Homework Module 8

1 Submission Rules

http://www.ccs.neu.edu/home/lieber/courses/algorithms/ cs5800/sp14/homeworks/submission-rules.pdf

2 Problems

- 1. (30 pts) Write a two page summary of all concepts and techniques in CLRS Chapter 10 (Elementary Datastructures).
- (30 pts) Write a two page summary of all concepts and techniques in CLRS Chapter 12 (Binary Search Trees).

The next 3 problems ask for pseudo code.

- 3. (10 pts) Exercise 10.1-6. (Simulate queue with two stacks)
- 4. (10 pts) Exercise 10.1-7. (Simulate stack with two queues)
- 5. (10 pts) Exercise 10.2-2. (Simulate stack with singly linked list)
- 6. (10 pts) Exercise 10.2-6. (UNION)
- 7. (10 points)

Debate the following claim and turn in your winning strategy.

Claim PascalTriangleAsymptotics: For all k in Nat Exists c in Nat binomial(n,k) is $\Theta(n^c)$.

This is in reaction to the midterm where some wrote $binomial(n,3) = \Theta(2^n)$ or $\Theta(n!)$.

8. (10 points)

Consider the following from the earlier HSR homework:

 $\label{eq:http://www.ccs.neu.edu/home/lieber/courses/algorithms/cs5800/sp14/labs/HSR-problem-CS5800-1.pdf$

HSR(n,k,q) = Exists T:DecisionTree(n,k,q) ForAll m in [0..n-1]: T correctly finds m (the highest safe rung) with at most q decisions. DecisionTree(n,k,q): A decision tree for HSR(n,k,q) must satisfy the following properties: 1) there are at most k yes from the root to any leaf. 2) the longest root-leaf path has q edges. 3) each rung 1..n-1

appears exactly once as internal node of the tree. 4) each rung 0..n-1 appears exactly once as a leaf.

Your task is to add a 5th property to the above 4 properties of DecisionTree(n,k,q) calling the new concept DecisionTree2(n,k,q) so that

HSR2(n,k,q) = Exists T:DecisionTree2(n,k,q): T correctly finds the highest safe rung with at most q decisions.

Debate the following claim and turn in your proof: For All n,k,q in Nat: $\mathrm{HSR}(n,k,q)$ if and only if $\mathrm{HSR2}(n,k,q)$.