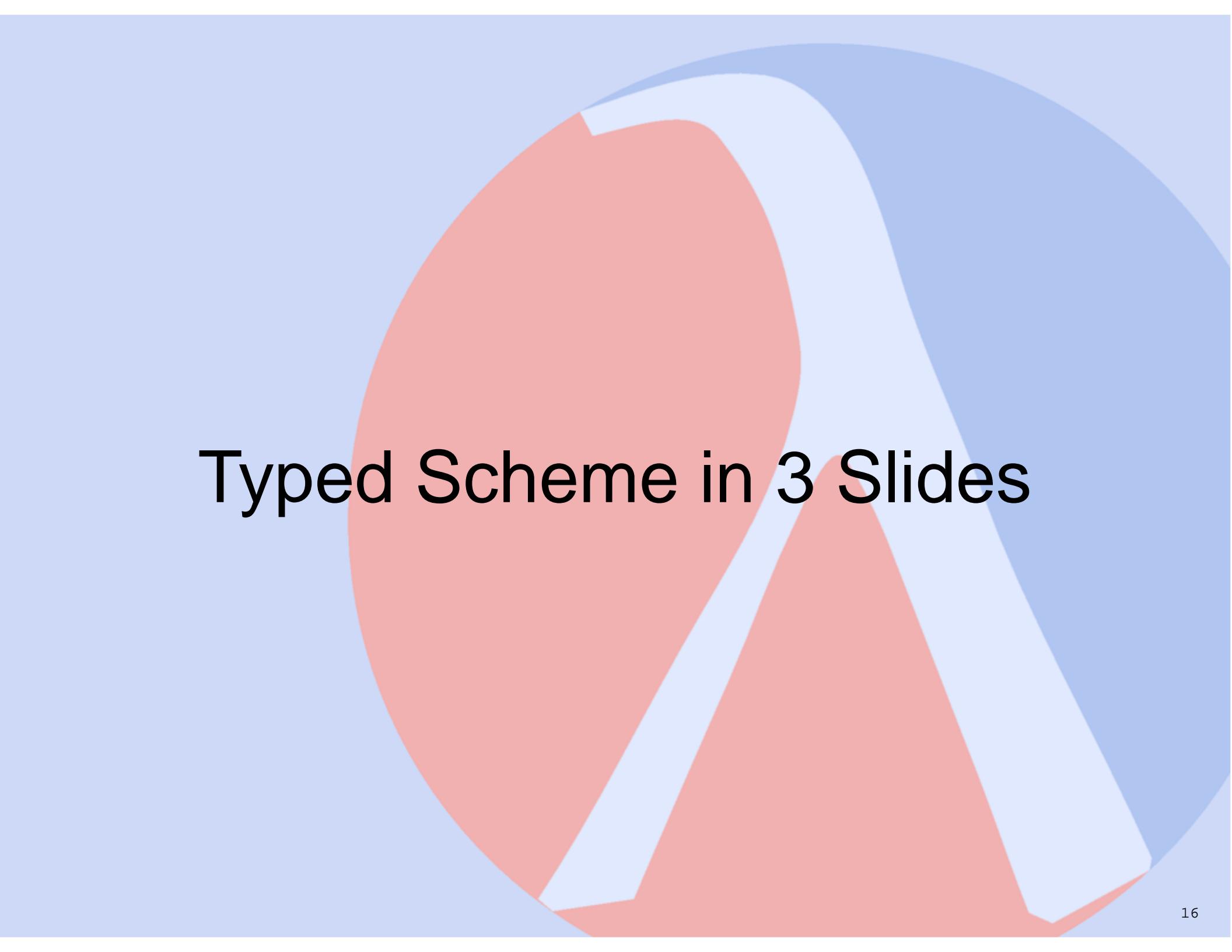
*Module-by-module porting of code from an untyped language to a typed sister language allows for an **easy transition** from untyped scripts to typed programs.*

Why PLT Scheme?

Modules

Contracts

Abstractions



Typed Scheme in 3 Slides

Hello World

```
#lang scheme hello  
(printf "Hello World\n")
```

Hello World

```
#lang typed-scheme
```

```
hello
```

```
(printf "Hello World\n")
```

Functions

#lang

scheme

ack

```
; ack : Integer Integer -> Integer
(define (ack m n)
  (cond [(<= m 0) (+ n 1)]
        [(<= n 0) (ack (- m 1) 1)]
        [else (ack (- m 1) (ack m (- n 1))))])))

(ack 2 3)
```

Functions

```
#lang typed-scheme
```

```
ack
```

```
(: ack (Integer Integer -> Integer))
(define (ack m n)
  (cond [(<= m 0) (+ n 1)]
        [(<= n 0) (ack (- m 1) 1)]
        [else (ack (- m 1) (ack m (- n 1))))])))

(ack 2 3)
```

Modules

#lang

scheme

ack

```
; ack : Integer Integer -> Integer
(define (ack m n)
  (cond [(<= m 0) (+ n 1)]
        [(<= n 0) (ack (- m 1) 1)]
        [else (ack (- m 1) (ack m (- n 1))))]))
```

#lang

scheme

compute

```
(require ack)

(ack 2 3)
```

```
#lang typed-scheme
```

ack

```
(: ack (Integer Integer -> Integer))
(define (ack m n)
  (cond [(<= m 0) (+ n 1)]
        [(<= n 0) (ack (- m 1) 1)]
        [else (ack (- m 1) (ack m (- n 1))))]))
```

```
#lang scheme
```

compute

```
(require ack)
```

```
(ack 2 3)
```

#lang

scheme

ack

```
; ack : Integer Integer -> Integer
(define (ack m n)
  (cond [(<= m 0) (+ n 1)]
        [(<= n 0) (ack (- m 1) 1)]
        [else (ack (- m 1) (ack m (- n 1))))]))
```

#lang typed-scheme

compute

```
(require [ack
          (Integer Integer -> Integer)])
(ack 2 3)
```

```
#lang typed-scheme
```

ack

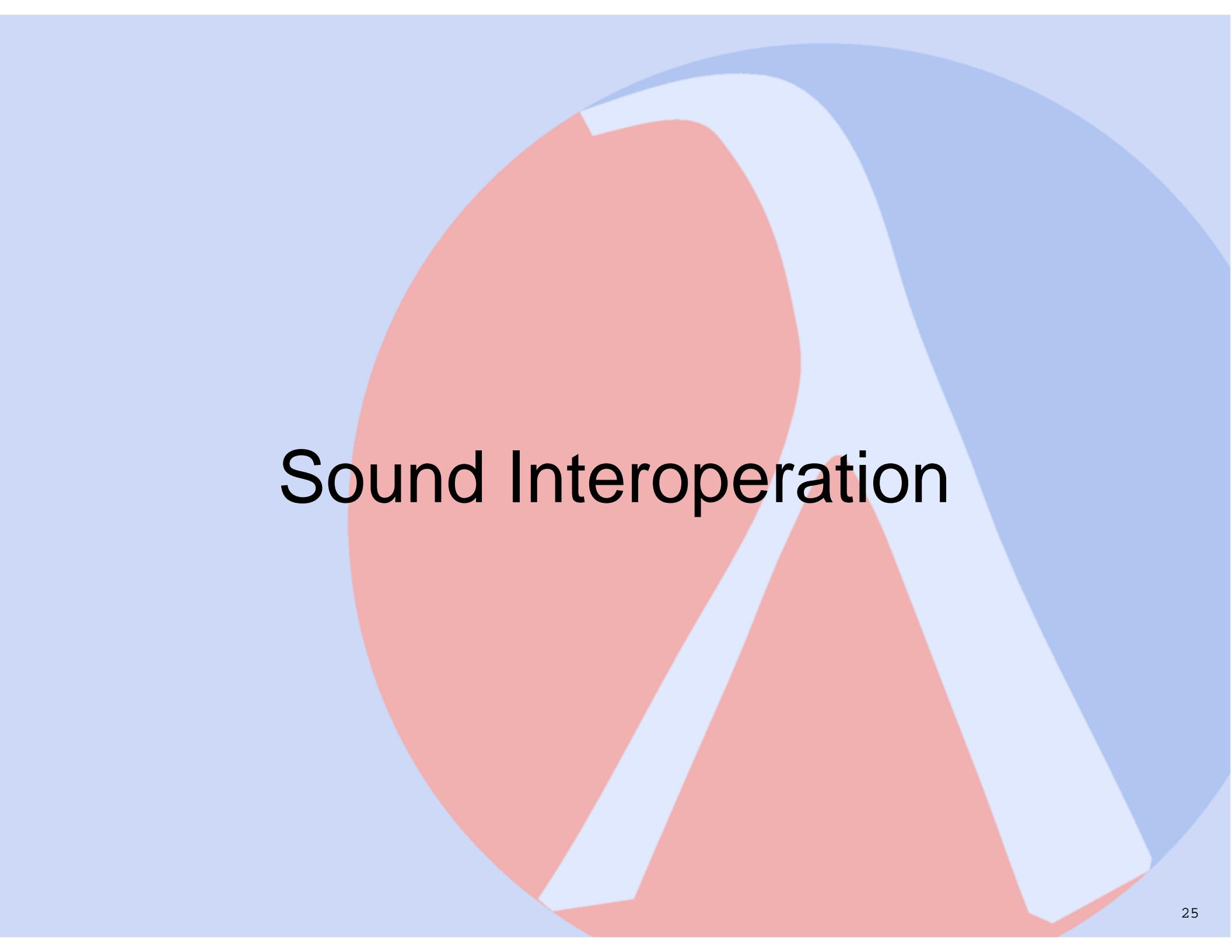
```
(: ack (Integer Integer -> Integer))
(define (ack m n)
  (cond [(<= m 0) (+ n 1)]
        [(<= n 0) (ack (- m 1) 1)]
        [else (ack (- m 1) (ack m (- n 1))))]))
```

```
#lang typed-scheme
```

compute

```
(require ack)
```

```
(ack 2 3)
```



Sound Interoperation

Typed & Untyped

```
#lang typed-scheme
```

server

```
( : add5 (Number -> Number) )  
(define (add5 x) (+ x 5))
```

```
#lang
```

scheme

client

```
(require server)  
(add5 7)
```

Typed & Untyped

Untyped code can make mistakes

```
#lang typed-scheme
```

server

```
( : add5 (Number -> Number) )  
(define (add5 x) (+ x 5))
```

```
#lang
```

scheme

client

```
(require server)  
(add5 "seven")
```

Typed & Untyped

Untyped code can make mistakes

```
#lang typed-scheme
```

server

```
( : add5 (Number -> Number) )  
(define (add5 x) (+ x 5))
```

```
#lang
```

scheme

client

```
(require server)  
(add5 "seven")
```

+ : expects type <number> as 1st argument

Typed & Untyped

Catch errors dynamically at the boundary

```
#lang typed-scheme
```

server

```
( : add5 (Number -> Number) )  
(define (add5 x) (+ x 5))
```

```
#lang
```

scheme

client

```
(require server)  
(add5 "seven")
```

client broke the contract on add5

Typed & Untyped

Catch errors dynamically at the boundary

#lang

scheme

server

```
(define (add5 x) "x plus 5")
```

#lang typed-scheme

client

```
(require server
          [ add5 (Number -> Number) ] )
(add5 7)
```

server interface broke the contract on add5

Typed & Untyped

Catch errors dynamically at the boundary

```
#lang typed-scheme server
(: addx (Number -> (Number -> Number)))
(define (addx x) (lambda (y) (+ x y)))
```

```
#lang scheme client
(require server)
((addx 7) 'bad)
```

client broke the contract on add5

The Blame Theorem

If the program raises a contract error, the blame is not assigned to a typed module.

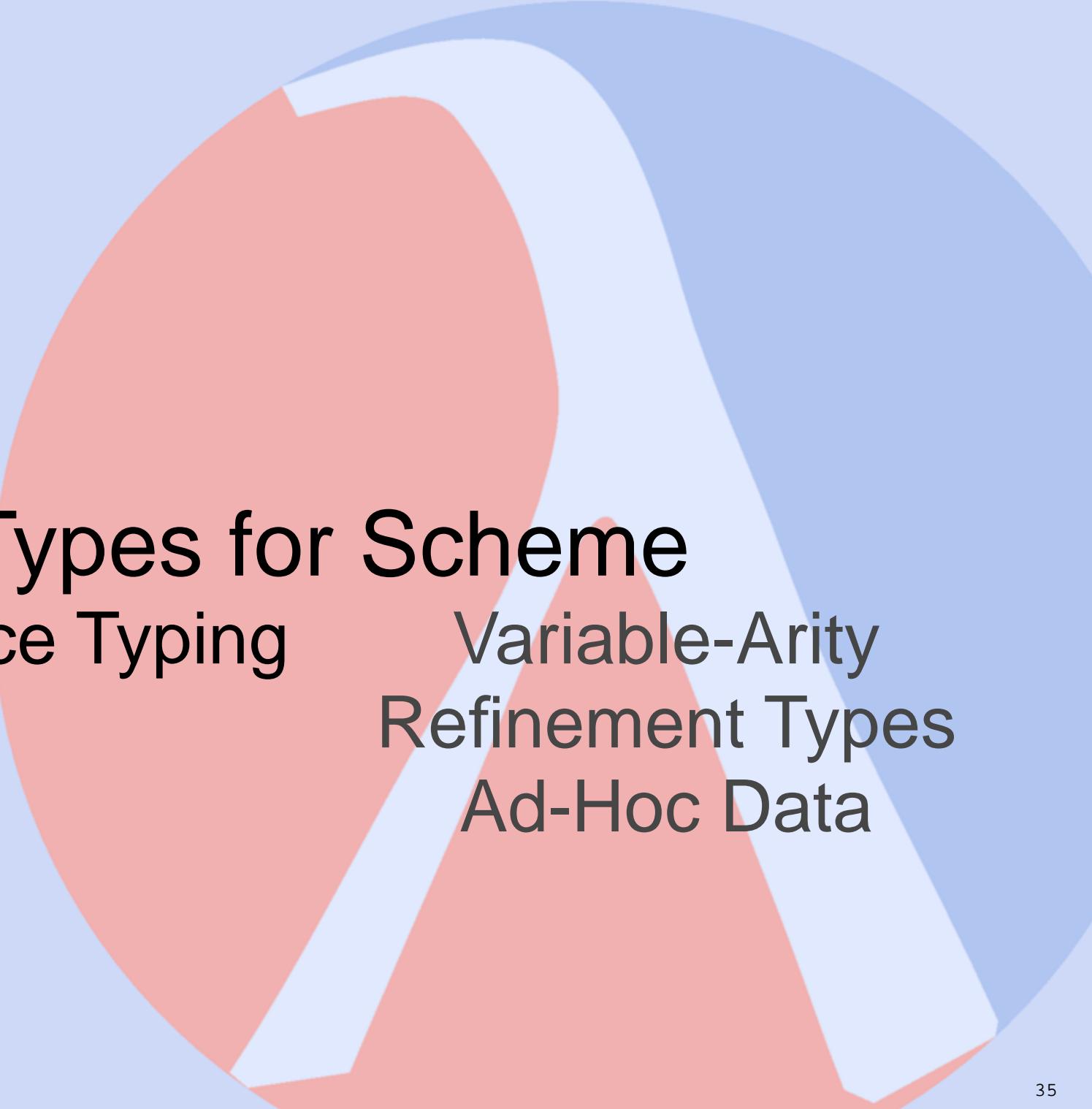
The Blame Theorem

Well-typed modules can't get blamed.

The Blame Theorem

Allows local reasoning about typed modules,
without changing untyped modules.

Choose how much static checking you want.



Types for Scheme

Occurrence Typing Variable-Arity
 Refinement Types
 Ad-Hoc Data

Types for Scheme

```
#lang typed-scheme  
  
( : f (Any -> Number) )  
(define (f x)  
  (if (number? x)  
      (add1 x)  
      0))
```

occur

Types for Scheme

```
#lang typed-scheme
```

```
refine
```

```
(: check (String -> (Refinement sql-safe?)))  
(define (check s)  
  (if (sql-safe? s)  
      s  
      (error "unsafe string!")))
```

Types for Scheme

```
#lang typed-scheme
```

union

```
(define-type-alia BT
  (U Number (Pair BT BT)))
(: sizeof (BT -> Number))
(define (sizeof b)
  (if (number? b)
      1
      (+ 1 (sizeof (car b)) (sizeof (cdr b))))))
```

Types for Scheme

```
#lang typed-scheme
```

varar

```
(: wrap ( $\forall$  (B A ...)  
          ((A ... -> B) -> (A ... -> B))))  
(define (wrap f)  
  (lambda args  
    (printf "args are: ~a\n" args)  
    (apply f args)))
```

Scheme Idioms

#lang scheme **number?**

```
(define (f x)
  (if (number? x)
      (add1 x)
      0))
```

Filters & Objects

```
#lang typed-scheme
```

```
number?
```

```
( : f (Any -> Number) )  
(define (f x)  
  (if (number? x)  
      (add1 x)  
      0))
```

Filters & Objects

```
#lang typed-scheme
```

```
number?
```

```
( : f (Any -> Number) )  
(define (f x) type: Any  
  (if (number? x)  
      (add1 x)  
      0))
```

Filters & Objects

```
#lang typed-scheme
```

```
number?
```

```
( : f (Any -> Number) )  
(define (f x)  
  (if (number? x)  
      (add1 x)  
      0))
```

type: Any

Filters & Objects

```
#lang typed-scheme
```

```
number?
```

```
( : f (Any -> Number) )  
(define (f x)  
  (if (number? x)  
      (add1 x)  
      0))
```

type: Number

Filters & Objects

```
#lang typed-scheme
```

```
number?
```

```
( : f (Any -> Number) )  
(define (f x)  
  (if (number? x)  
      (add1 x)  
      0))
```

```
type: (Any -> Boolean : Number)
```

Filters & Objects

```
#lang typed-scheme
```

```
number?
```

```
( : f (Any -> Number) )  
(define (f x)  
  (if (number? x)  
      (add1 x)  
      0))
```

type: Any
object: x

Filters & Objects

```
#lang typed-scheme
```

```
number?
```

```
( : f (Any -> Number) )  
(define (f x)  
  (if (number? x)  
      (add1 x)  
      0))
```

type: Boolean

filter: (apply-filter Number x)

Filters & Objects

```
#lang typed-scheme
```

```
number?
```

```
( : f (Any -> Number) )  
(define (f x)  
  (if (number? x)  
      (add1 x)  
      0))
```

type: Boolean
filter: Number_x

Filters & Objects

```
#lang typed-scheme
```

```
number?
```

```
( : f (Any -> Number) )  
(define (f x)  
  (if (number? x)  
      (add1 x)  
      0))
```

env: x:Any + Number_x

Filters & Objects

```
#lang typed-scheme
```

```
number?
```

```
( : f (Any -> Number) )  
(define (f x)  
  (if (number? x)  
      (add1 x)  
      0))
```

env: x:Number
type: Number

Scheme Idioms

```
#lang scheme  
else  
;  
; s is a symbol, number or string  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

Then & Else

```
#lang typed-scheme  
else  
( : ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

Then & Else

```
#lang typed-scheme  
  
(: ->string ((U Symbol Number String) type: (U Symbol Number String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

else

Then & Else

```
#lang typed-scheme
```

```
( : ->string ((U Symbol Number String) -> string))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

else

type: Symbol

Then & Else

```
#lang typed-scheme  
else  
( : ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))  
type: (U Number String)
```

Then & Else

```
#lang typed-scheme  
  
(: ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

else

type: Number

Then & Else

```
#lang typed-scheme  
else  
( : ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

type: String

Then & Else

```
#lang typed-scheme
```

```
else
```

```
( : ->string ( type: (Any -> Boolean : Symbol | Symbol)
(define (->string? s,
  (cond [(symbol? s) (symbol->string s)]
        [(number? s) (number->string s)]
        [else s]))
```

Then & Else

```
#lang typed-scheme  
else  
( : ->string ((U Symbols)  
type: Boolean  
filter: Symbolss | Symbolss)  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

Then & Else

```
#lang typed-scheme  
else  
( : ->string  
  env: s:(U Symbol Number String) + Symbols  
(define (string->s  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

Then & Else

```
#lang typed-scheme  
  
(: ->string ((U Symbol env: s:Symbol) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

else

env: s:Symbol

Then & Else

```
#lang typed-scheme  
else  
( : ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

nv: s:(U Symbol Number String) + Symbol_s

Then & Else

```
#lang typed-scheme  
else  
( : ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

env: s:(U Number String)

Then & Else

```
#lang typed-scheme  
else  
( : ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else]))  
type: (Any -> Boolean : Number | Number)
```

Then & Else

```
#lang typed-scheme  
  
(: ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

else

type: Boolean
filter: Number_s | Number_s

Then & Else

```
#lang typed-scheme  
else  
( : ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else]))  
env: s:(U Number String) + Numbers
```

Then & Else

```
#lang typed-scheme  
  
(: ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

else

env: s:Number

Then & Else

```
#lang typed-scheme  
  
(: ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))
```

env: s:(U Number String) + Number_s

Then & Else

```
#lang typed-scheme  
else  
( : ->string ((U Symbol Number String) -> String))  
(define (->string s)  
  (cond [(symbol? s) (symbol->string s)]  
        [(number? s) (number->string s)]  
        [else s]))  
  
env: s:String
```

Scheme Idioms

```
#lang scheme  
; g : Any (U String Number) -> Number  
(define (g x y)  
  (cond [(and (number? x) (string? y))  
         (+ x (string-length y))]  
        [(number? x) (+ x y)]  
        [else y]))
```

and

Logical Reasoning

```
#lang typed-scheme  
(: g (Any (U Number String) -> Number))  
(define (g x y)  
  (cond [(and (number? x) (string? y))  
         (+ x (string-length y))]  
        [(number? x) (+ x y)]  
        [else y]))
```

and

Logical Reasoning

```
#lang typed-scheme
(: g (filter: Numberx | Numberx) )
(define (g x y)
  (cond [(and (number? x) (string? y))
          (+ x (string-length y))]
        [(number? x) (+ x y)]
        [else y]))
```

and

Logical Reasoning

```
#lang typed-scheme  
(: g (Any (U Number Stringy))  
  filter: Stringy | Stringy)  
and  
(define (g x y)  
  (cond [(and (number? x) (string? y))  
          (+ x (string-length y))]  
        [(number? x) (+ x y)]  
        [else y]))
```

Logical Reasoning

```
#lang typed-scheme  
(filter: Numberx Stringy |  
  and (Number? x) (String? y))  
  (+ x (string-length y)))  
  [(+ x y)]  
  [else y]))
```

and

Logical Reasoning

```
#lang typed-scheme  
(filter: Numberx Stringy | Numberx ⊇ Stringy)  
(define (f x y)  
  (cond [(and (number? x) (string? y))  
          (+ x (string-length y))]  
    [(number? x) (+ x y)]  
    [else y]))
```

and

Logical Reasoning

```
#lang typed-scheme  
(: g (Any (U Number String) -> Number))  
(define (g x y)  
  (cond [(and (number? x) (string? y))  
         (+ x (string-length y))]  
        [(number? x) (+ x y)]  
        [else y]))
```

and

env: $\text{Number}_x \supset \text{String}_y$
filter: Number_x

Logical Reasoning

```
#lang typed-scheme  
(: g (Any (U Number String) -> Number))  
(define (g x y)  
  (cond [(and (number? x) (string? y))  
         (+ x (string-length y))]  
        [(number? x) (+ x y)]  
        [else y]))
```

and

env: $\text{Number}_x \supset \overline{\text{String}_y}$
filter: $\text{Number}_x \text{ } \overline{\text{String}_y}$

Logical Reasoning

```
#lang typed-scheme  
(: g (Any (U Number String) -> Number))  
(define (g x y)  
  (cond [(and (number? x) (string? y))  
         (+ x (string-length y))]  
        [(number? x) (+ x y)]  
        [else (error "bad arguments")]))
```

and

env: x: Any y: (U Number String) + Number_x String_y

Logical Reasoning

```
#lang typed-scheme  
(: g (Any (U Number String) -> Number))  
(define (g x y)  
  (cond [(and (number? x) (string? y))  
         (+ x (string-length y))]  
        [(number? x) (+ x y)]  
        [else (error "bad arguments")]))
```

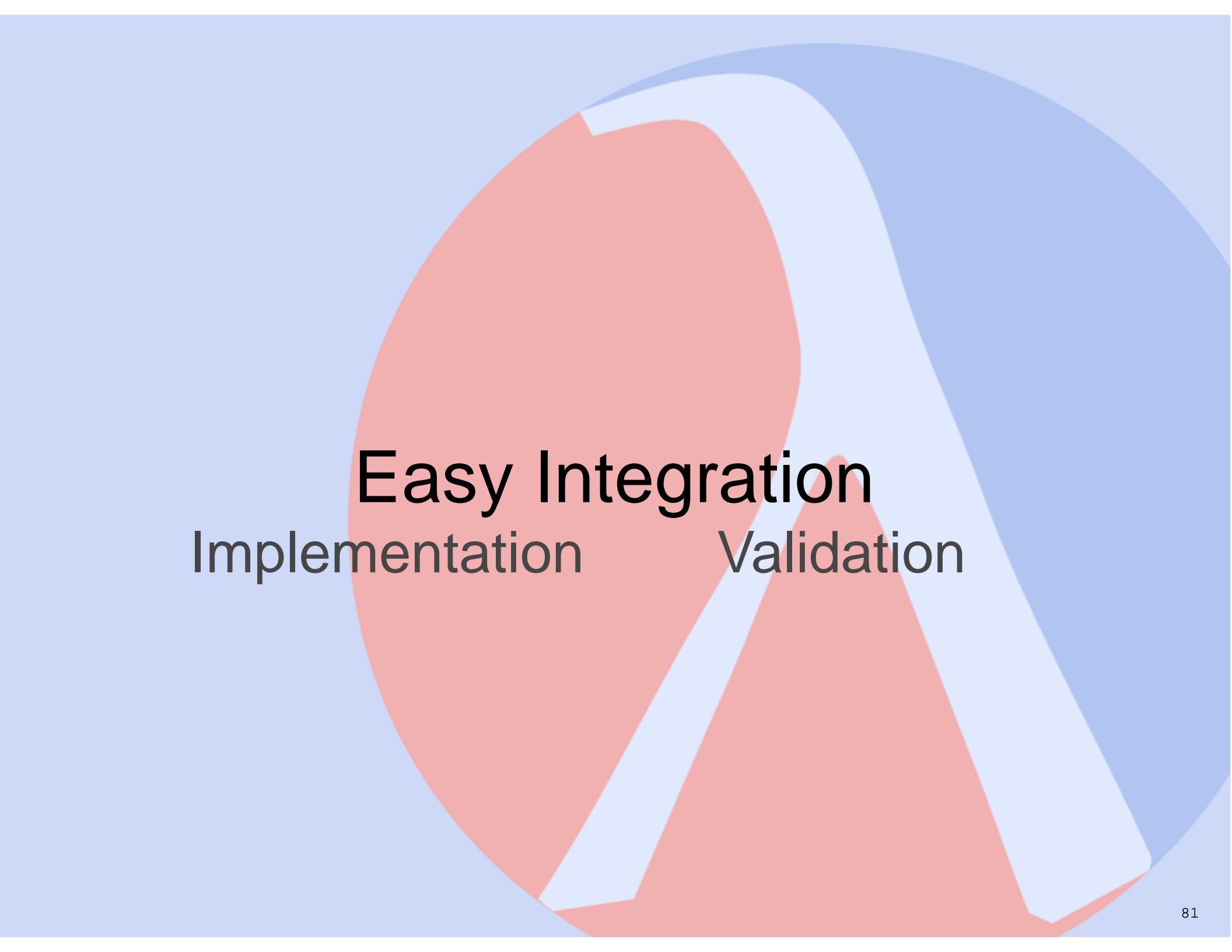
and

env: x:Number y:Number

All Together Now

```
#lang typed-scheme

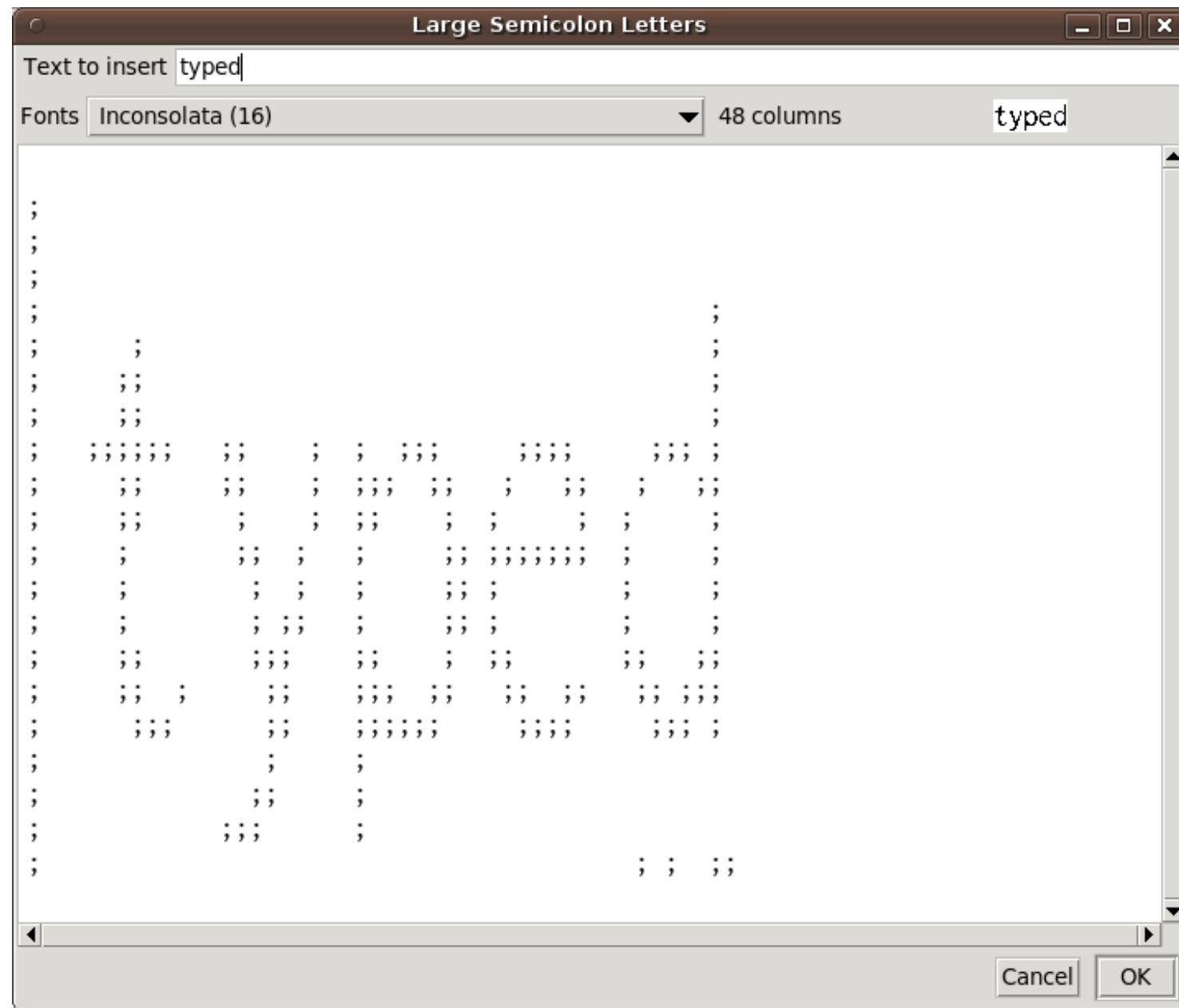
(: f ((U Number String) (Pair Any Any) -> Number))
(define (f input extra)
  (cond
    [(and (number? input) (number? (car extra)))
     (+ input (car extra))]
    [(number? (car extra))
     (+ (string-length input) (car extra))]
    [else 0]))
```



Easy Integration

Implementation Validation

Implementation



Implementation

```
#lang typed-scheme tslide  
  
(: subtitle-pict : (String -> Pict))  
(define (subtitle-pict s)  
  (text s (current-title-font) large-text-size))
```

Validation

	Squad	Metrics	Acct	Spam	System	Rand	Total
Lines	2369	511	407	315	1290	618	5510
Increase	7%	25%	7%	6%	1%	3%	7%
Fixes (Good)	5	3	4	5	8	0	25
Problems (Bad)	7	4	3	1	0	1	16

Sample Fixes

```
#lang
```

```
scheme
```

```
assert
```

```
(+ 10 (string->number str)))
```

Sample Fixes

```
#lang typed-scheme           assert  
  
(+ 10 (assert (string->number str))))
```

Sample Fixes

```
#lang
```

```
scheme
```

```
div
```

```
(define (divs . args)
  (* -1 (apply / args))))
```

Sample Fixes

```
#lang typed-scheme           div

(define (divs arg . args)
  (* -1 (apply / arg args)))
```

Sample Problems

#lang	scheme	cond
	(cond [(< x 0) 'negative] [(= x 0) 'zero] [(> x 0) 'positive])	

Sample Problems

```
#lang typed-scheme  
  
(cond [(< x 0) 'negative]  
      [(= x 0) 'zero]  
      [else 'positive])
```

cond

Sample Problems

#lang scheme

mutate

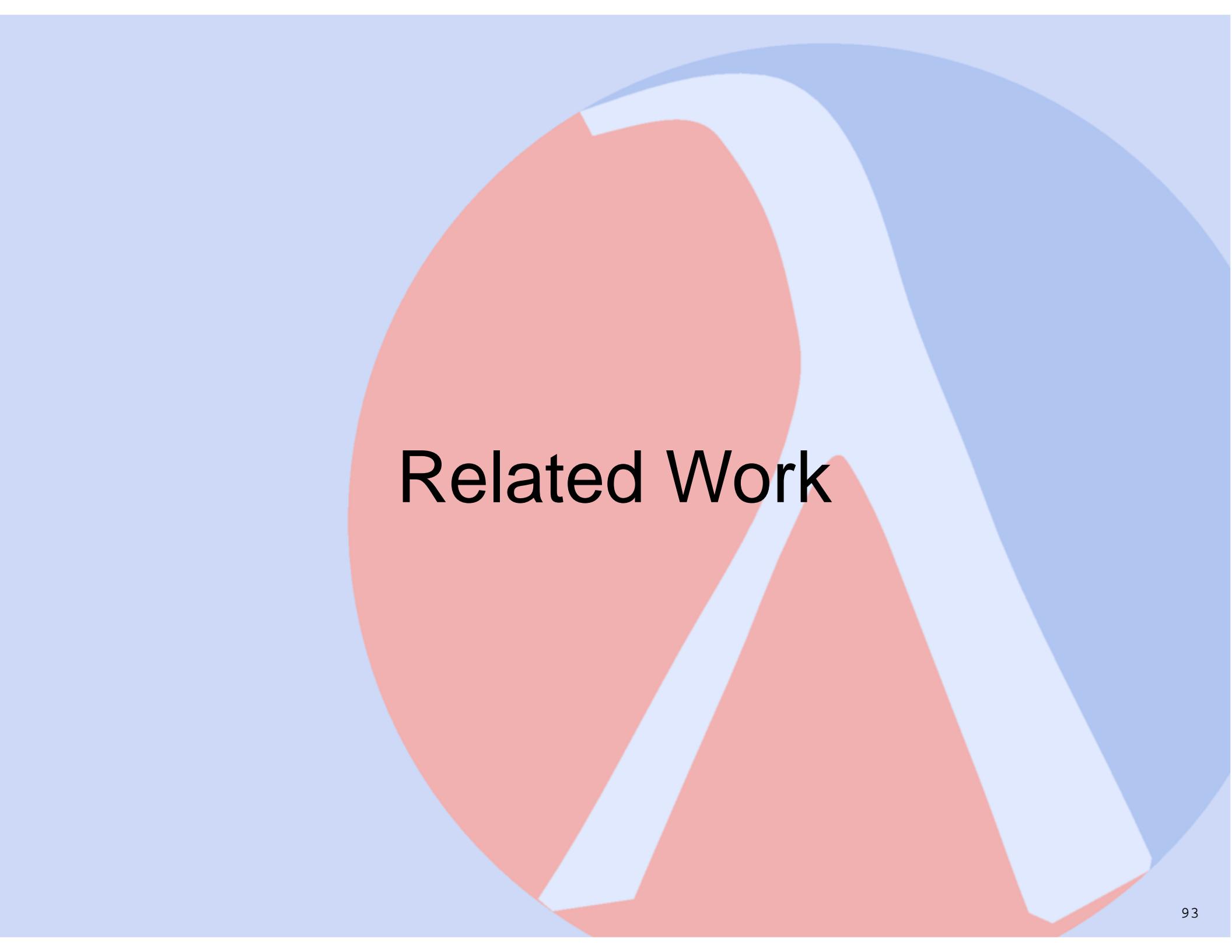
```
(define pr (make-pair x y))
(when (string? (pair-left pr))
  (set-pair-left! pr (string->symbol (pair-left pr))))
```

Sample Problems

```
#lang typed-scheme
```

mutate

```
(define pr (make-pair
  (if (string? x) (string->number x) x)
  y))
```



Related Work

Interlanguage Integration

ProfessorJ

Gray et al. (2005)

Multilanguage Systems

Matthews and Findler (2007)

Types for Untyped Languages

John Reynolds (1968)

"Some account should be taken of the premises
in conditional expressions."

Soft Typing

Types for Scheme

Strongtalk

Types for Untyped Languages

John Reynolds (1968)

Soft Typing

Fagan (1991), Aiken (1994)

Wright (1997), Flanagan (1999)

Types for Scheme

Strongtalk

Types for Untyped Languages

John Reynolds (1968)

Soft Typing

Types for Scheme

SPS (Wand 1984), Leavens (2005)

Infer (Haynes 1995)

Strongtalk

Types for Untyped Languages

John Reynolds (1968)

Soft Typing

Types for Scheme

Strongtalk

Bracha and Griswold (1993)

Contracts & Modules

Contracts

Findler & Fellesien (2002)

Modules with Macros

Flatt (2002)

Gradual Typing

Siek et al (2006-2009), Wadler & Findler (2007),
Herman et al (2007)

DRuby

Furr et al (2009)

Conclusion

Module-by-module porting of code from an untyped language to a typed sister language allows for an easy transition from untyped scripts to typed programs.

Sound Typed-Untyped Interoperation

Type System for Scheme

Full-scale Implementation

Empirical Validation

Try Typed Scheme

Installer and Documentation
<http://www.plt-scheme.org>

Thanks to Olin Shivers

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Installer and Documentation
<http://www.plt-scheme.org>

Thanks to Aaron Turon

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<http://www.plt-scheme.org>

Thanks to Felix Klock

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Thanks to James Hamblin

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Thanks to James Jungbauer

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Thanks to Dan Brown

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Thanks to Lazlo Babai

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Thanks to Stevie Strickland

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Thanks to Guy Steele

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Thanks to Robby Findler

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Thanks to Sukyoung Ryu

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Thanks to Carl Eastlund

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Thanks to Eric Allen

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Thanks to Ivan Gazeau

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Thanks to Katie Edmonds

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Thanks to Mitch Wand

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Thanks to Dave Herman

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Thanks to Jan-Willem Maessen

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Thanks to Matthias Felleisen

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Thanks to Ryan Culpepper

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Thanks to Vincent St-Amour

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Thanks to Jesse Tov

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Thanks to Christine Flood

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Thanks to David Chase

Try Typed Scheme

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<http://www.plt-scheme.org>

Thanks to Elizabeth Tobin

Try Typed Scheme

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<http://www.plt-scheme.org>

Thanks to Victor Luchangco

Try Typed Scheme

Installer and Documentation
<http://www.plt-scheme.org>

Thanks to Ryan Culpepper

Occurrence Typing

- Done, and more

Variable-arity Polymorphism

- Done

Keyword and Optional Arguments

- Done: Use & Import/Export
- Not Done: Definition

Validation

- Some Done