

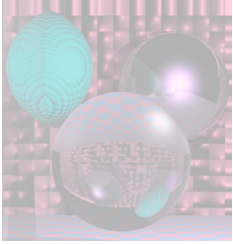
CS G140

Graduate Computer Graphics

Prof. Harriet Fell

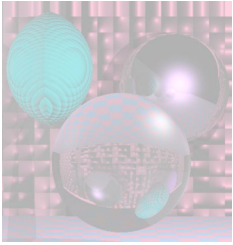
Spring 2009

Lecture 1 - January 7, 2009

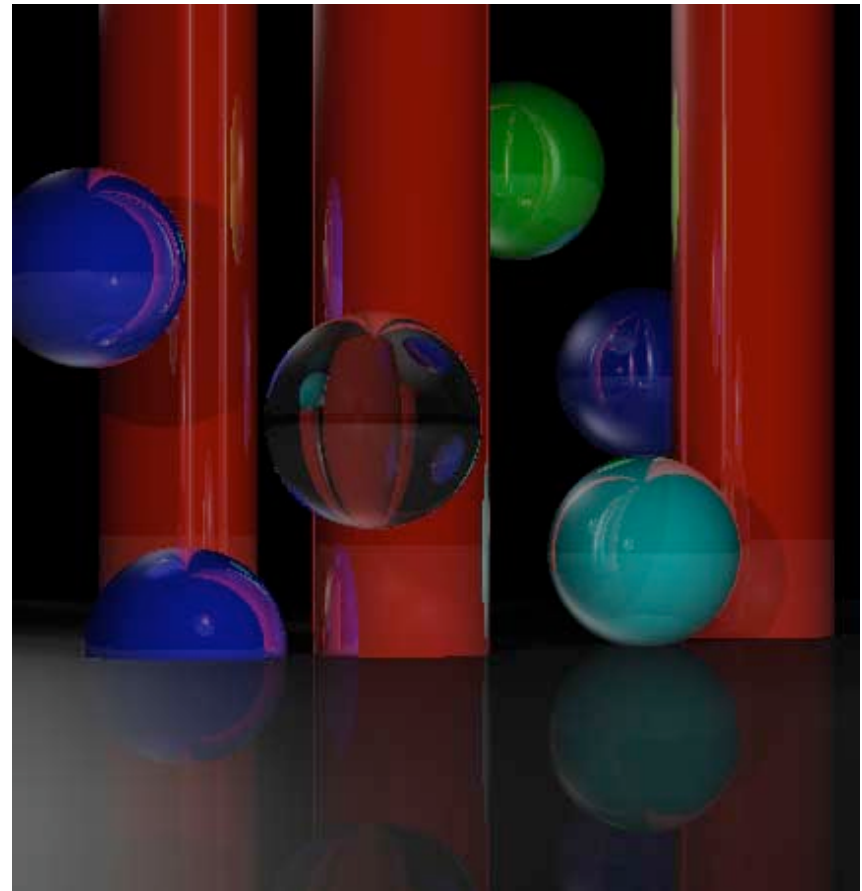
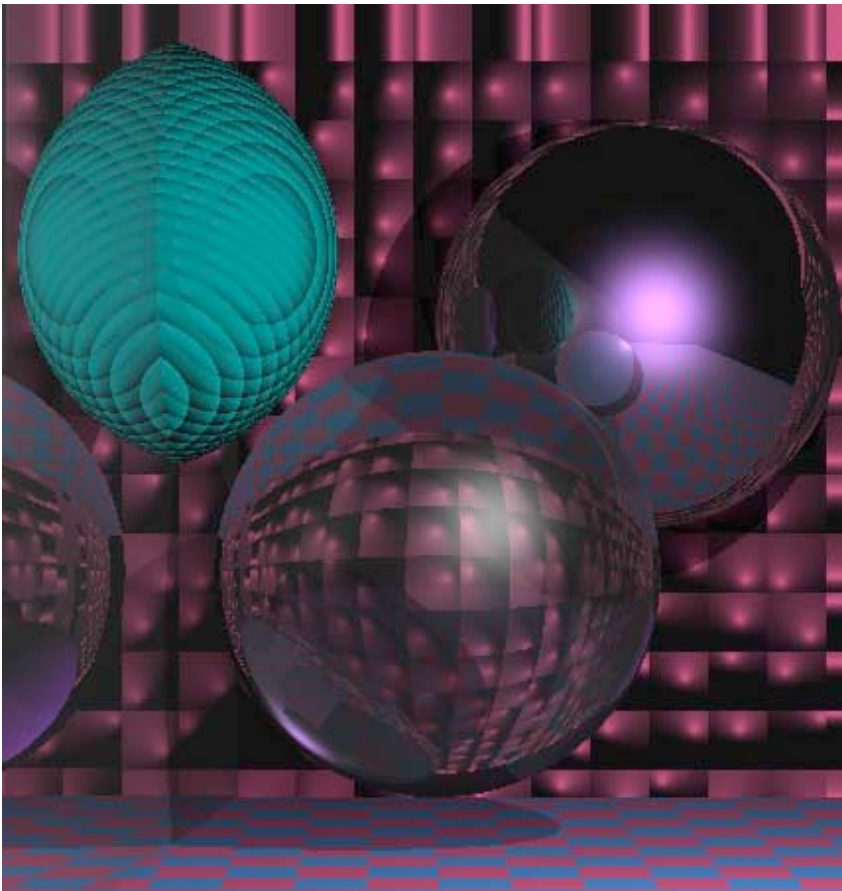


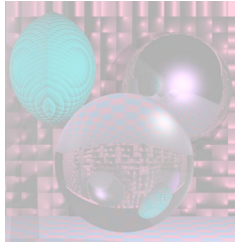
Course Overview - Topics

- Emphasis on rendering realistic images.
- Fundamentals of 2- and 3- dimensional computer graphics
 - 2-dimensional algorithms for drawing lines and curves, anti-aliasing, filling, and clipping
 - Using ray-tracing to render 3-dimensional scenes
 - composed of spheres, polygons, quadric surfaces, and bi-cubic surfaces
 - Techniques for adding texture to surfaces using texture and bump maps, noise, and turbulence
- Other topics as time permits

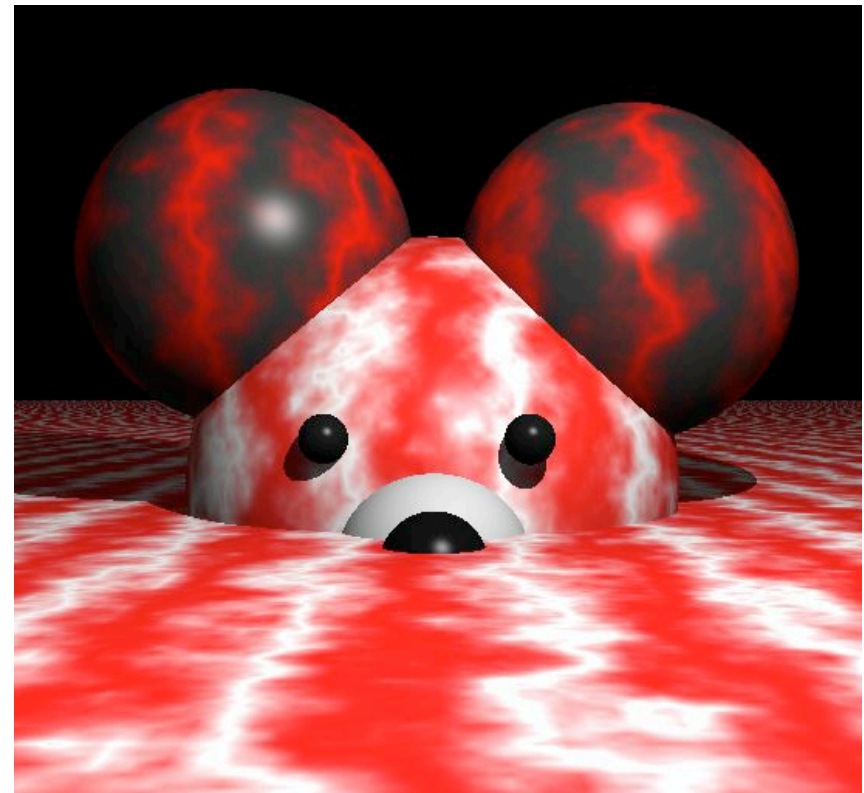


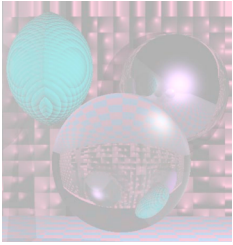
Sample Images



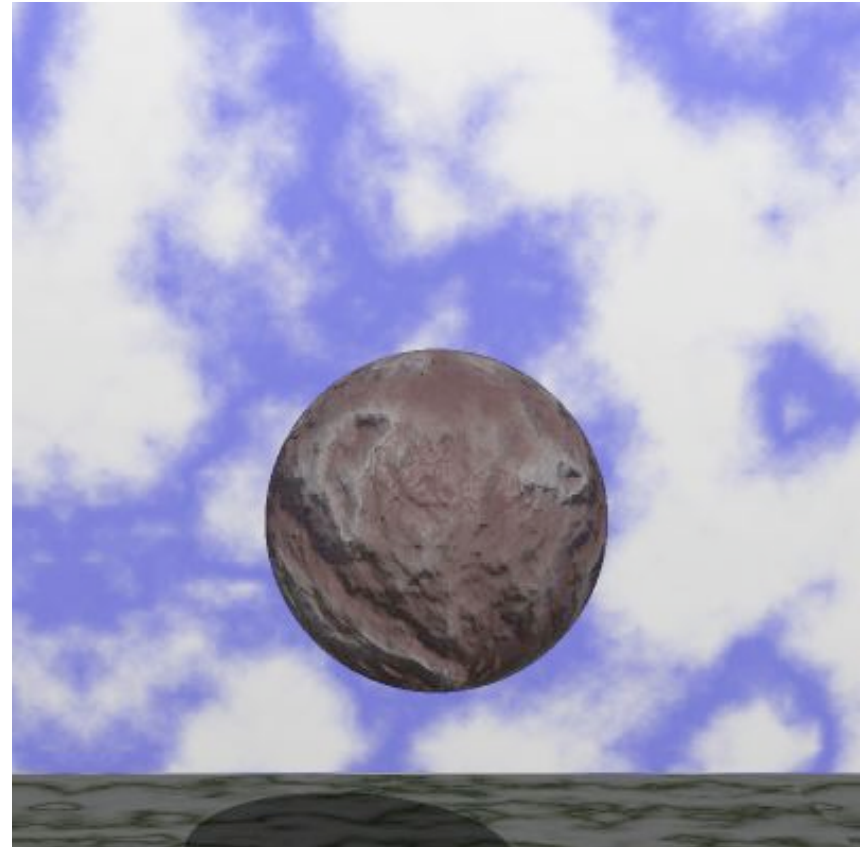


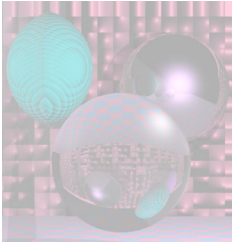
Sample Images



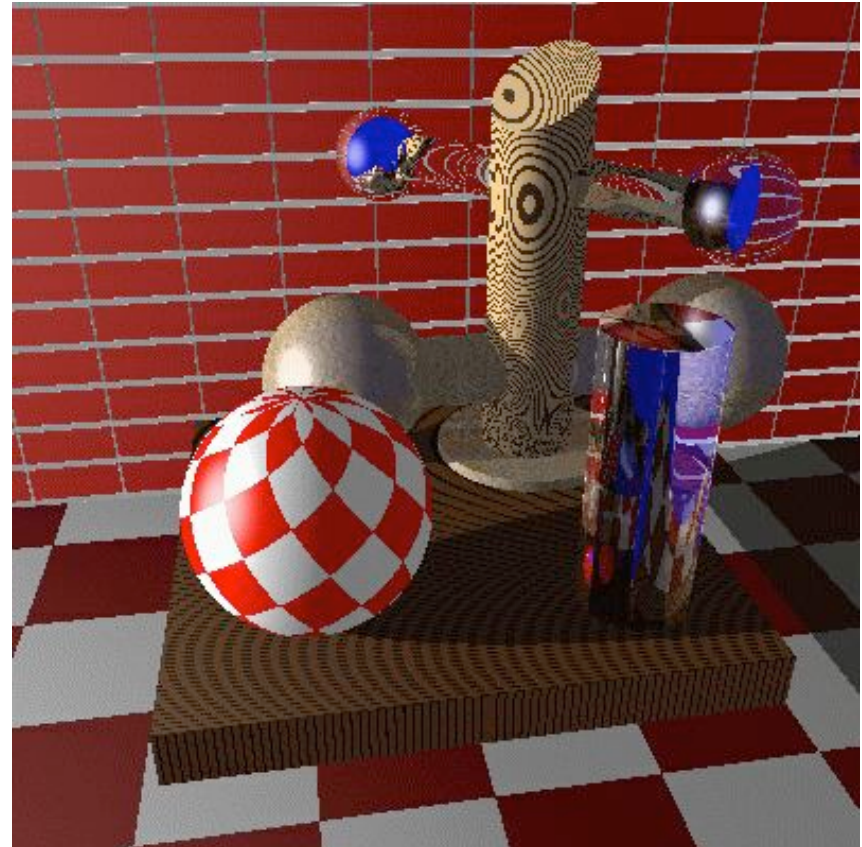
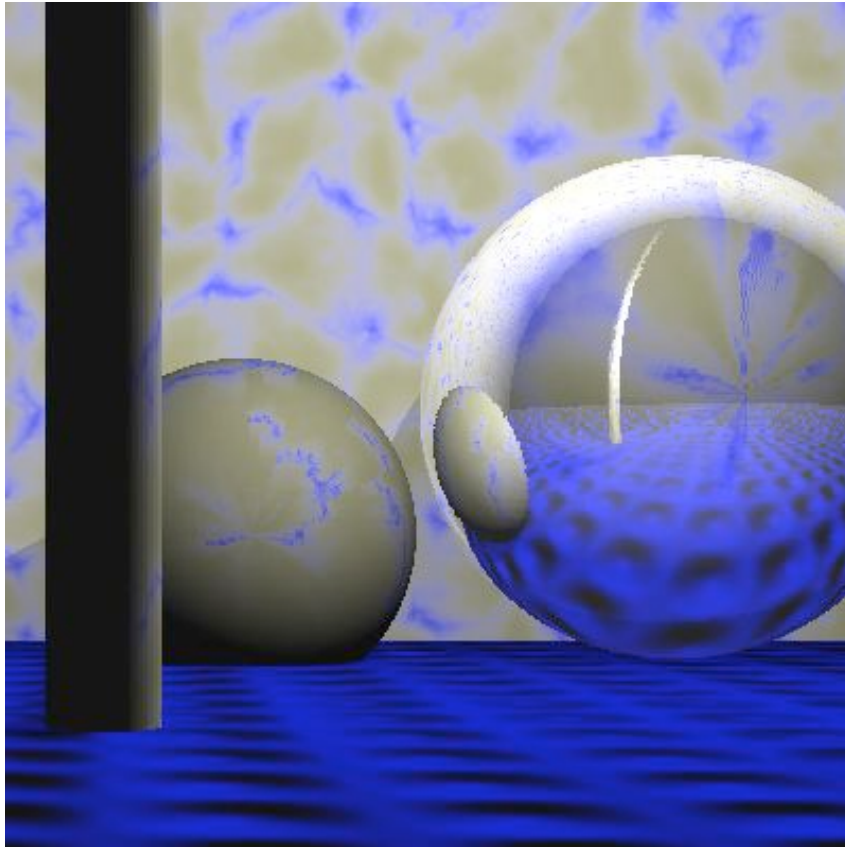


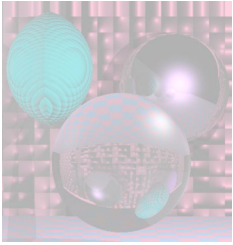
Sample Images



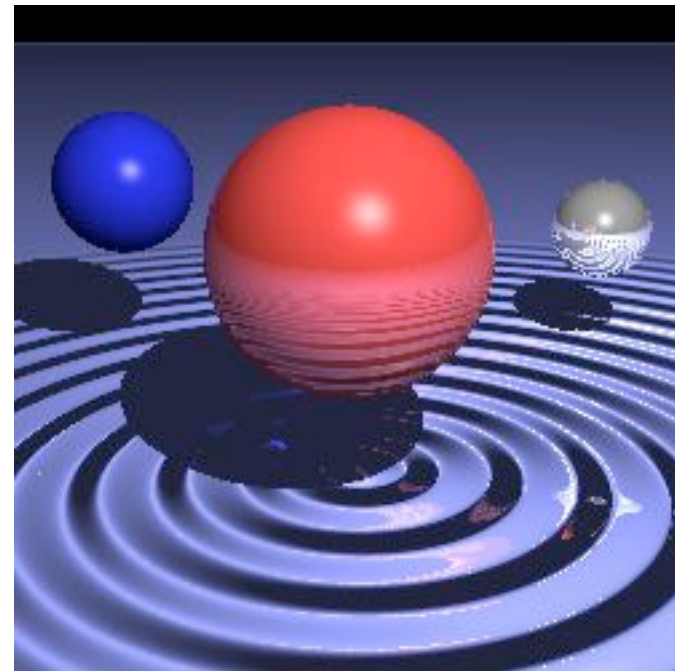
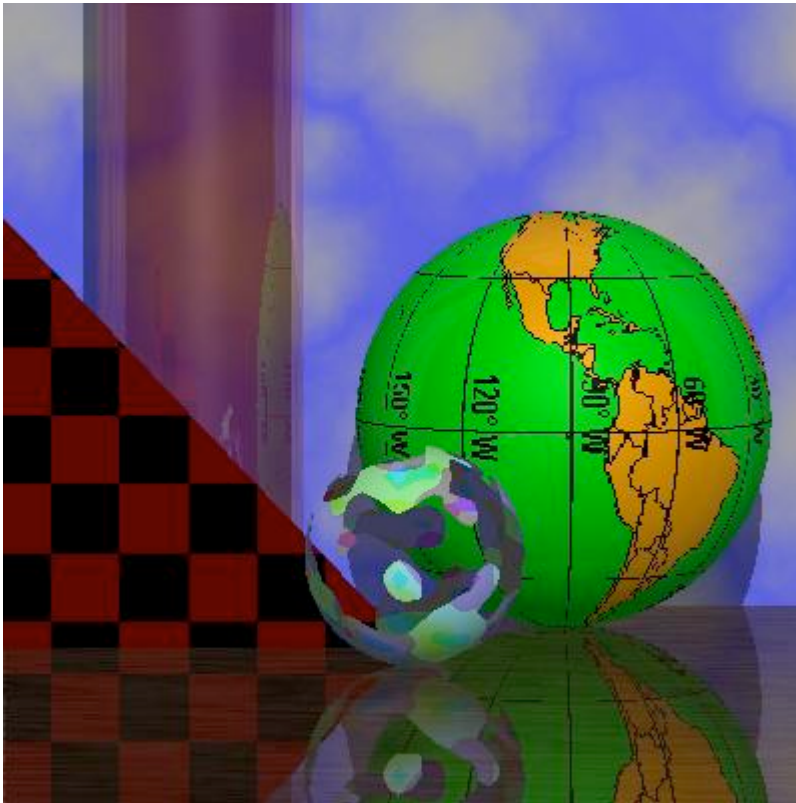


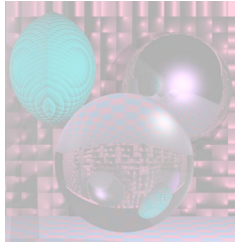
Sample Images





Sample Images





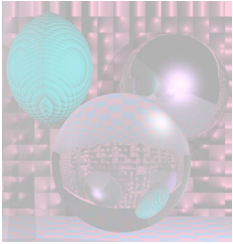
Course Overview - Organization

- **Texts:**

- Peter Shirley, *et al.* *Fundamentals of Computer Graphics, 2nd Edition*, A K Peters, 2005
- Alan Watt, *3D Computer Graphics, 3rd Edition*, Addison Wesley, 1999.

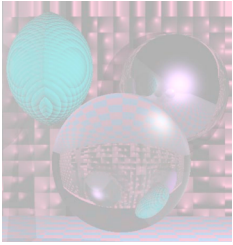
- **Grading**

- Assignment 0: 10%
- Assignment 1: 15%
- Assignment 2: 15%
- Assignment 3: 10%
- Assignment 4: 10%
- Exam: 25%
- Project and Presentation: 15%



Early History

- <http://accad.osu.edu/~waynec/history/timeline.html>
- http://sophia.javeriana.edu.co/~ochavarr/computer_graphics_history/historia/
- 1801 Joseph-Marie Jacquard invented an automatic loom using punched cards to control patterns in the fabrics. The introduction of these looms caused the riots against the replacement of people by machines.
- 1941 First U.S. regular TV broadcast,
1st TV commercial (for Bulova watches)
- 1948 Transistors
- 1949 Williams tube (CRT storage tube)



Jacquard Loom

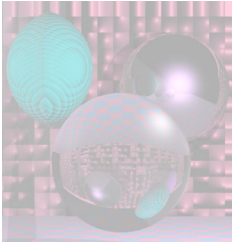


From Wikipedia.org

January 10, 2009

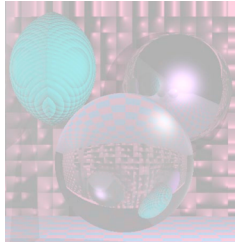
©College of Computer and Information Science, Northeastern University

10



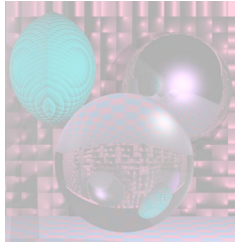
Early TV





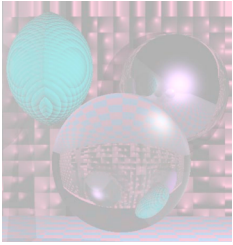
History – the 50s

- 1951 Graphics display, Whirlwind computer
- 1954 color TV
- 1955 Light Pen, SAGE- Lincoln Lab
- 1958 Graphics Console, TX-1 MIT
- 1958 John Whitney Sr. uses analog computer to make art



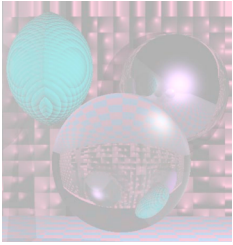
1951 Graphics display, Whirlwind computer



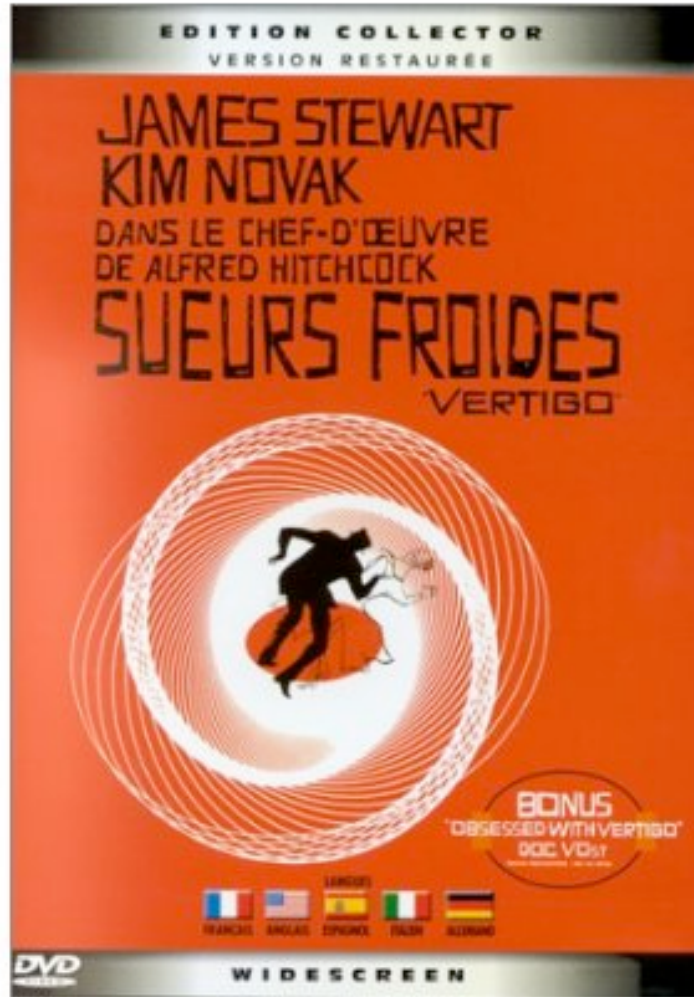


SAGE

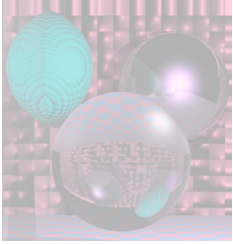




John Whitney Sr. 1958 CG

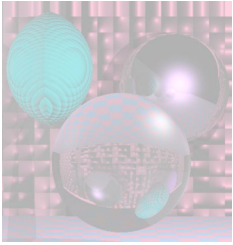


Vertigo Start Titles

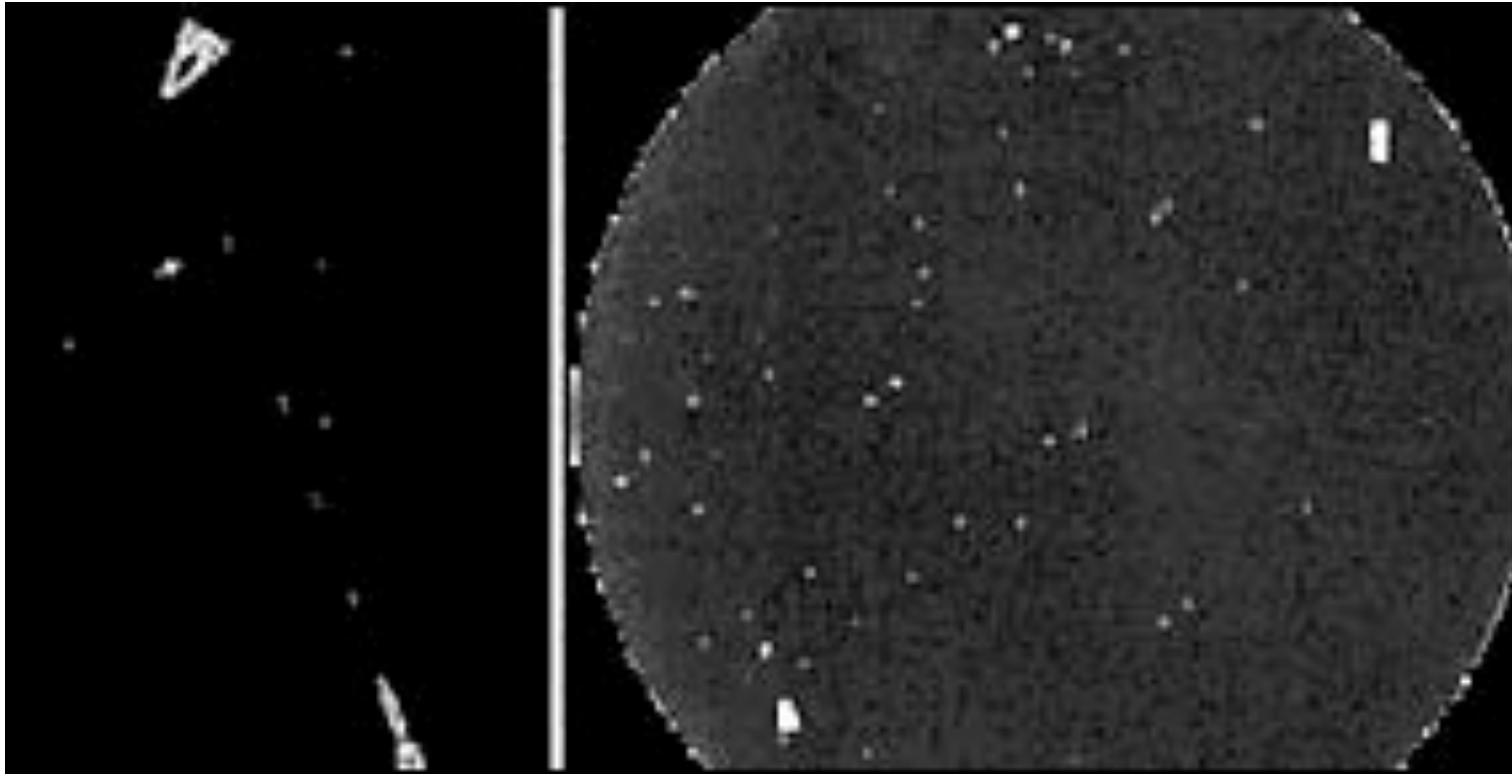


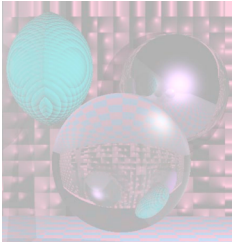
History - the 60s

- 1961 Spacewars, 1st video game, Steve Russell, MIT for PDP-1
- **1963** Sketchpad, Ivan Sutherland, MIT
- 1963 Mouse invented, Doug Englebart, SRI
- 1963 Roberts hidden line algorithm, MIT
- 1965 Bresenham Algorithm for plotting lines, IBM
- 1966 Odyssey, home video game, Ralph Baer,
 - Sanders Assoc, is 1st consumer CG product
- 1967 Full-color, real-time, interactive flight simulator for NASA - Rod Rougelet, GE



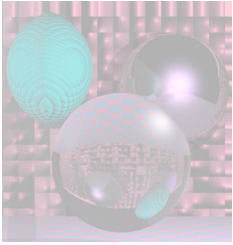
Spacewars





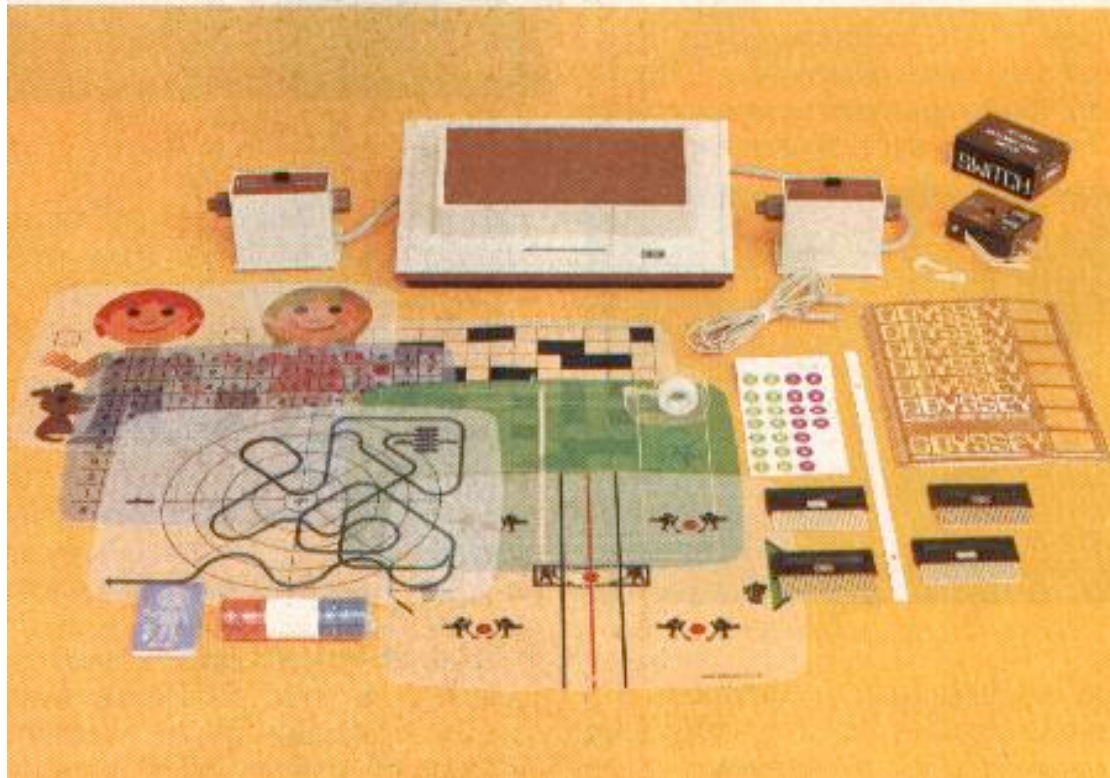
Ivan Sutherland & Sketchpad System on TX-2 at MIT(1963)



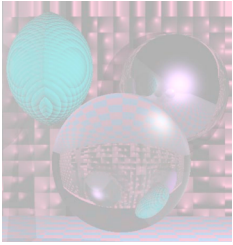


Odyssey

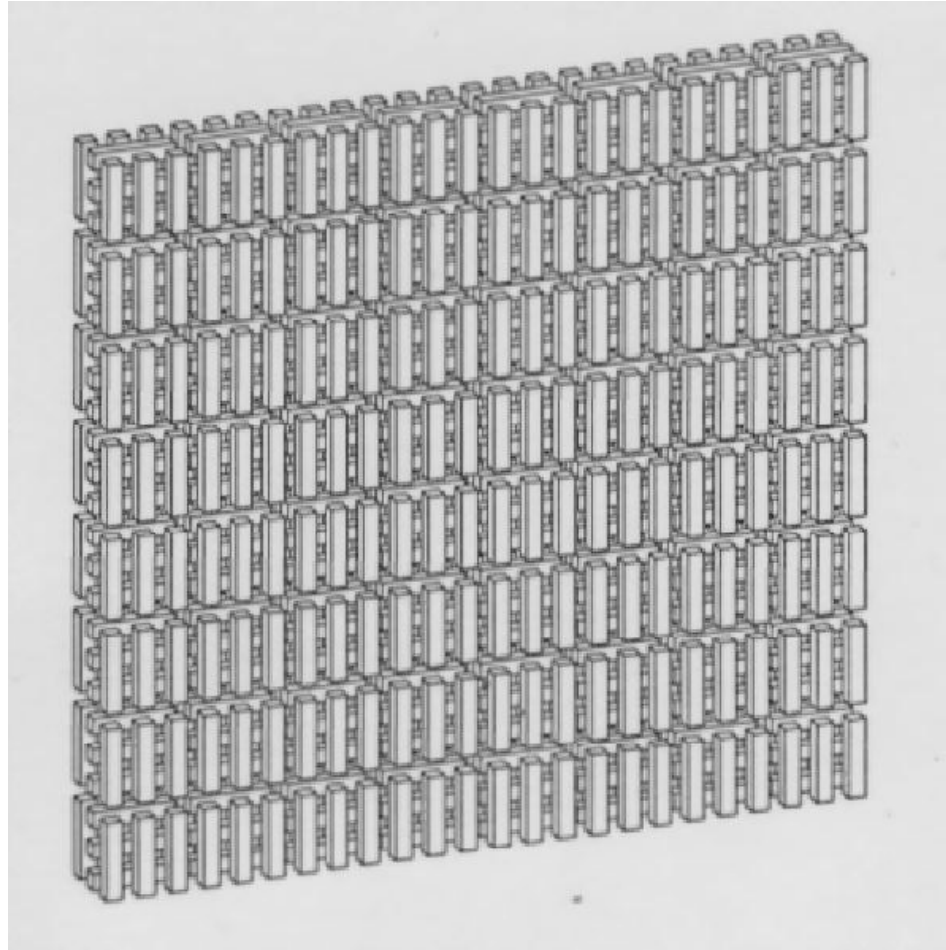
The very first home videogame, Odyssey, used Laner-created transparent overlays in lieu of computer-generated graphics.

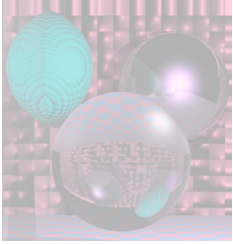


<http://www.geekcomix.com/vgh/first/odyssey.shtml>

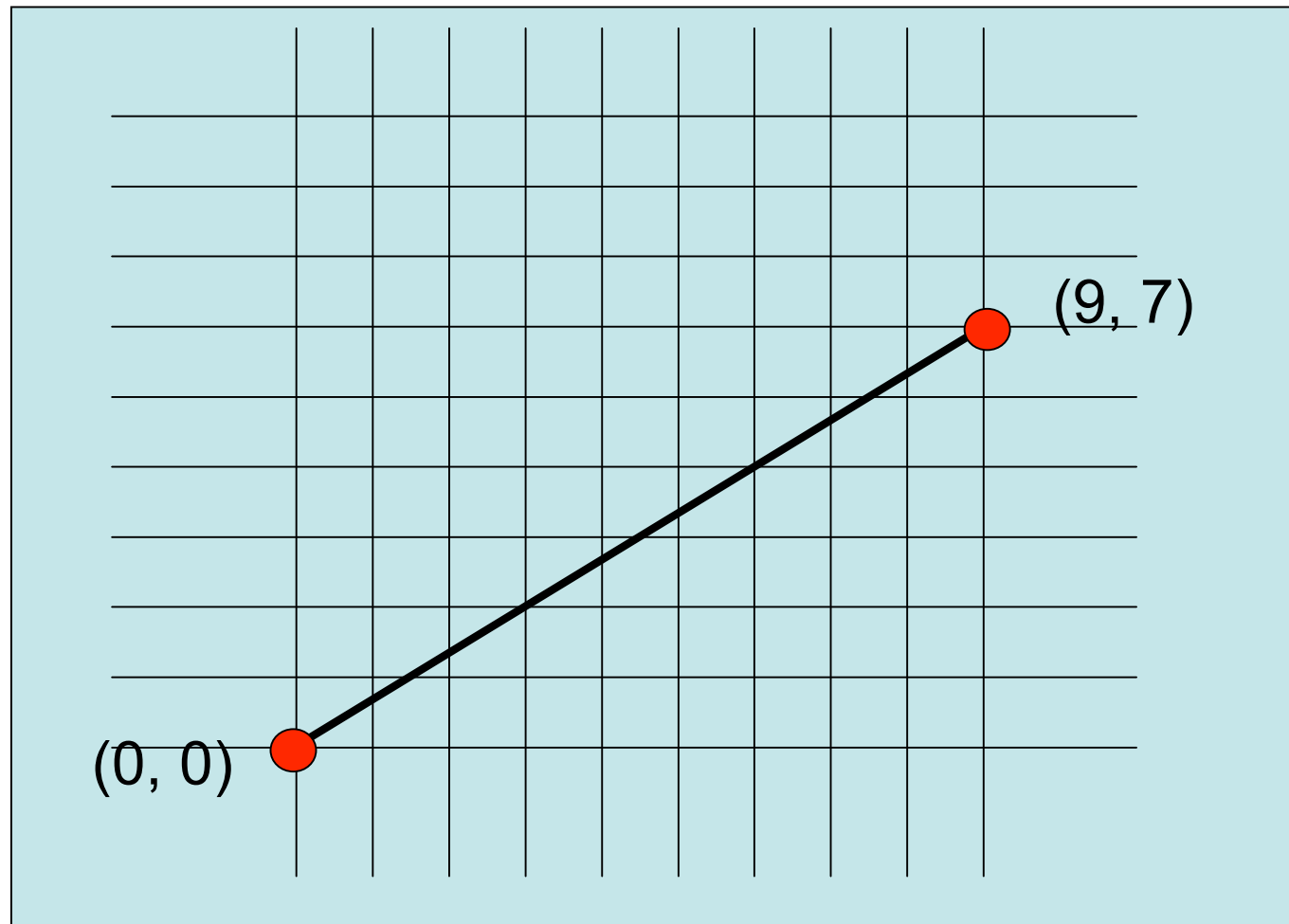


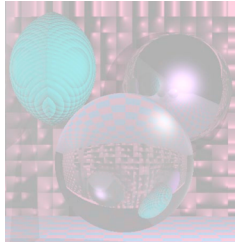
Roberts Hidden Line Algorithm Block scene (576 blocks)





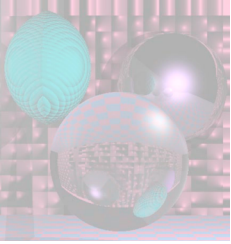
Bresenham Line Algorithm



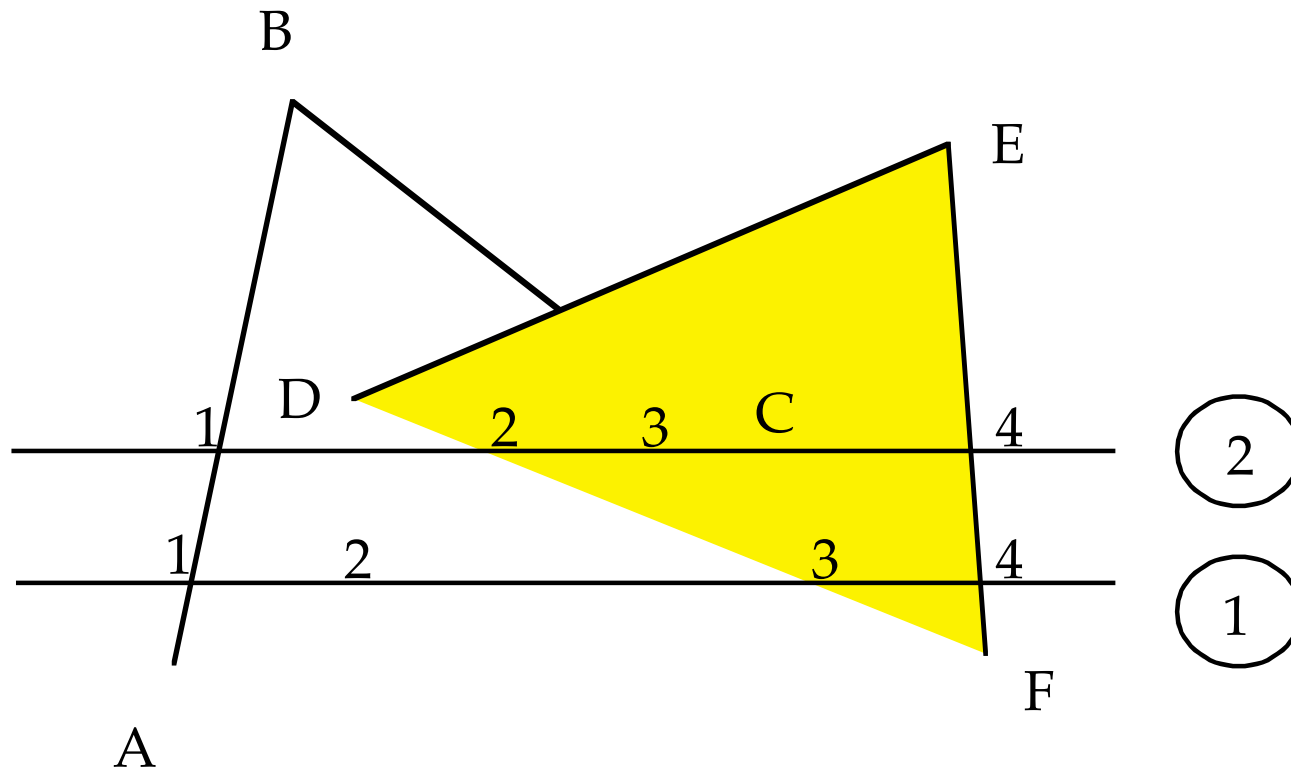


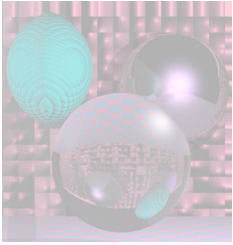
History – the 70s

- **1970s** **Utah dominated - algorithm development**
- 1970 [Watkins algorithm for visible surfaces](#)
- 1970 [Bezier free-form curve](#) representation
- 1971 [Gouraud shading](#)
- 1973 Principles of Interactive Computer Graphics (Newman and Sproull)
- 1974 Addressable cursor in a graphics display terminal - DEC VT52
- 1974 z-buffer developed by Ed Catmull (Univ of Utah)
- 1975 [Phong shading](#)
- 1975 [Fractals](#) - Benoit Mandelbrot (IBM)
- 1978 [Bump mapping](#), Blinn
- 1979 George Lucas starts Lucasfilm
 - with Ed Catmull, Ralph Guggenheim, and Alvy Ray Smith

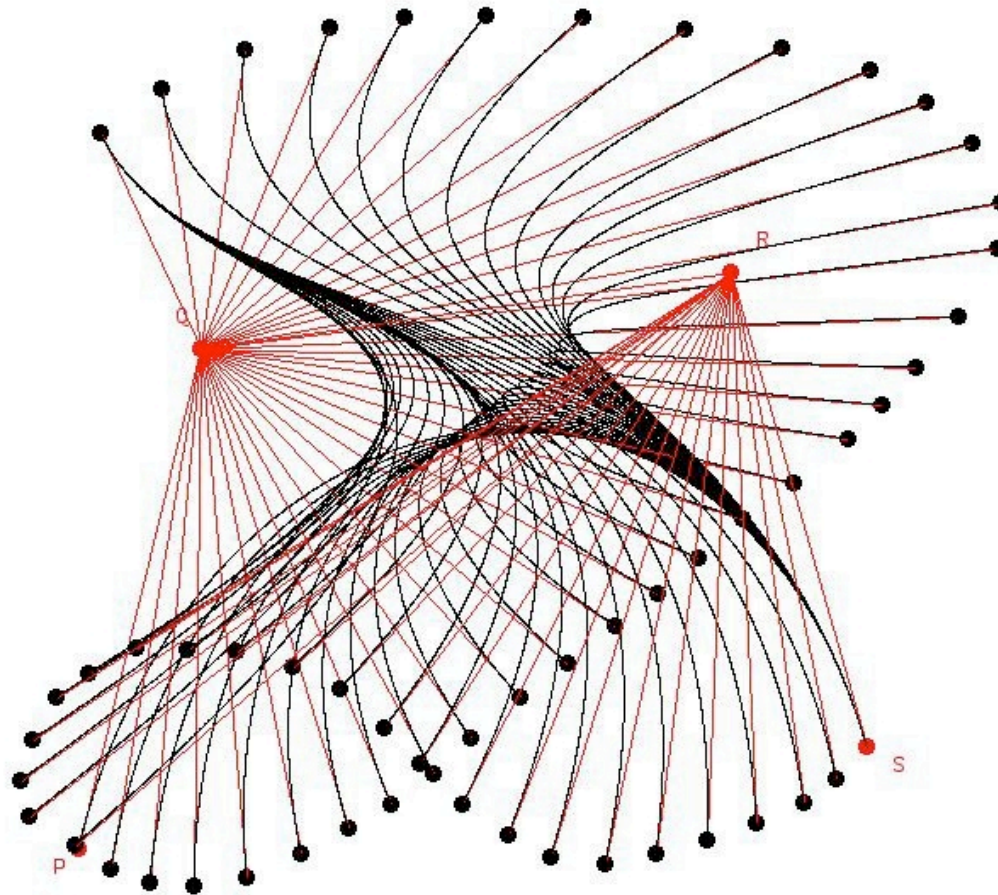


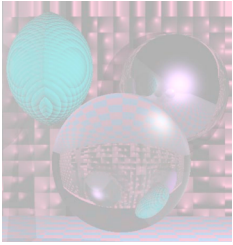
Watkins Scan-Line Algorithm



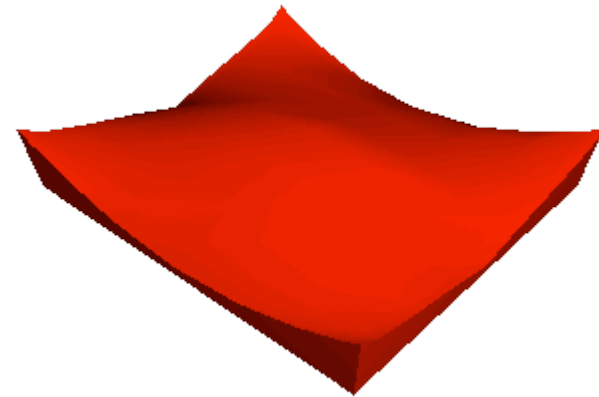


Bezier Curves

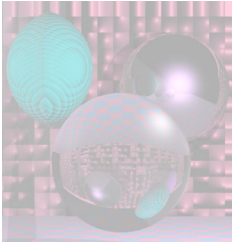




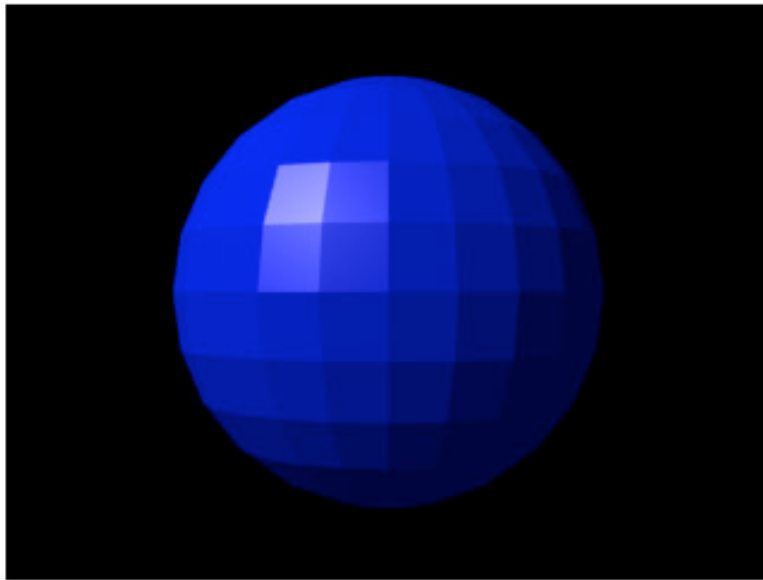
Gouraud Shading



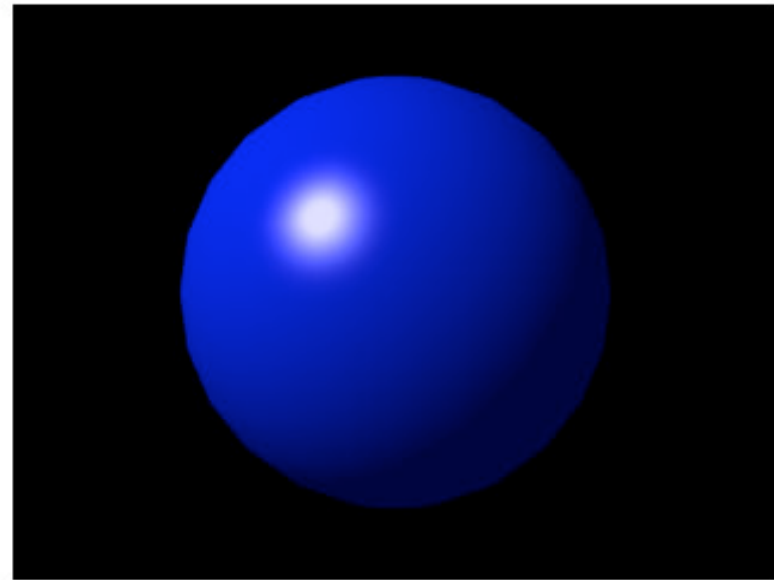
http://freespace.virgin.net/hugo.elias/graphics/x_polygo.htm



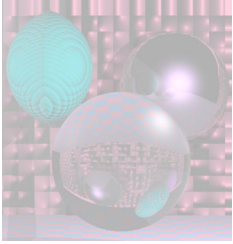
Phong Shading



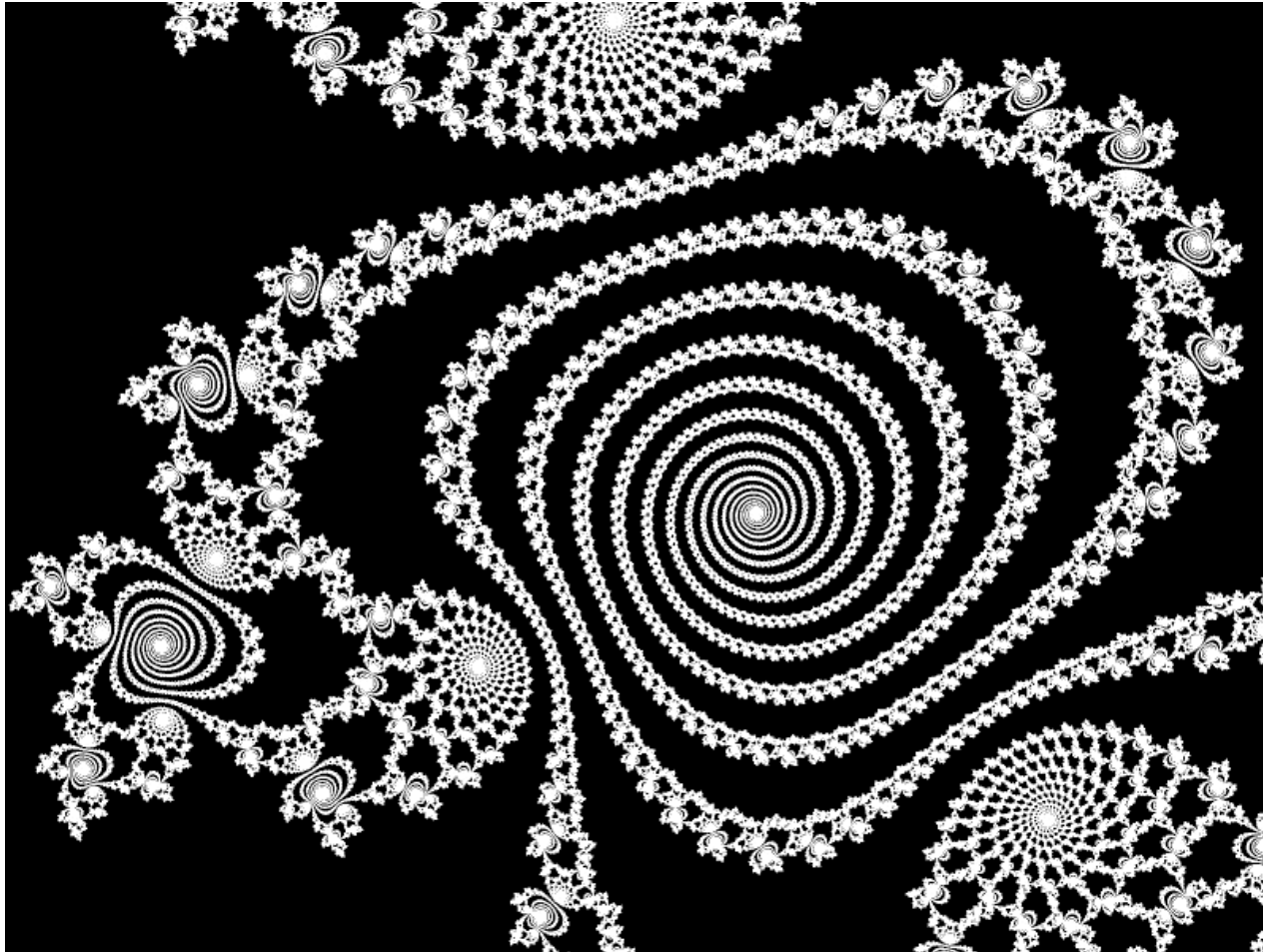
FLAT SHADING

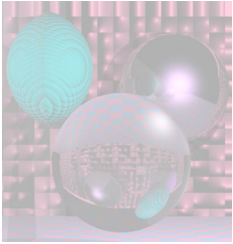


PHONG SHADING

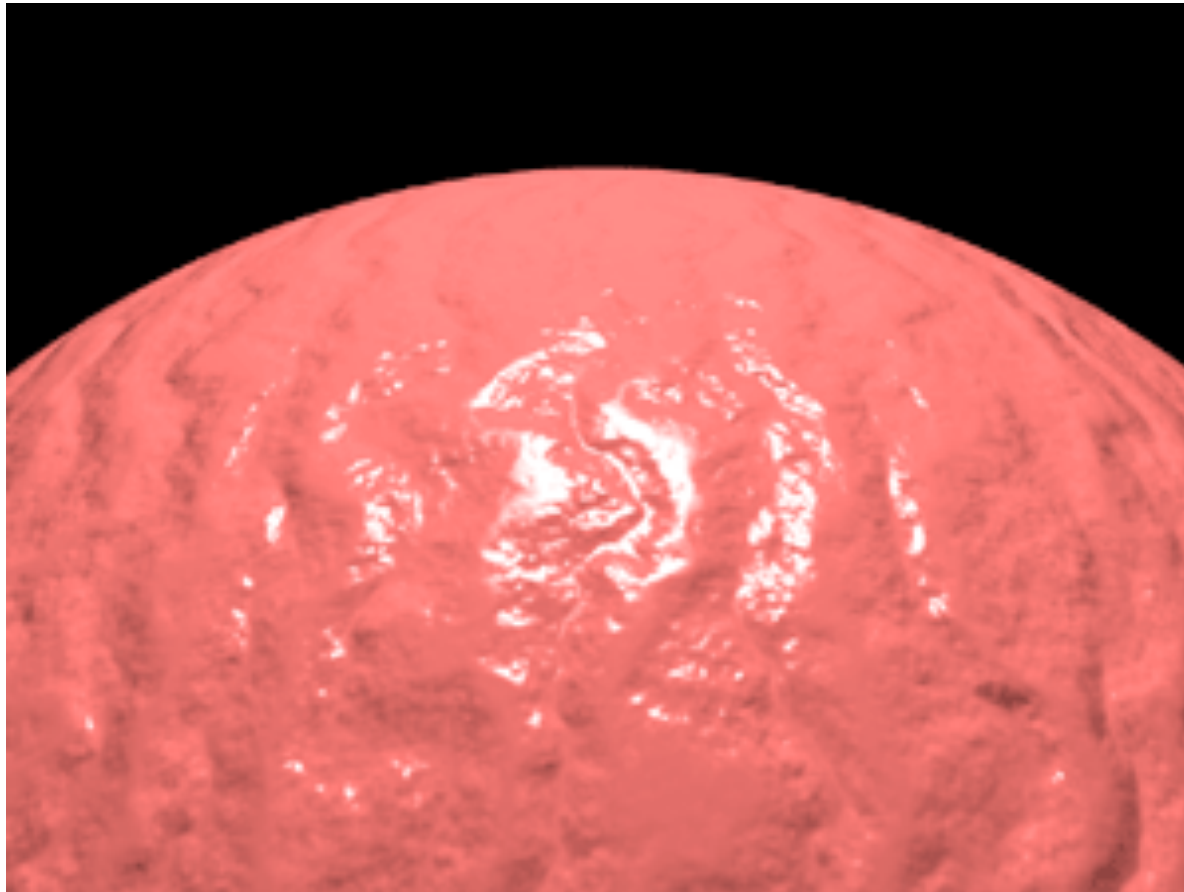


Fractals

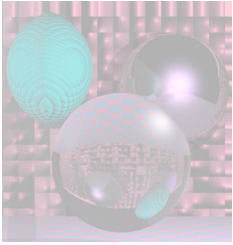




Bump Map

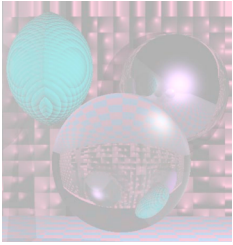


[Bump Maps in PovRay](#)

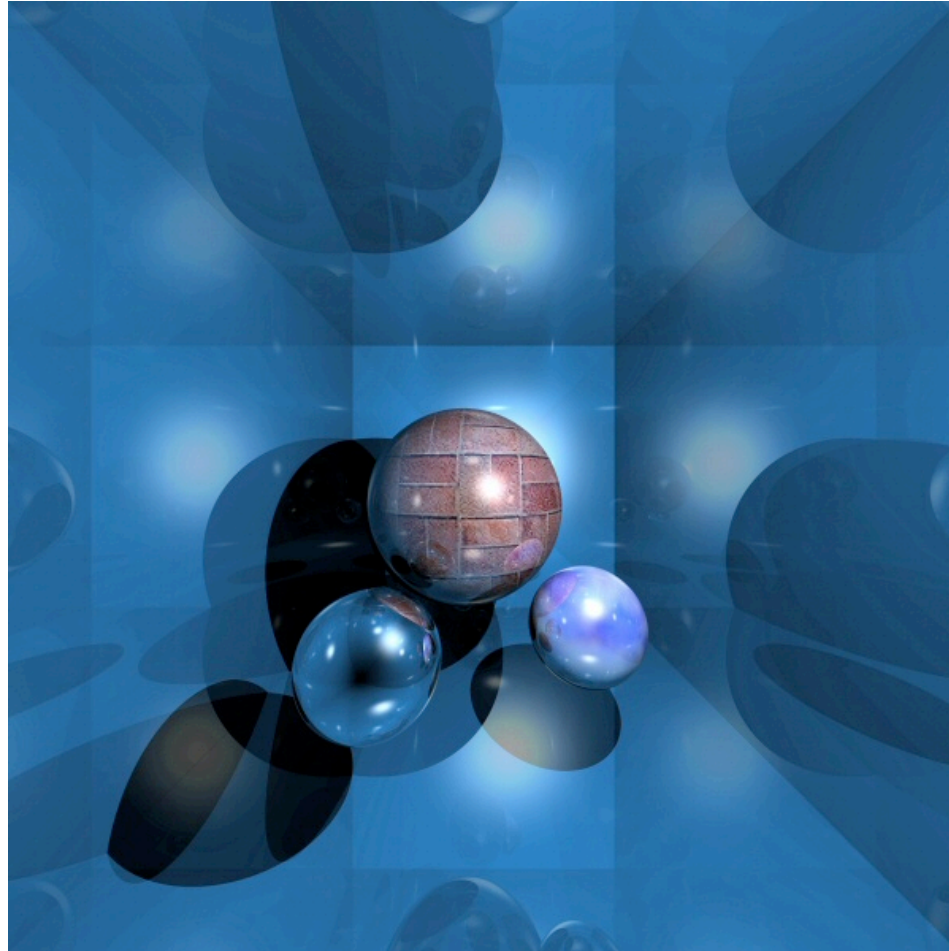


History - the 80s

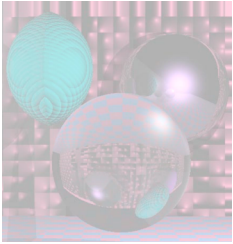
- **1980s Cheaper machines, memory - quest for realism**
- 1980 [Ray Tracing](#), Turner Whitted, Bell Labs
- 1981 IBM introduces the first IBM PC (16 bit 8088 chip)
- 1982 Data Glove, Atari
- 1984 [Macintosh](#) computer
 - introduced with Clio award winning commercial during Super Bowl
- 1985 [Perlin Noise](#)
- 1986 GIF format (CompuServe)
- 1988 [Who Framed Roger Rabbit](#) live action & animation



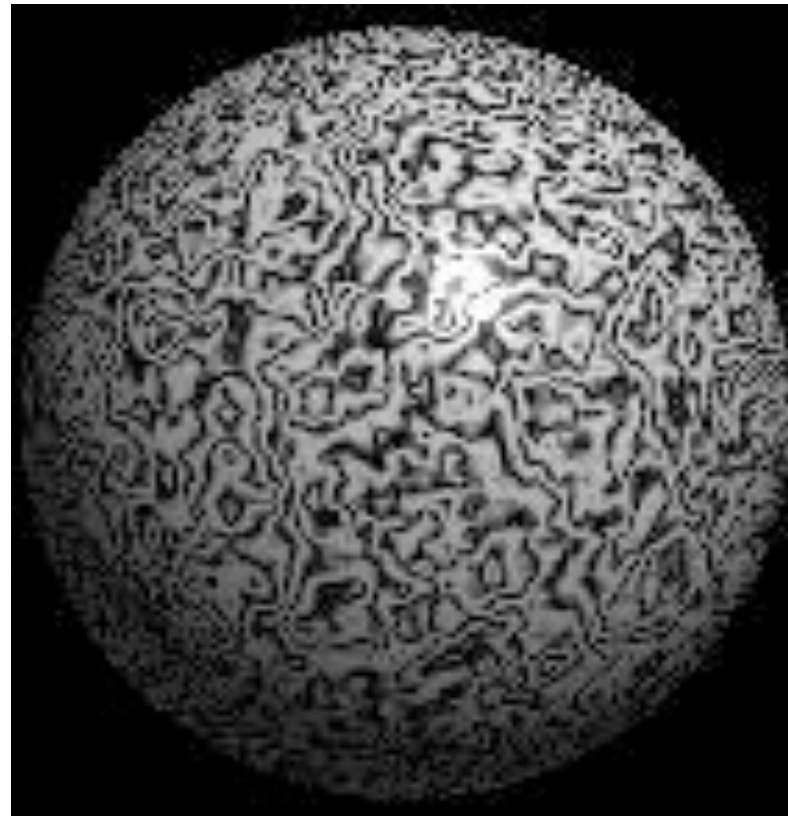
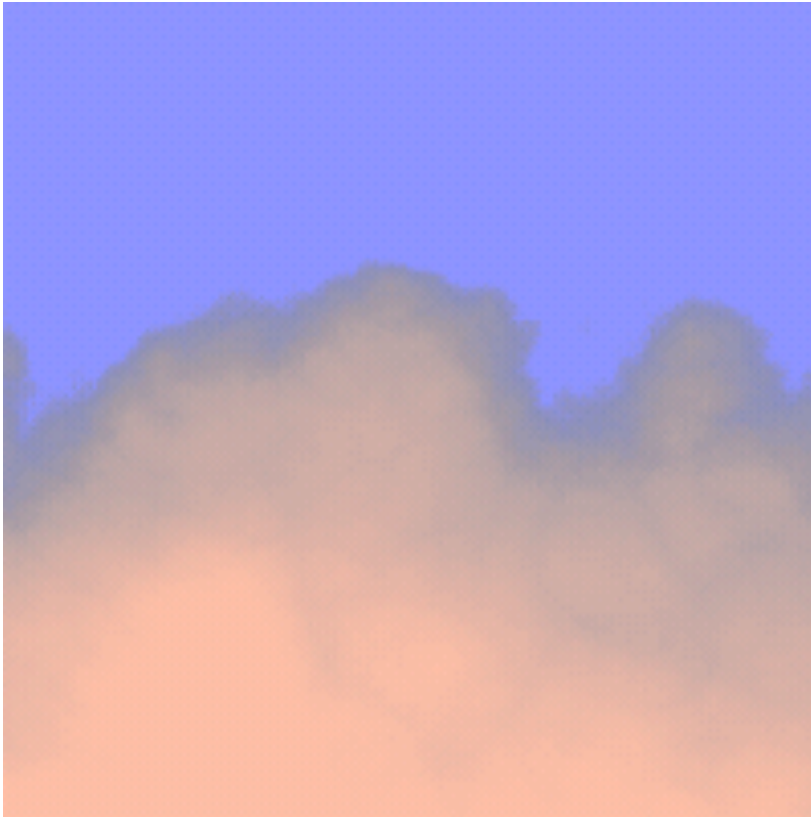
Whitted Ray-Tracing

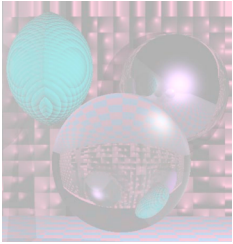


http://en.wikipedia.org/wiki/Ray_tracing



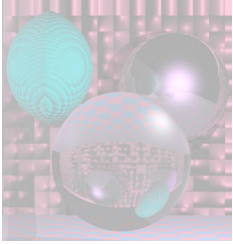
Perlin Noise





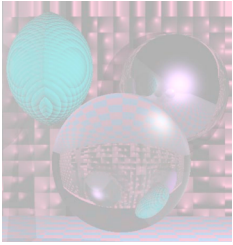
Who Framed Roger Rabbit





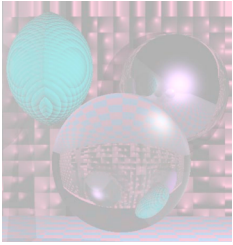
History- the 90s

- **1990s Visualization, Multimedia, the Net**
- 1991 JPEG/MPEG
- 1993 [Myst](#), Cyan
- 1994 U.S. Patent to Pixar
 - for creating, manipulating and displaying images
- 1995 [Toy Story](#), Pixar
- 1995 Internet 2 unveiled
- 1997 DVD technology unveiled
- 1998 XML standard
- 1999 deaths



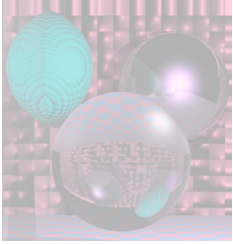
Myst





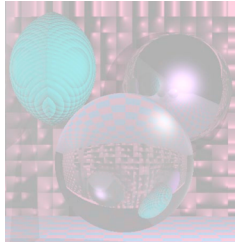
Toy Story





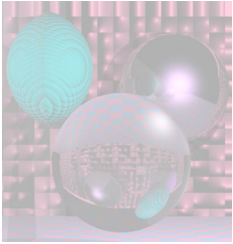
Recent History

- **2000s Virtual Reality, Animation Reality**
- 2001 Significant Movies
 - Final Fantasy, Square)
 - Monsters Inc, Pixar
 - Harry Potter, A.I., Lord of the Rings, Shrek, PDI
 - The Mummy, ILM
 - Tomb Raider, Cinesite
 - Jurassic Park III, Pearl Harbor, ILM
 - Planet of the Apes, Asylum
- 2001 Microsoft xBox and Nintendo Gamecube
- 2001, 2002, 2003 [Lord of the Rings](#)



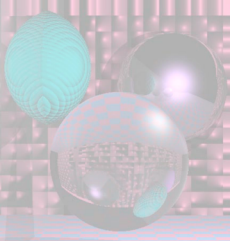
from Lord of the Rings

- **Motion Capture Technology**
 - Andy Serkis "played" Gollum by providing his voice and movements on set, as well as performing within a motion capture suit.
- **SKIN**
 - Christopher Hery, Ken McGaugh and Joe Letteri received a 2003 Academy Award, Scientific or Technical for implementing the BSSRDF (Bidirectional Surface Scattering Reflection Distribution Function) technique used for Gollum's skin in a production environment. Henrik Wann Jensen, Stephen Robert Marschner, and Pat Hanrahan, who developed BSSRDF, won another the same year.
- **MASSIVE**
 - a computer program developed by WETA to create automatic battle sequences rather than individually animate every soldier. Stephen Regelous developed the system in 1996, originally to create crowd scenes in *King Kong*.



Time for a Break

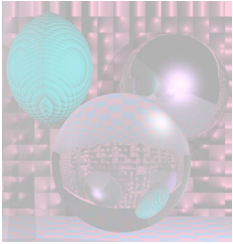




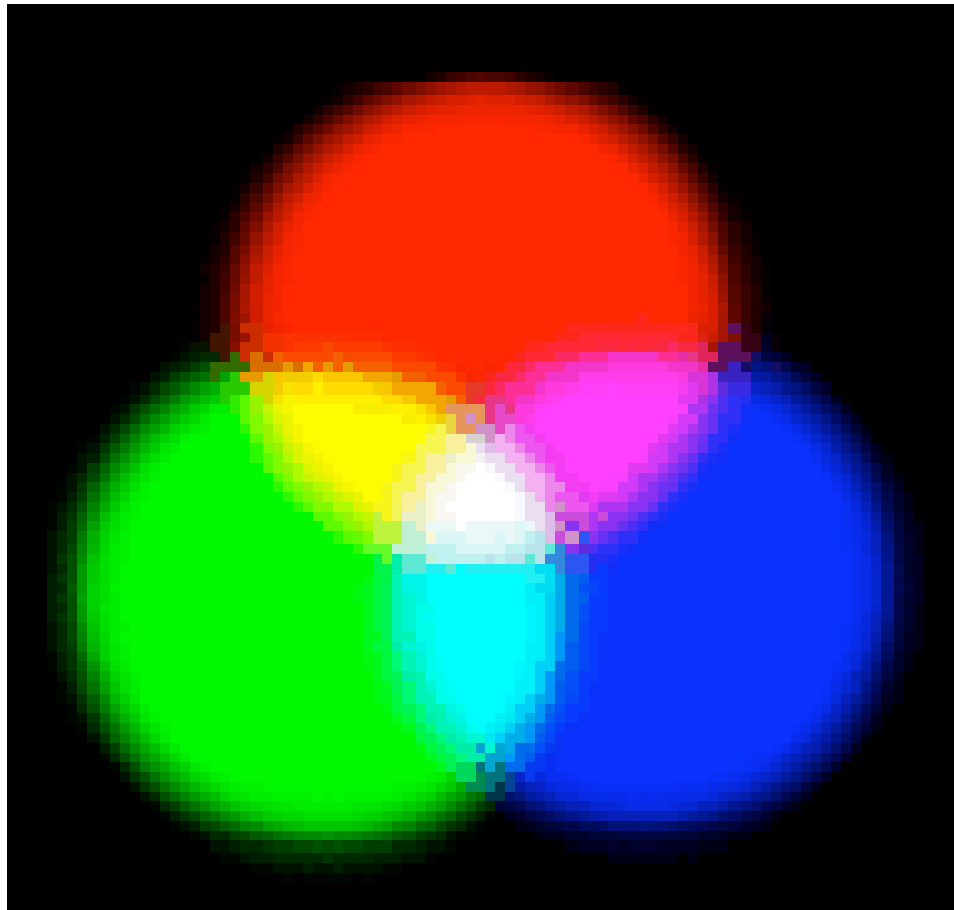
Color

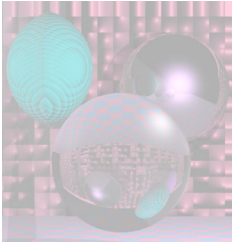


www.thestagecrew.com

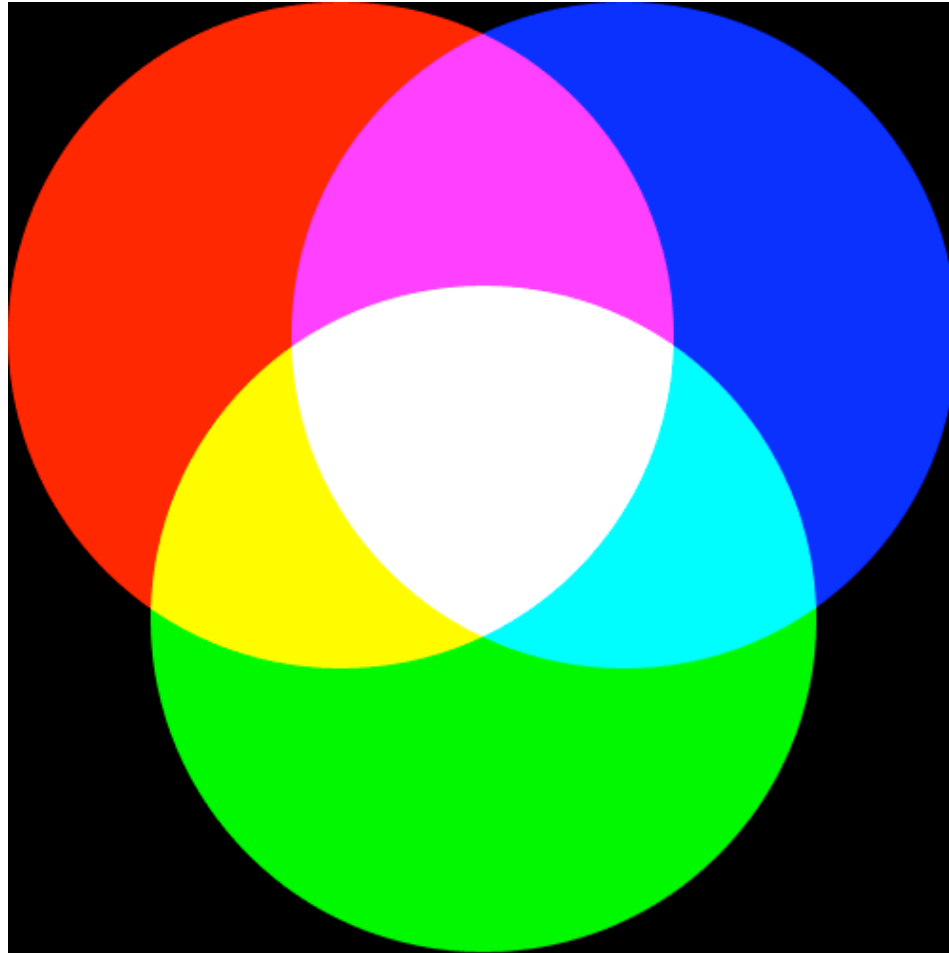


Red, Green, and Blue Light

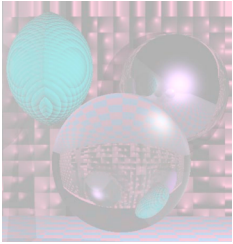




Adding R, G, and B Values



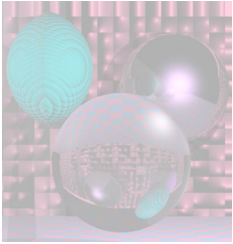
<http://en.wikipedia.org/wiki/RGB>



From the Hubble

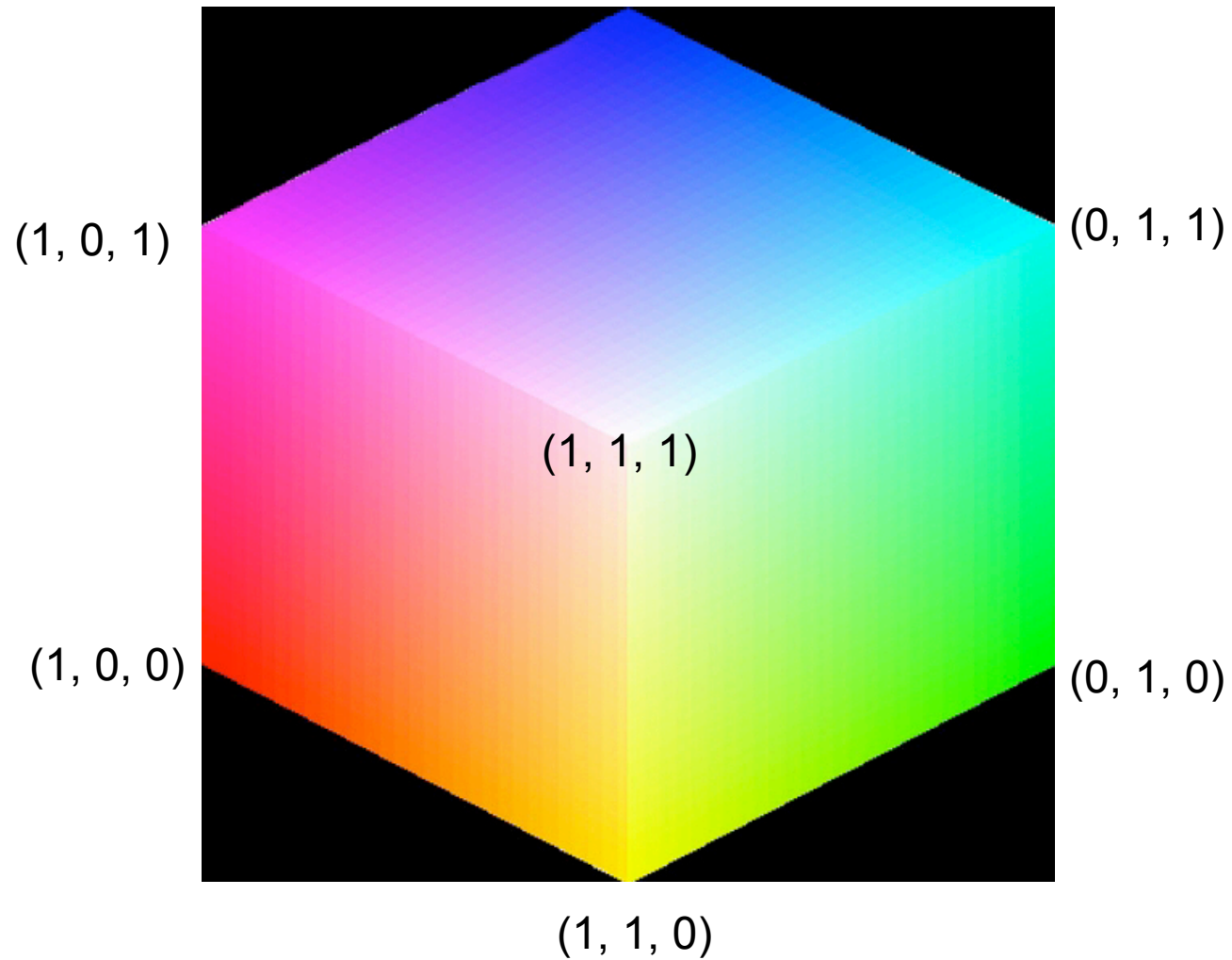
[Hubble Site Link](#)

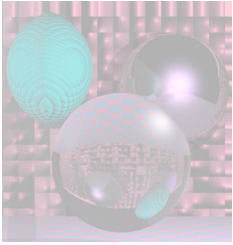




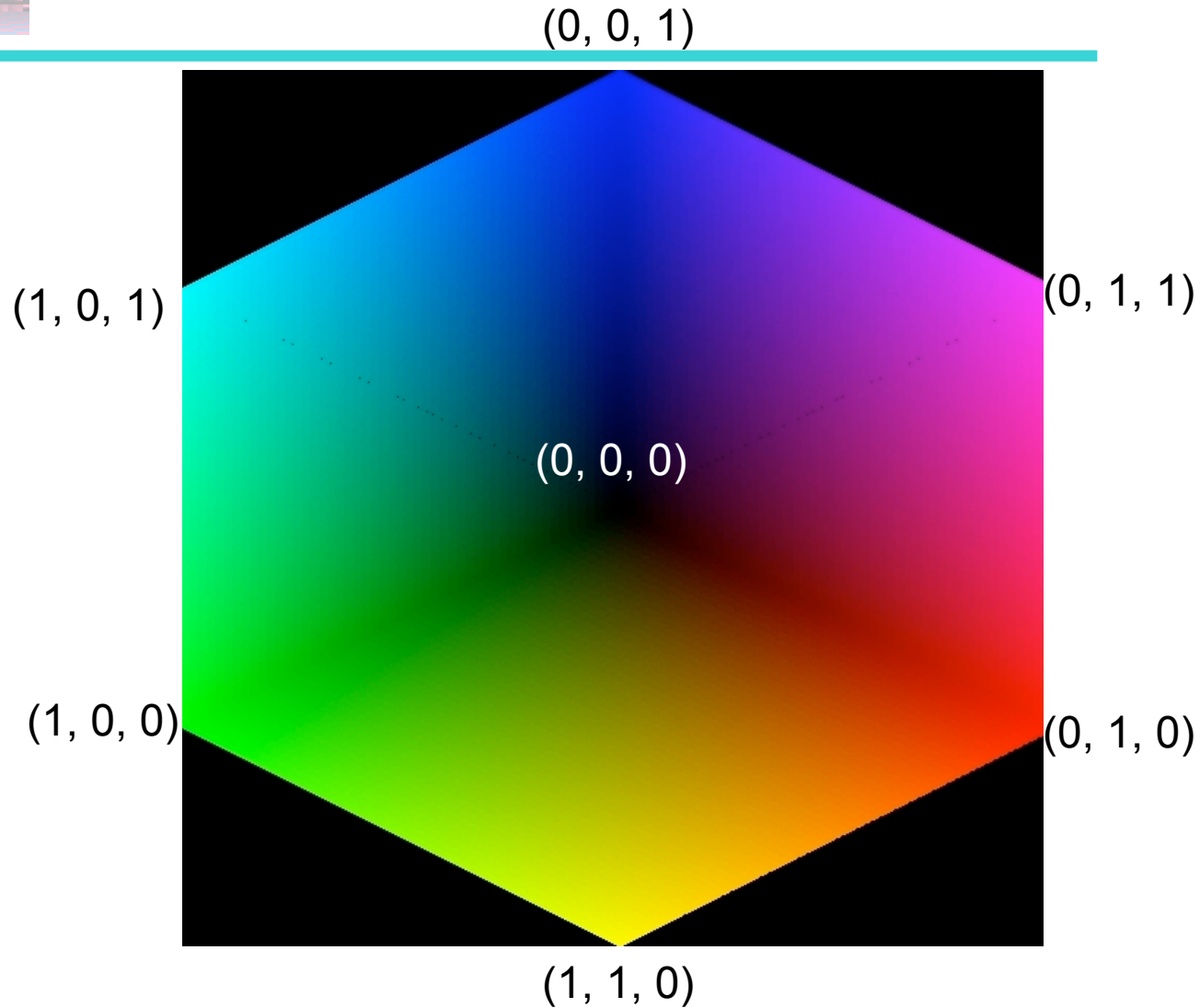
RGB Color Cube

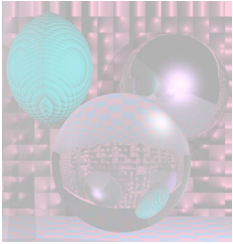
$(0, 0, 1)$





RGB Color Cube The Dark Side





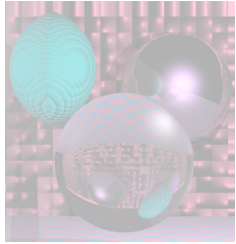
Doug Jacobson's RGB Hex Triplet Color Chart

RGB Hex Triplet Color Chart
E-mail-ware...What a concept!

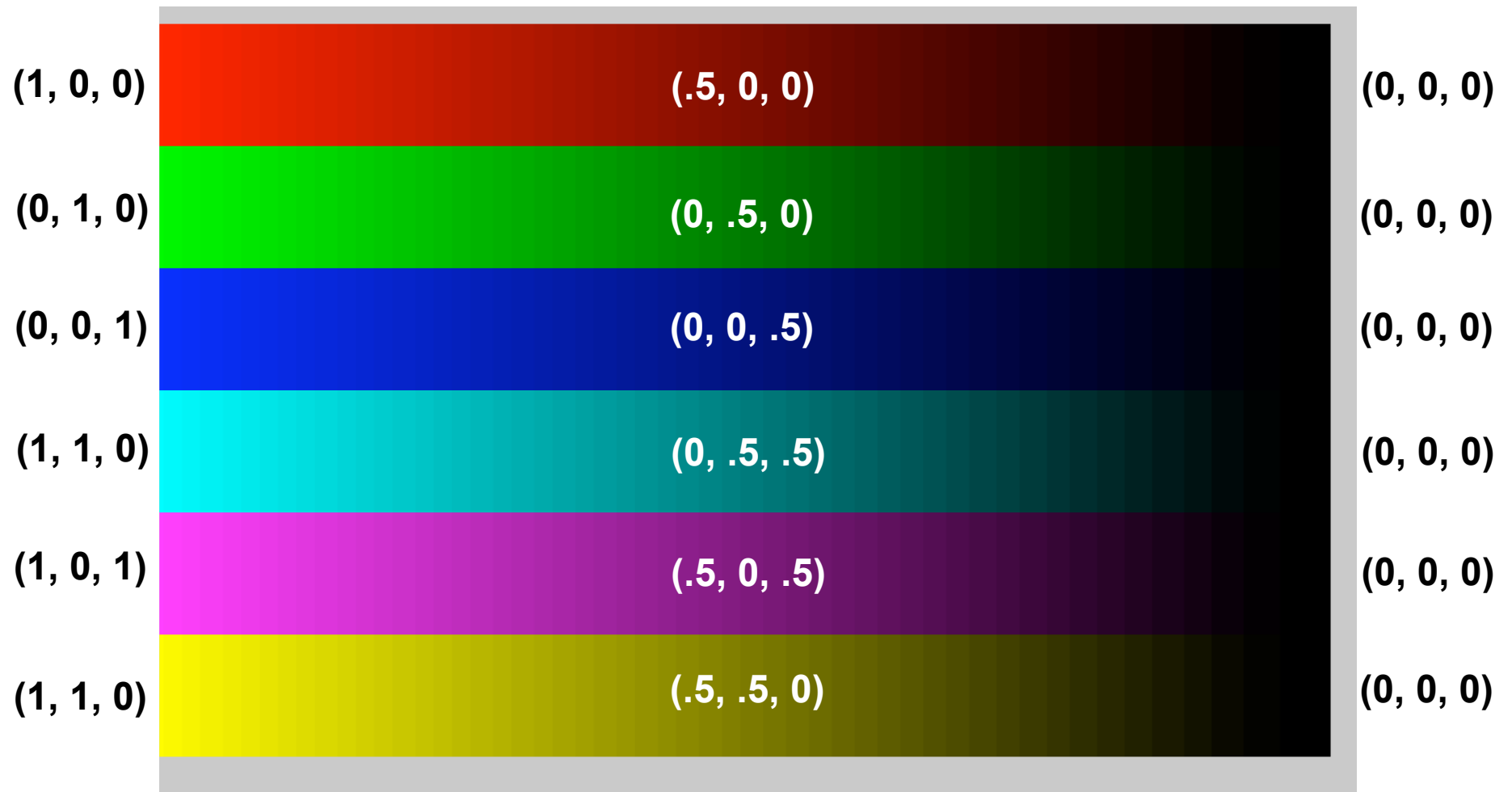
*If you find this chart helpful, send mail to Doug and say "Thanks!".
 jacobson@phoenix.net*

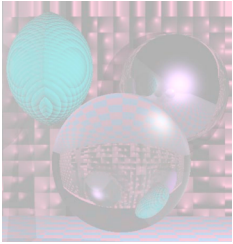
		FFFFFF		FFCCFF		FF99FF		FF66FF		FF33FF		FF00FF	
	EEEEEE		FFFFCC		FFCCCC		FF99CC		FF66CC		FF33CC		FF00CC
	DDDDDD		FFFF99		FFCC99		FF9999		FF6699		FF3399		FF0099
	CCCCCC		FFFF66		FFCC66		FF9966		FF6666		FF3366		FF0066
	BBBBBB		FFFF33		FFCC33		FF9933		FF6633		FF3333		FF0033
	AAAAAA		FFFF00		FFCC00		FF9900		FF6600		FF3300		FF0000
	999999		CCFFFF		CCCCFF		CC99FF		CC66FF		CC33FF		CC00FF
	888888		CCFFCC		CCCCCC		CC99CC		CC66CC		CC33CC		CC00CC
	777777		CCFF99		CCCC99		CC9999		CC6699		CC3399		CC0099
	666666		CCFF66		CCCC66		CC9966		CC6666		CC3366		CC0066
	555555		CCFF33		CCCC33		CC9933		CC6633		CC3333		CC0033
	444444		CCFF00		CCCC00		CC9900		CC6600		CC3300		CC0000
	333333		99FFFF		99CCFF		9999FF		9966FF		9933FF		9900FF
	222222		99FFCC		99CCCC		9999CC		9966CC		9933CC		9900CC
	111111		99FF99		99CC99		999999		996699		993399		990099
	000000		99FF66		99CC66		999966		996666		993366		990066
	FF0000		99FF33		99CC33		999933		996633		993333		990033
	EE0000		99FF00		99CC00		999900		996600		993300		990000
	DD0000		66FFFF		66CCFF		6699FF		6666FF		6633FF		6600FF
	CC0000		66FFCC		66CCCC		6699CC		6666CC		6633CC		6600CC
	BB0000		66FF99		66CC99		669999		666699		663399		660099
	AA0000		66FF66		66CC66		669966		666666		663366		660066
	990000		66FF33		66CC33		669933		666633		663333		660033
	880000		66FF00		66CC00		669900		666600		663300		660000
	770000		33FFFF		33CCFF		3399FF		3366FF		3333FF		3300FF
	660000		33FFCC		33CCCC		3399CC		3366CC		3333CC		3300CC
	550000		33FF99		33CC99		339999		336699		333399		330099
	440000		33FF66		33CC66		339966		336666		333366		330066
	330000		33FF33		33CC33		339933		336633		333333		330033
	220000		33FF00		33CC00		339900		336600		333300		330000
	110000		00FFFF		00CCFF		0099FF		0066FF		0033FF		0000FF
			00FFCC		00CCCC		0099CC		0066CC		0033CC		0000CC
			00FF99		00CC99		009999		006699		003399		000099
			00FF66		00CC66		009966		006666		003366		000066
			00FF33		00CC33		009933		006633		003333		000033
			00FF00		00CC00		009900		006600		003300		000000

Copyright © 1995 Douglas R. Jacobson
 All Rights Reserved



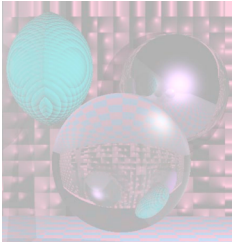
Making Colors Darker





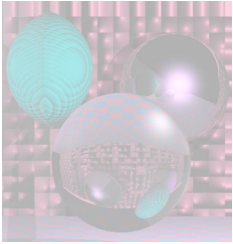
Getting Darker, Left to Right

```
for (int b = 255; b >= 0; b--){  
    c = new Color(b, 0, 0); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 50, 3, 150);  
    c = new Color(0, b, 0); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 200, 3, 150);  
    c = new Color(0, 0, b); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 350, 3, 150);  
    c = new Color(0, b, b); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 500, 3, 150);  
    c = new Color(b, 0, b); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 650, 3, 150);  
    c = new Color(b, b, 0); g.setPaint(c);  
    g.fillRect(800+3*(255-b), 800, 3, 150);  
}
```

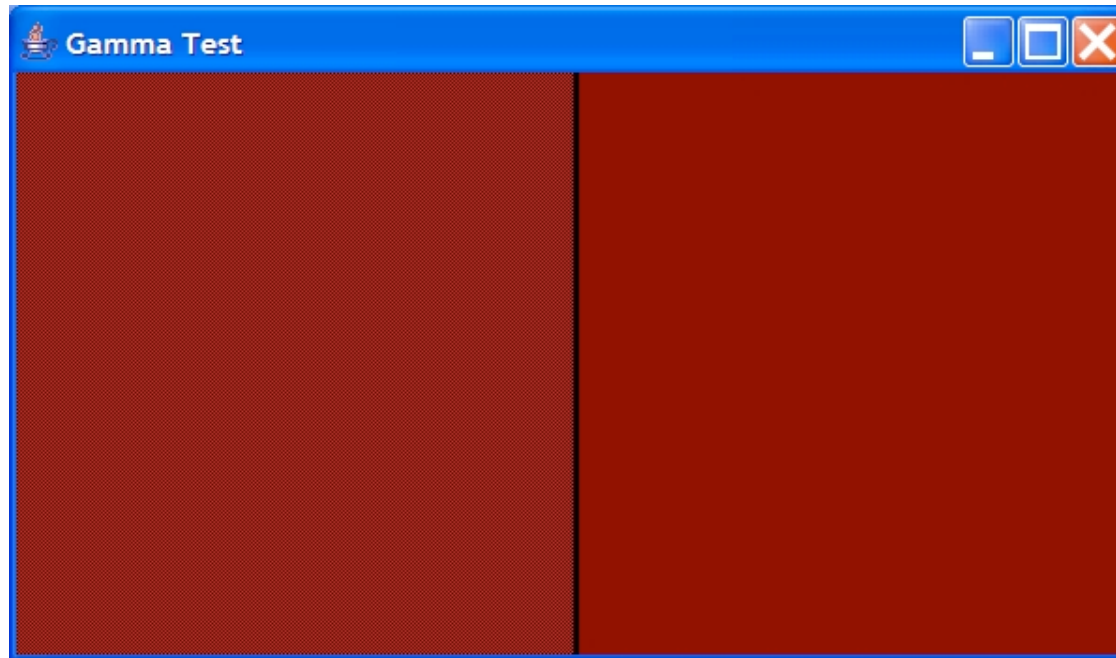


Gamma Correction

- Generally, the displayed intensity is not linear in the input ($0 \leq a \leq 1$).
- $\text{dispIntensity} = (\text{maxIntensity})a^\gamma$
- To find γ
 - Find a that gives you .5 intensity
 - Solve $.5 = a^\gamma$
 - $\gamma = \frac{\ln(.5)}{\ln(a)}$



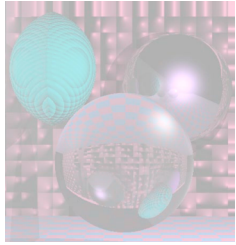
Gamma Correction



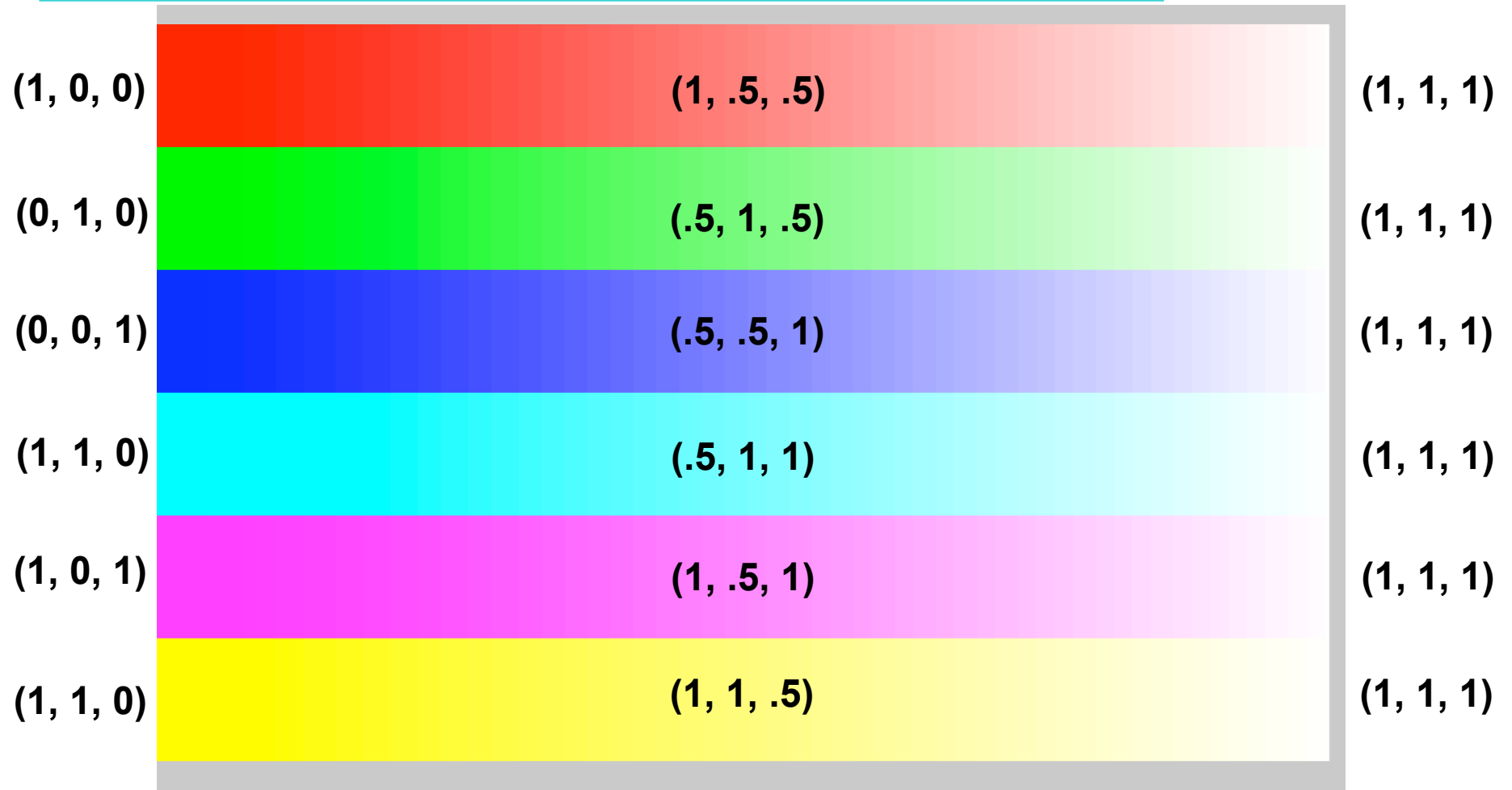
half black half red

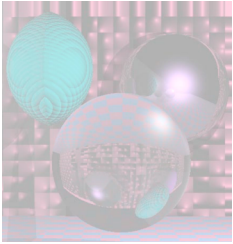
(127, 0, 0)

- Gamma



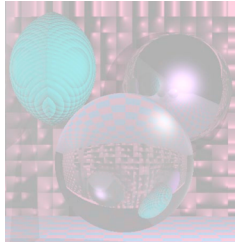
Making Pale Colors





Getting Paler, Left to Right

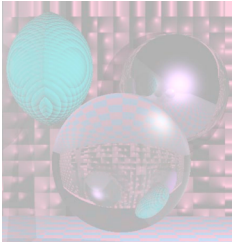
```
for (int w = 0; w < 256; w++){  
    c = new Color(255, w, w); g.setPaint(c);  
    g.fillRect(3*w, 50, 3, 150);  
    c = new Color(w, 255, w); g.setPaint(c);  
    g.fillRect(3*w, 200, 3, 150);  
    c = new Color(w, w, 255); g.setPaint(c);  
    g.fillRect(3*w, 350, 3, 150);  
    c = new Color(w, 255, 255); g.setPaint(c);  
    g.fillRect(3*w, 500, 3, 150);  
    c = new Color(255,w, 255); g.setPaint(c);  
    g.fillRect(3*w, 650, 3, 150);  
    c = new Color(255, 255, w); g.setPaint(c);  
    g.fillRect(3*w, 800, 3, 150);  
}
```



Portable Pixmap Format (ppm)

A "magic number" for identifying the file type.

- A ppm file's magic number is the two characters "P3".
 - Whitespace (blanks, TABs, CRs, LFs).
- A width, formatted as ASCII characters in decimal.
 - Whitespace.
- A height, again in ASCII decimal.
 - Whitespace.
- The maximum color value again in ASCII decimal.
 - Whitespace.
- Width * height pixels, each 3 values between 0 and maximum value.
 - start at top-left corner; proceed in normal English reading order
 - three values for each pixel for red, green, and blue, resp.
 - 0 means color is off; maximum value means color is maxxed out
 - characters from "#" to end-of-line are ignored (comments)
 - no line should be longer than 70 characters



ppm Example

P3

feep.ppm

4 4

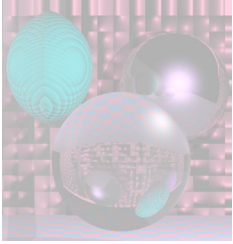
15

```
0 0 0 0 0 0 0 0 0 0 15 0 15
0 0 0 0 15 7 0 0 0 0 0 0 0
0 0 0 0 0 0 0 0 15 7 0 0 0
15 0 15 0 0 0 0 0 0 0 0 0 0
```

```

private void saveImage() {
    String outFileFileName = "my.ppm";
    File outFile = new File(outFileFileName);
    int clrR, clrG, clrB;
    try {
        PrintWriter out = new PrintWriter(new BufferedWriter(new FileWriter(outFile)));
        out.println("P3");
        out.print(Integer.toString(xmax-xmin+1)); System.out.println(xmax-xmin+1);
        out.print(" ");
        out.println(Integer.toString(ymax-ymin+1)); System.out.println(ymax-ymin+1);
        out.println("255");
        for (int y = ymin; y <= ymax; y++){
            for (int x = xmin; x <= xmax; x++) {
                // compute clrR, clrG, clrB
                out.print(" "); out.print(clrR);
                out.print(" "); out.print(clrG);
                out.print(" "); out.println(clrB);
            }
        }
        out.close();
    } catch (IOException e) {
        System.out.println(e.toString());
    }
}

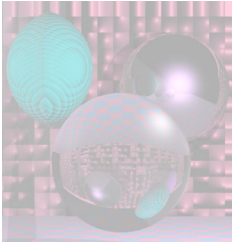
```

Math Basics

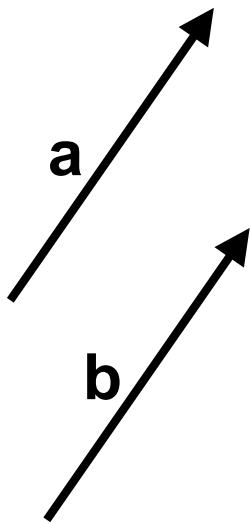
(All Readings from Shirley)

- Sets and Mappings – 2.1
- Quadratic Equations – 2.2
- Trigonometry – 2.3
- Vectors – 2.4
- 2D Parametric Curves – 2.6
- 3D Parametric Curves – 2.8
- Linear Interpolation – 2.10
- Triangles – 2.11



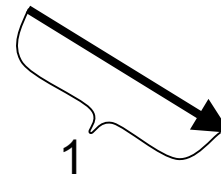
Vectors

- A *vector* describes a length and a direction.

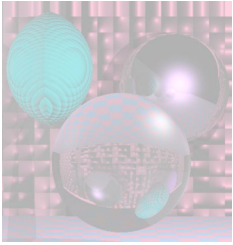


$$\mathbf{a} = \mathbf{b}$$

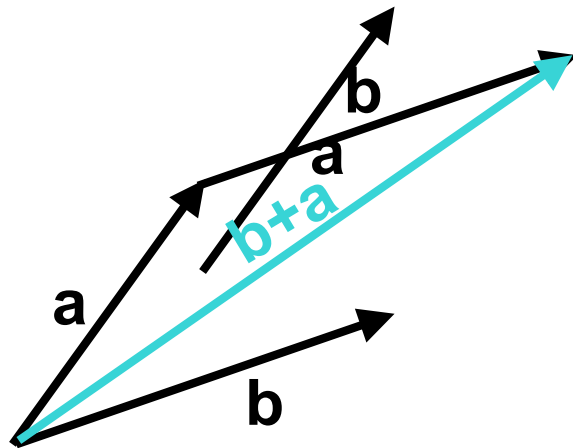
- a zero length vector



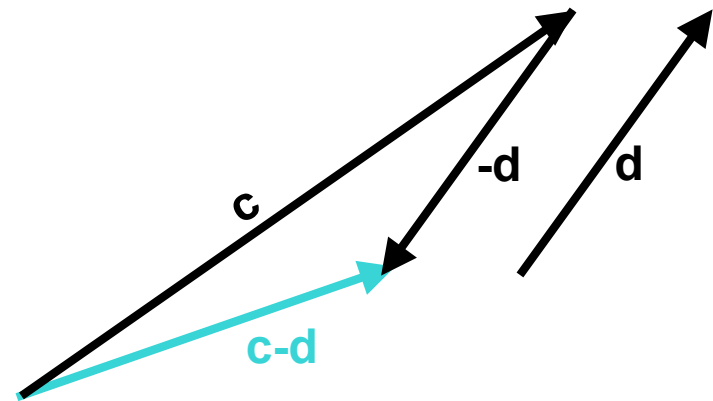
a unit vector



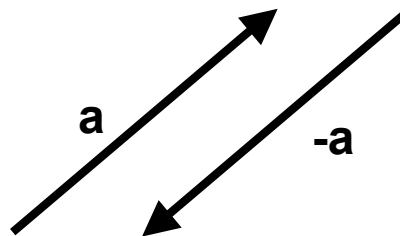
Vector Operations

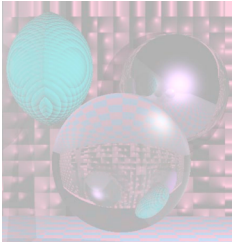


Vector Sum



Vector Difference





Cartesian Coordinates

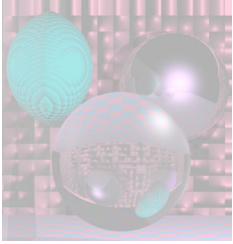
- Any two non-zero, non-parallel 2D vectors form a *2D basis*.
- Any 2D vector can be written uniquely as a linear combination of two 2D basis vectors.
- \mathbf{x} and \mathbf{y} (or \mathbf{i} and \mathbf{j}) denote unit vectors parallel to the *x-axis* and *y-axis*.
- \mathbf{x} and \mathbf{y} form an *orthonormal* 2D basis.

$$\mathbf{a} = x_a \mathbf{x} + y_a \mathbf{y}$$

$$\mathbf{a} = (x_a, y_a) \quad \text{or} \quad \mathbf{a} = \begin{bmatrix} x_a \\ y_a \end{bmatrix}$$

$$\text{or } \mathbf{a} = (a_x, a_y)$$

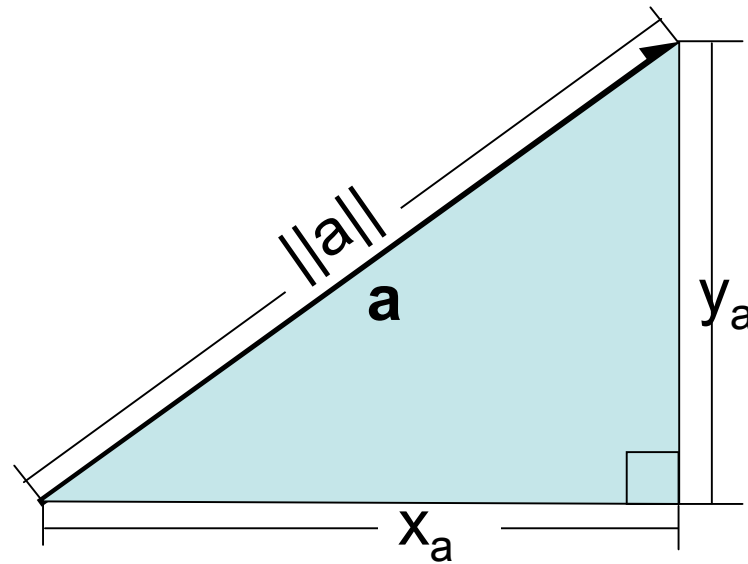
- \mathbf{x} , \mathbf{y} and \mathbf{z} form an *orthonormal* 3D basis.

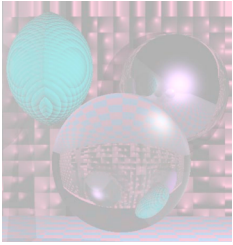


Vector Length

Vector $\mathbf{a} = (x_a, y_a)$

$$\text{Length}(\mathbf{a}) = \text{Norm}(\mathbf{a}) = \|\mathbf{a}\| = \sqrt{x_a^2 + y_a^2}$$





Dot Product

Dot Product

$$\mathbf{a} = (x_a, y_a) \quad \mathbf{b} = (x_b, y_b)$$

$$\mathbf{a} \cdot \mathbf{b} = x_a x_b + y_a y_b$$

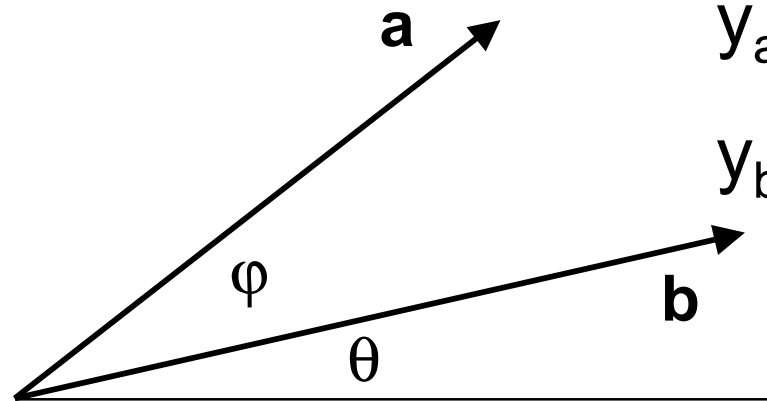
$$\mathbf{a} \cdot \mathbf{b} = \|\mathbf{a}\| \cdot \|\mathbf{b}\| \cos(\varphi)$$

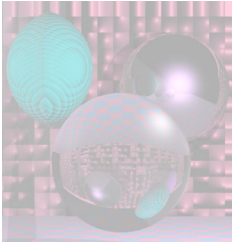
$$x_a = \|\mathbf{a}\| \cos(\theta + \varphi)$$

$$x_b = \|\mathbf{b}\| \cos(\theta)$$

$$y_a = \|\mathbf{a}\| \sin(\theta + \varphi)$$

$$y_b = \|\mathbf{b}\| \sin(\theta)$$





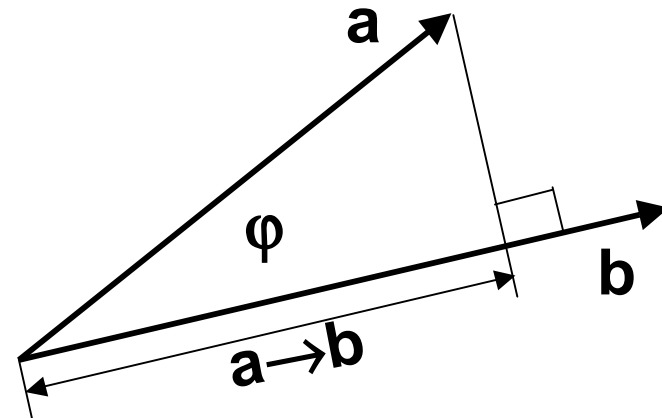
Projection

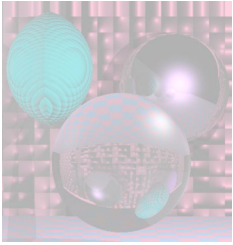
$$\mathbf{a} = (x_a, y_a) \quad \mathbf{b} = (x_b, y_b)$$

$$\mathbf{a} \cdot \mathbf{b} = \|\mathbf{a}\| \cdot \|\mathbf{b}\| \cos(\varphi)$$

The length of the projection of \mathbf{a} onto \mathbf{b} is given by

$$\mathbf{a} \rightarrow \mathbf{b} = \|\mathbf{a}\| \cos(\varphi) = \frac{\mathbf{a} \cdot \mathbf{b}}{\|\mathbf{b}\|}$$





3D Vectors

This all holds for 3D vectors too.

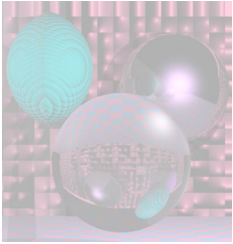
$$\mathbf{a} = (x_a, y_a, z_a) \quad \mathbf{b} = (x_b, y_b, z_b)$$

$$\text{Length}(\mathbf{a}) = \text{Norm}(\mathbf{a}) = \|\mathbf{a}\| = \sqrt{x_a^2 + y_a^2 + z_a^2}$$

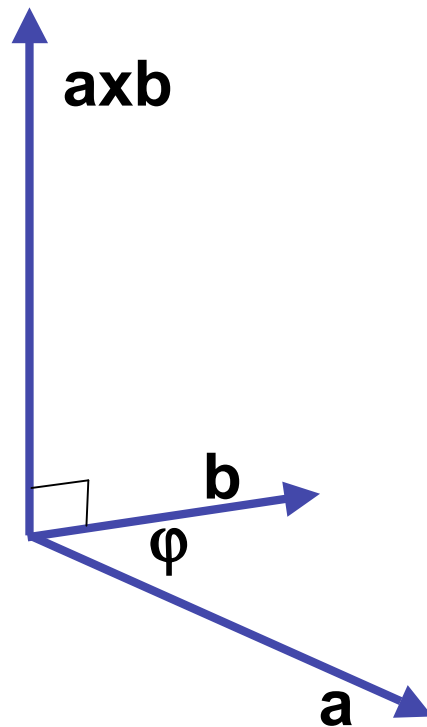
$$\mathbf{a} \cdot \mathbf{b} = x_a x_b + y_a y_b + z_a z_b$$

$$\mathbf{a} \cdot \mathbf{b} = \|\mathbf{a}\| \cdot \|\mathbf{b}\| \cos(\varphi)$$

$$\mathbf{a} \rightarrow \mathbf{b} = \|\mathbf{a}\| \cos(\varphi) = \frac{\mathbf{a} \cdot \mathbf{b}}{\|\mathbf{b}\|}$$



Vector Cross Product



$$\|\mathbf{a} \times \mathbf{b}\| = \|\mathbf{a}\| \|\mathbf{b}\| \sin \varphi$$

$\mathbf{a} \times \mathbf{b}$ is perpendicular to \mathbf{a} and \mathbf{b} .

Use the right hand rule to determine the direction of $\mathbf{a} \times \mathbf{b}$.

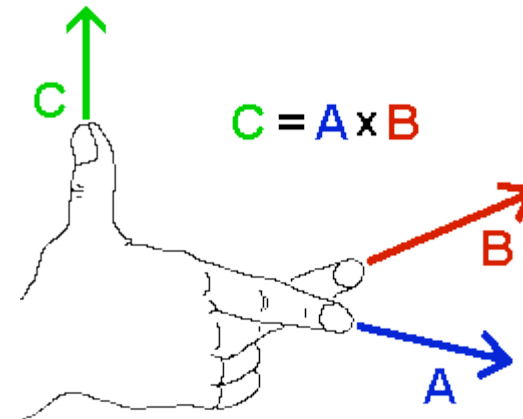
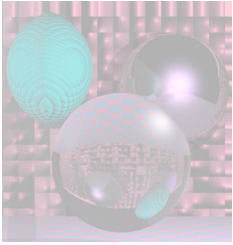
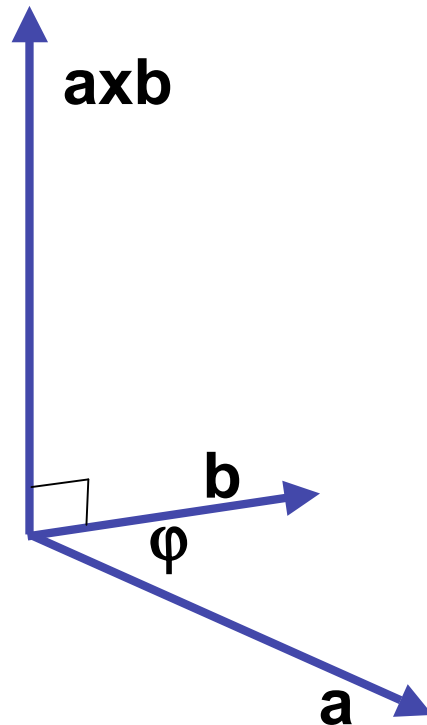


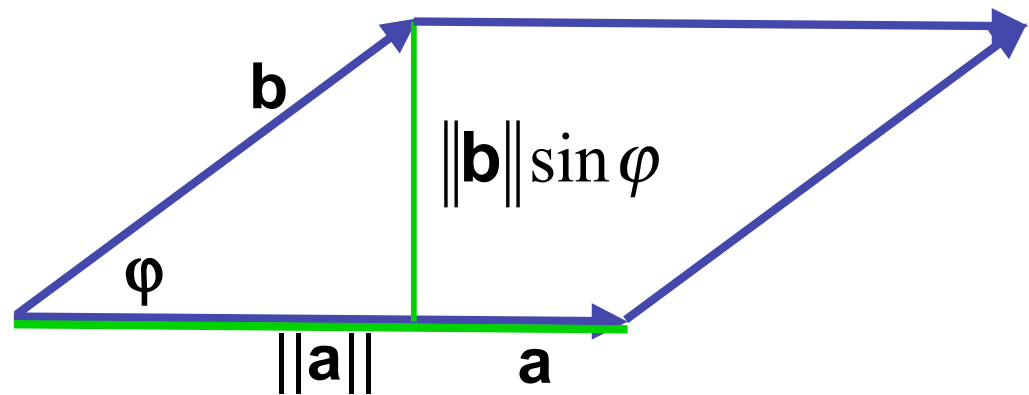
Image from www.physics.udel.edu



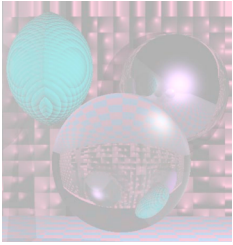
Cross Product and Area



$$\|\mathbf{a} \times \mathbf{b}\| = \|\mathbf{a}\| \|\mathbf{b}\| \sin \varphi$$



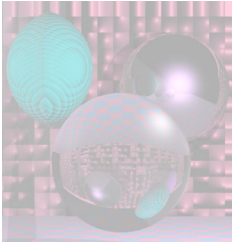
$$\|\mathbf{a}\| \times \|\mathbf{b}\| = \text{area of the parallelogram.}$$



Computing the Cross Product

$$\mathbf{a} \times \mathbf{b} = \begin{vmatrix} i & j & k \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$$

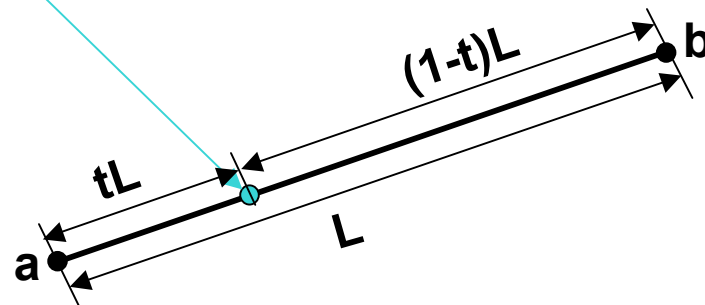
$$= (a_y b_z - a_z b_y)i + (a_z b_x - a_x b_z)j + (a_x b_y - a_y b_x)k$$

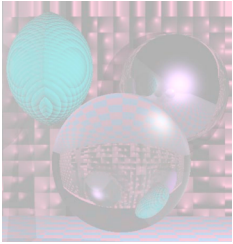


Linear Interpolation

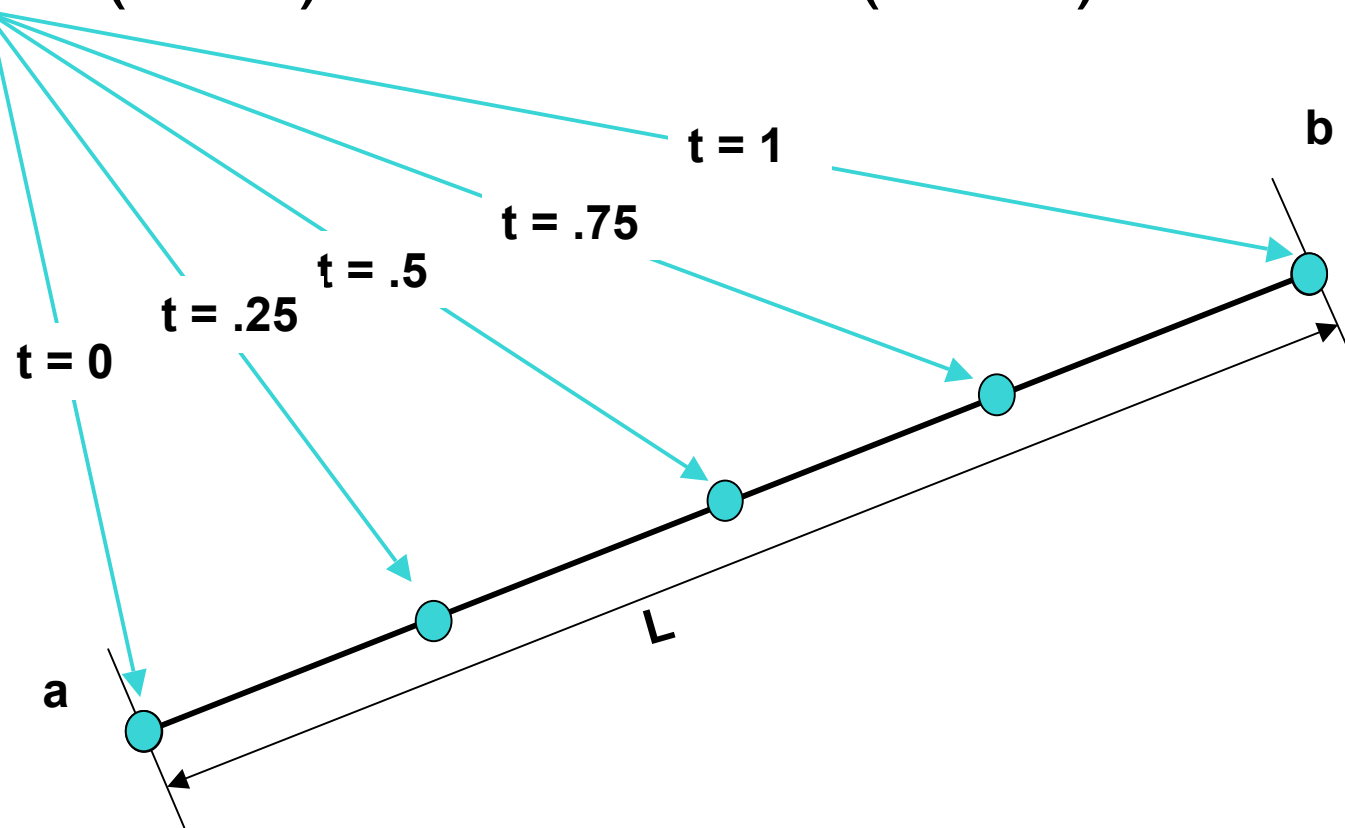
- **LERP**: /lerp/, vi.,n.
 - Quasi-acronym for Linear Interpolation, used as a verb or noun for the operation.
 - “Bresenham's algorithm lerps incrementally between the two endpoints of the line.”

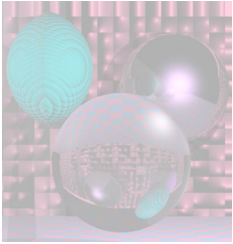
$$p = (1 - t) a + t b = a + t(b - a)$$



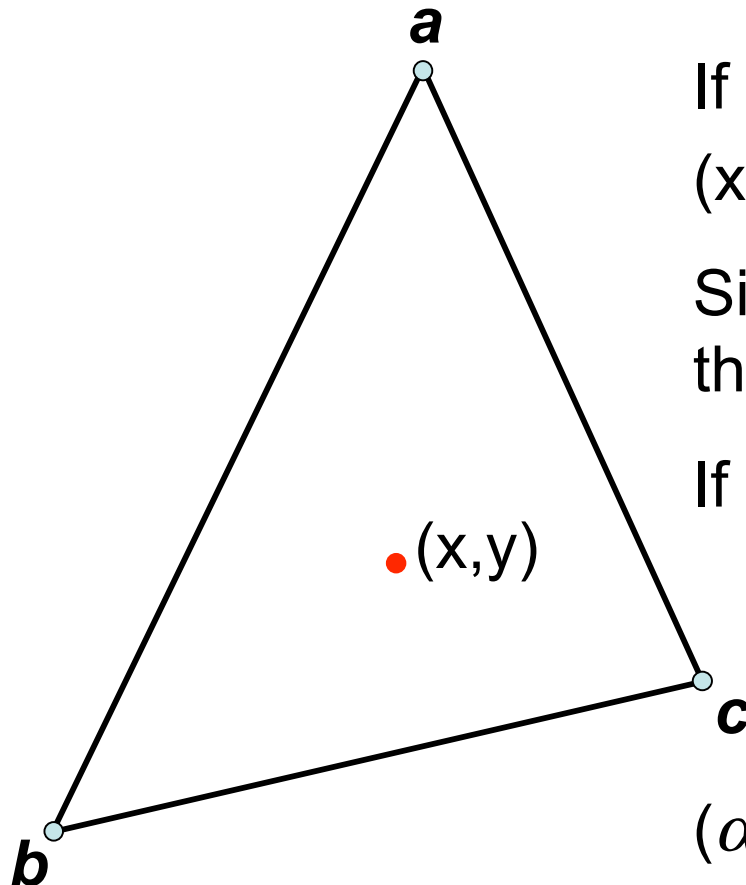


$$p = (1 - t) a + t b = a + t(b - a)$$





Triangles



If (x, y) is on the edge ab ,
 $(x, y) = (1 - t) a + t b = a + t(b - a)$.

Similar formulas hold for points on the other edges.

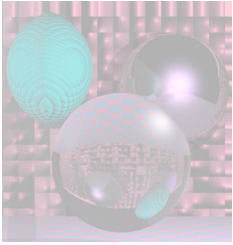
If (x, y) is in the triangle:

$$(x, y) = \alpha a + \beta b + \gamma c$$

$$\alpha + \beta + \gamma = 1$$

(α, β, γ) are the

Barycentric coordinates of (x, y) .



Triangles

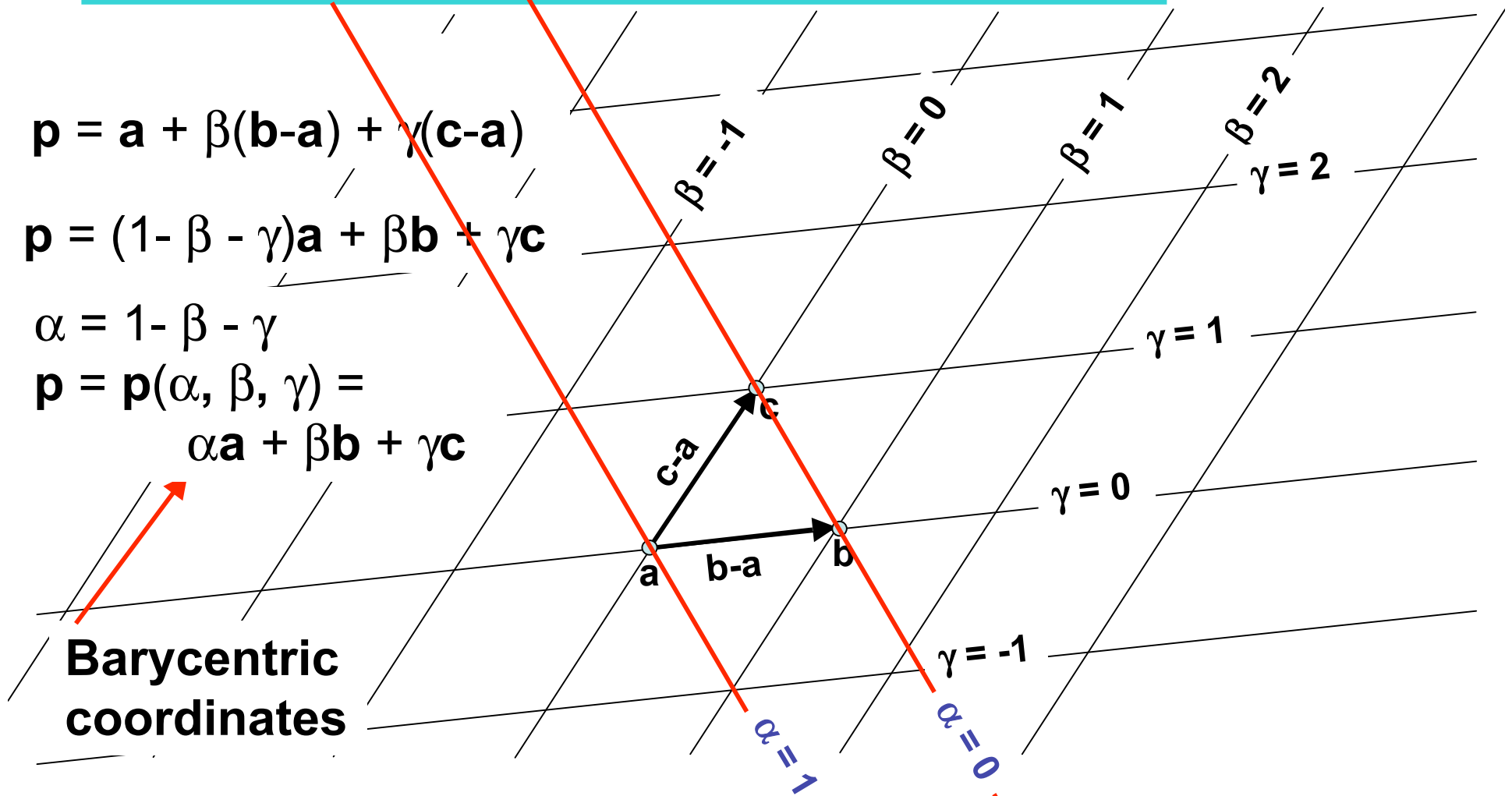
$$\mathbf{p} = \mathbf{a} + \beta(\mathbf{b}-\mathbf{a}) + \gamma(\mathbf{c}-\mathbf{a})$$

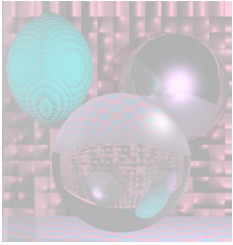
$$\mathbf{p} = (1 - \beta - \gamma)\mathbf{a} + \beta\mathbf{b} + \gamma\mathbf{c}$$

$$\alpha = 1 - \beta - \gamma$$

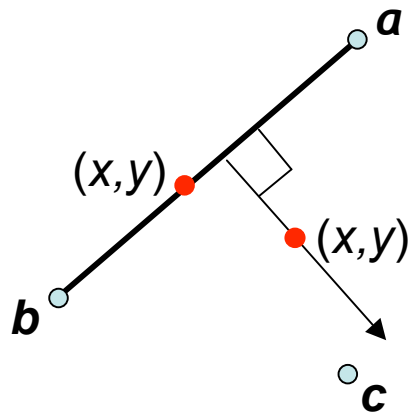
$$\mathbf{p} = \mathbf{p}(\alpha, \beta, \gamma) = \alpha\mathbf{a} + \beta\mathbf{b} + \gamma\mathbf{c}$$

**Barycentric
coordinates**





Computing Barycentric Coordinates

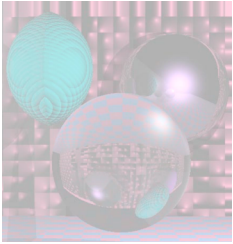


$$\frac{y - y_a}{x - x_a} = \frac{y_b - y_a}{x_b - x_a}$$

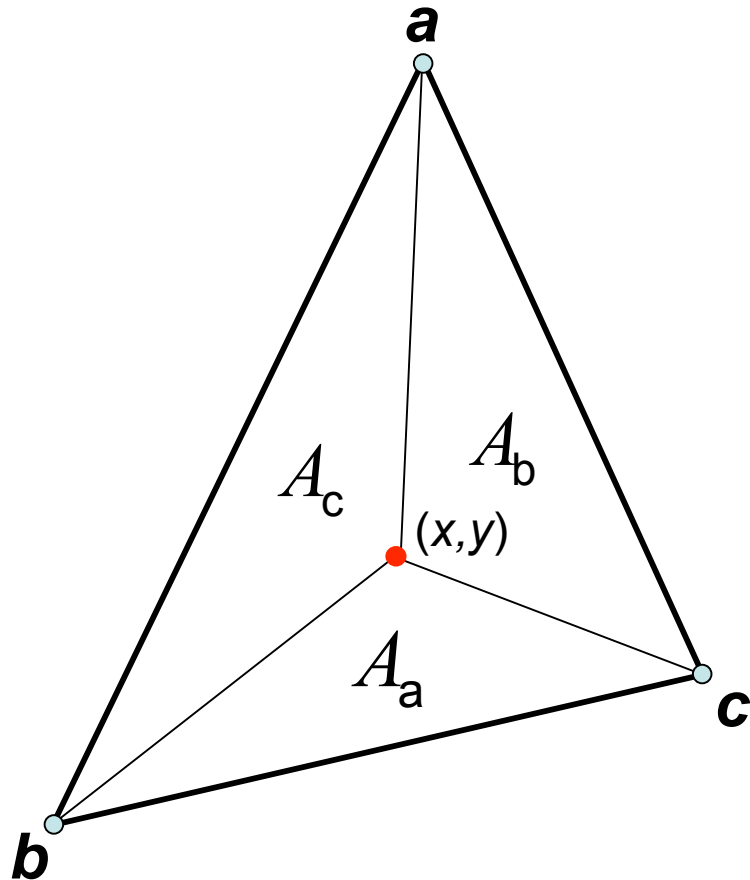
$$(y - y_a)(x_b - x_a) - (y_b - y_a)(x - x_a) = 0$$

$$f_{ab}(x, y) = (y - y_a)(x_b - x_a) - (y_b - y_a)(x - x_a)$$

$$\gamma = \frac{f_{ab}(x, y)}{f_{ab}(x_c, y_c)}$$



Barycentric Coordinates as Areas



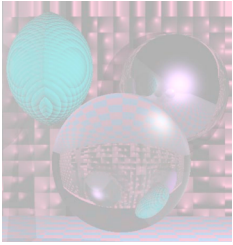
$$\alpha = A_a / A$$

$$\beta = A_b / A$$

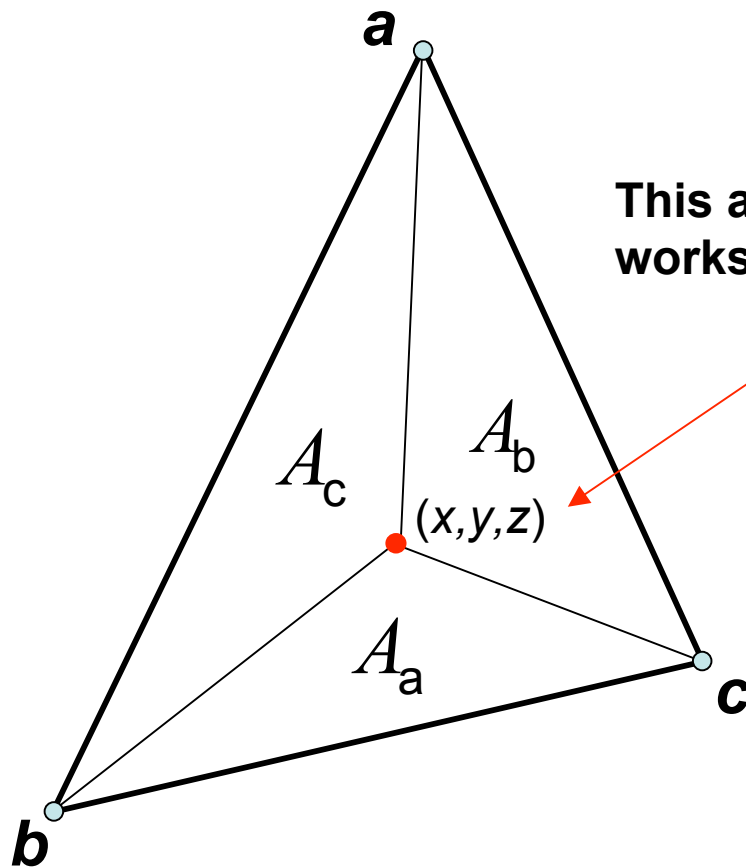
$$\gamma = A_c / A$$

where A is the area of the triangle.

$$\alpha + \beta + \gamma = 1$$



3D Triangles



This all still works in 3D.

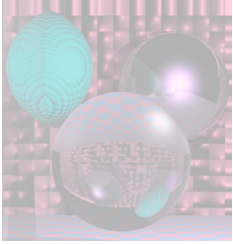
$$\alpha = A_a / A$$

$$\beta = A_b / A$$

$$\gamma = A_c / A$$

where A is the area of the triangle.

$$\alpha + \beta + \gamma = 1$$



Assignment 0

- You will choose a programming platform for the quarter and familiarize yourself with RGB color and the ppm format. In part, this assignment is to ensure that you have a method of submitting your work so that I can:
 - read the code
 - compile (or interpret) the code
 - run the code to produce a file in ppm format.
- [Sample Program](#)
- You will write your own 3D vector tools (e.g. as a JAVA class) that you will use for your later programming assignments.