Functional Adaptive Programming

A dissertation presented

by

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Abstract

The development of complex software requires the implementation of operations over recursively defined data structures. Complex data structures lead to an increase of code dealing with structure access and navigation. This 'boilerplate' code in turn makes programs tedious to develop, difficult to maintain, prone to errors, and separates important functionality, all of which result in the loss of clarity. Generic (or polytypic) programming and higher-order functions can resolve some of these issues, but are usually too general to be practically useful for large collections of data types.

This dissertation proposes a new approach to developing structure-based functions and describes an implementation of these ideas in Java, called DemeterF. Our approach uses function-objects over an adaptive traversal to implement deep, fold-like functions over data structures. Function-classes (and objects) provide a useful and flexible form of generic programming that adapts to different data structures using a type-based multiple dispatch. We model DemeterF with function sets and structural recursion, and give it a type system that shows our function-objects, multiple dispatch, and traversals can be checked for safety. In order to show that our approach is efficient we present the results of several performance tests comparing DemeterF to handwritten methods and visitor implementations in Java.

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¹After all, he is a yoga instructor.

²Technically 7, or maybe 11, but who's counting now...

³Note the single 'n'.

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There are two ways of constructing a software design: one way is to make it so simple that there are obviously no deficiencies, and the other way is to make it so complicated that there are no obvious deficiencies.

— Tony Hoare

CHAPTER 1

Introduction

The development of complex software requires programmers to implement operations over a variety of recursively defined data structures. While the design and modeling of interesting data structures can be difficult, complex data leads to more complex operations. A typical side-effect of complex data structures is an increase in so-called *boilerplate* code (*c.f.*, listings 1.2 and 1.2) that deals with data structure access and navigation. Boilerplate code makes programs tedious to develop, prone to errors, and difficult to maintain, and entangles and scatters important functionality, resulting in a loss of software clarity.

In object-oriented methodology the scattering of interesting code is obvious (and extreme), since functions (*i.e.*, methods) are grouped by class. Abstract classes can be viewed as types, with concrete subclasses akin to *value constructors*.¹ Each class contains all of its related methods, though common cases can be moved up to a common superclass.

In functional languages the scattering of functionality is a bit more subtle. Since each function handles a single type, it usually contains cases for all value constructors of a datatype. When implementing a single operation over small, self-recursive datatypes, a single function will suffice. Complex data structures are, however, typically made up of multiple mutuallyrecursive types. Since each type requires a separate function, our initial cohesion is lost.

Taming increases in the structural complexity of software requires a different approach, and typical solutions differ by implementation language and paradigm. In class-based object-oriented languages, such as Java [30] or C# [33], the visitor design pattern [27] is traditionally used as a guide to separate operations from data structures. In functional languages like Haskell [39], ML [58], or Scheme [40], reusable computation is abstracted into *higher-order* functions called folds [36]. Neither one is a perfect solution.

The visitor pattern is useful for abstracting certain parts of an implementation, *e.g.*, case dispatch or data structure traversal, but there is a tension

¹More accurately, an abstract class is like a *type constructor* in, say, Haskell.

between safety and flexibility. Many instantiations of the pattern, including the original description, opt for imperative, *i.e.*, void, methods rather than forcing clients to deal with return types, contravariance, and composition. Imperative methods force clients to implement functionality via mutation to shared state, which makes functions difficult, if not impossible, to understand. The pattern can be functionalized [43, 61], but not without inhibiting safety, flexibility, or data structure extension. Overall, the visitor pattern is simply a *pattern* for separating operations from structures, and is not meant to help programmers deal directly with complex data hierarchies.

In contrast, functional languages typically separate the definitions of functions and data structures. Since functions are values, programmers typically write structurally recursive functions, called *folds*, that act as recursion operators, replacing value constructors, like cons, with client functions. Generalized folds [55, 65] provide a blueprint for writing (or generating) fold abstractions for user-defined datatypes, but with more complex datatypes containing multiple or mutually-recursive types, the number and order of functions that must be passed can quickly become overwhelming. Polytypic programming [38, 54, 28, 9] provides a similar service, allowing programmers to define functions that are applicable to *all* datatypes. There are situations where this is useful, but functions are usually defined over a universal datatype consisting of binary sum and product types. The universal nature of the definitions makes writing functions that require high-level datatype notions impossible. For example, an evaluation function for an abstract syntax tree must operate on expressions and values, structural information which is lost in the low level encoding.

1.1 My Thesis

This dissertation presents a complete reformulation of Adaptive Programming (AP) [52] to provide a flexible, safe, and efficient approach to writing side-effect free operations over complex data structures in an object-oriented setting. We refer to the approach as *functional adaptive programming*, or AP-F. The goals of AP-F are to: (1) eliminate the boilerplate code associated with the implementations of data structures and operations, (2) separate and modularize interesting functionality while retaining safety, and (3) provide maximum flexibility in both function and traversal implementations, while maintaining a high level of performance.

We achieve these goals by grouping methods of an operation into a *function-class*, instances of which (*i.e.*, *function-objects*) are applied over a data structure by a generic traversal. After an object's fields have been processed, the traversal uses a type-based multiple dispatch to select an appropriate method that matches the type of the current object and the types of the recursive results. The separation of traversal, function-objects, and dispatch supports four important features:

- *Function-class extension*: new methods can be added using normal object-oriented inheritance,
- *Case abstraction*: a single method can be called for multiple type cases,
- *Case specialization*: a more specific method/signature can override a more general one, and
- *Traversal control*: recursion can be easily controlled/limited for efficiency and/or algorithm correctness.

This brings me to my thesis:

Function-objects applied over data structure traversals are a useful, safe, and efficient way to write functions.

In support of this thesis I have developed *DemeterF* [16, 19], a library and collection of tools that enable flexible, safe, and efficient traversal-based (generic) programming with function-objects/classes. My implementation combines features of object-oriented traversals, adaptive programming [52], higher-order functions, and multiple dispatch to support the development of traversal-based functions that are flexibly typed, provably safe, and efficient to execute.

1.2 Dissertation Outline

The rest of this dissertation is structured as follows:

- The rest of this chapter gives a background on functions, data structures, and traversals.
- In chapter 2, I introduce DemeterF, its class generator, and its traversal library. I use examples to demonstrate my approach to traversal-based programming with function-objects and how they can be used for both specific and generic programming.
- I then present a model of DemeterF's essential features in chapter 3, providing syntax, a small-step operational semantics, and a type system. I prove that our model of dispatch is type safe, meaning that well-typed traversals do not *go wrong*.
- Chapter 4 describes the implementation of DemeterF and its connection to the model. In particular I focus on the use of traversals, function objects, and algorithms within the context of the system's class/traversal generation and type checking.
- Chapter 5 discusses abstractions of several algorithms involved in the implementation, safety, and performance of DemeterF-based programs.

- The final portion of my thesis is addressed in chapter 6, where I discuss empirical results of testing the performance of a number of DemeterF-based programs, including DemeterF itself.²
- Chapter 7 discusses previous works related to AP-F, DemeterF, and my implementation.
- Chapter 8 completes the dissertation with conclusions and a discussion of future work.

1.3 Background

I complete the introduction by giving a background of data structures, operations, and traversals, sprinkled with a brief review of related work.

1.3.1 Data Structures and Operations

There are two main schools of thought as to the definition and extension of data structures and operations. The first is well known by object-oriented programmers, where operations are grouped together with the structure to which they apply. I refer to this organization as *datatype-centric*, since it allows programmers to easily extend their datatypes, but adding new operations requires programmers to add a new method to each of the classes of related datatypes. On the other side is the more function-based approach that one uses, for instance, in Scheme. I refer to this as *function-centric*, since it allows programmers to easily add new functions to her system, but adding a new datatype case requires an addition to the functions of all related datatypes.

Of course, this data versus function dilemma is not new. It is traditionally called the *expression problem* (a term coined by Wadler [71]) and has been studied extensively [43, 74, 14, 68, 1, 60]. To make the idea more concrete, we will illustrate using representations of an abstract syntax tree (AST) of Boolean expressions. Our initial structures will include Boolean literals (True and False), unary negation, and binary And and Or.

1.3.1.1 Datatype-Centric: Java

We begin by representing the structures in a typical class-based object-oriented language, namely Java. Listing 1.1 shows straightforward class definitions that describe our types to represent Boolean expressions, BExps. We use **abstract** classes to represent disjoint unions, *e.g.*, BExp and Lit, and concrete classes to represent variants, *e.g.*, True and False. An instance of BExp that represents the expression $(true \land \neg false)$ can be constructed as follows:

²DemeterF is, of course, implemented in DemeterF.

```
// Boolean Expression
                                         // Binary And
abstract class BExp{}
                                         class And extends BExp{
                                           BExp left, right;
// Literals
                                            And(BExp left, BExp right)
abstract class Lit extends BExp{}
                                            { /*...*/ }
class True extends Lit{}
                                        }
class False extends Lit{}
                                        // Binary Or
// Negation
                                        class Or extends BExp{
class Neg extends BExp{
                                            BExp left, right;
  BExp inner;
                                           Or(BExp left, BExp right)
   Neg(BExp inner){ /*...*/ }
                                            { /*...*/ }
}
```

Listing 1.1: Boolean expression structures in Java.

If we follow good object-oriented style, then implementing an operation over BExps requires that we add a new method to each class. Listing 1.2 shows an implementation of evaluation, eval(), which reduces a BExp to a Lit representing true or false. The comments above the methods describe into

```
// Added to Neg
// Added to BExp
abstract Lit eval();
                                          Lit eval(){
                                            if(inner.eval().isTrue())
                                              return new False();
// Added to Lit
                                            return new True();
abstract Lit eval();
                                          }
                                          // Added to And
abstract boolean isTrue();
                                          Lit eval(){
                                            if(left.eval().isTrue())
// Added to True
                                              return right.eval();
Lit eval(){ return this; }
                                            return new False();
boolean isTrue(){ return true; }
                                          }
                                          // Added to Or
// Added to False
                                          Lit eval(){
Lit eval(){ return this; }
                                            if(!left.eval().isTrue())
boolean isTrue(){ return false; }
                                              return right.eval();
                                            return new True();
                                          }
```

Listing 1.2: Boolean expression evaluation in Java.

which class they should be placed. We use Lit rather than **boolean** in order to provide a fair comparison between later implementations in different languages.

Within the Lit and **BExp** classes we introduce an **abstract** method, eval() that will be implemented in concrete subclasses. For True and False we simply return **this** instance of Lit. To determine the representative **boolean** value of a Lit we introduce another **abstract** helper method, isTrue(), within Lit, and provide implementations in True and False. The eval methods for other concrete classes are straightforward, testing the result of recursive eval calls to subcomponents and returning the correct result.

Operation Extension Adding a new operation requires us to add a new method to each class. For example, adding an operation to convert a BExp to a String requires the addition of a toString() method to each class. Most method implementations will follow a similar pattern to eval, but will nonetheless be spread throughout our class definitions.

Datatype Extension In contrast, adding a new datatype is comparatively easy. For example, adding an Xor expression variant only requires that we add a new class, shown in listing 1.3. The class **extends** BExp, and provides

```
class Xor extends BExp{
  BExp left, right;
  Or(BExp left, BExp right){ /*...*/ }
  Lit eval(){ /*...*/ }
  String toString(){ /*...*/ }
}
```

Listing 1.3: Datatype extension in Java

implementations for each of its operations, similar to And and Or.³

1.3.1.2 Function-Centric: Scheme

Similar Boolean expression structures can also be defined in a functional language. Listing 1.4 shows a structure-based Boolean expression representation written in Scheme. Our use of **define-struct** is analogous to our

```
;; A BExp is one of Lit, Neg,...
;; A Lit is one of True or False
;; (make-True)
(define-struct True ())
;; (make-False)
(define-struct False ())
;; (make-Neg BExp)
(define-struct Neg (inner))
;; (make-And BExp BExp)
(define-struct And (left right))
;; (make-Or BExp BExp)
(define-struct Or (left right))
```

Listing 1.4: Boolean expression structures in Scheme.

concrete classes in Java. Comments take the place of abstract classes, documenting our intended unions, *e.g.*, BExp and Lit, and the expected values to be stored in our concrete structures. A value representing the expression $(true \land \neg false)$ can be constructed as follows:

8

³We could actually have extended And or Or in order to partially reuse an implementation of eval, but this is clearer, and maintains our implicit ideal of subsumption.

```
(make-And (make-True)
          (make-Neg (make-False)))
```

In Scheme we can implement most operations on BExps as a single function. We use a **cond** expression to differentiate between the structure variants, and decompose the concrete structure to compute a result. For example, listing 1.5 shows an implementation of evaluation, eval, which reduces a BExp to a Lit representing #t or #f.⁴ There is a **cond**-clause for each de-

Listing 1.5: Boolean expression evaluation in Scheme

fined structure that handles its particular case, but the implementation is otherwise identical in spirit to the Java methods.

Datatype Extension Adding a new datatype requires us to add a new case to each previously defined function. Following our Java example, adding a new Xor structure requires us to update the implementation of eval by adding a new case to the **cond**. If there are more operations on BExps then our necessary updates are scattered throughout the program.

Operation Extension On the other hand, adding a new operation only requires that we add a new function. Following our Java example, adding an operation to convert a BExp to a string is shown in listing 1.6. The imple-

```
;; tostring: BExp -> string
(define (tostring e)
   (cond [(True? e) "true"]
       [(False? e) "false"]
       [(Neg? e) #/.../#]
       [(And? e) #/.../#]
       [(0r? e) #/.../#])
```

Listing 1.6: Operational extension in Scheme

⁴In Scheme examples we will use both parentheses () and square brackets [] within code for readability.

mentation follows a similar pattern to eval, selecting branches of the cond based on the structure type, but all our functionality is centrally located.

1.3.2 Implementing Operations

While the organization of datatypes and operations differs in our two examples, they do have something in common. When implementing operations (functions and methods) over a data structure, each operation requires a large amount of code that deals with structural recursion. Our function/method has a recursive call at every point where our data structure is recursive.⁵ In many situations the code dealing strictly with structural recursion is almost identical across all operations. In this section we review solutions that attempt to remove structural boilerplate code. We discuss the limitations of these solutions and mention related work and extensions to the approaches.

1.3.2.1 Visitors and Traversals

It is likely that every object-oriented programmer has seen or heard of the visitor pattern in one form or another. The original description by Gamma *et al.* [27] uses a combination of accept and visit methods to define operations over a collection of classes (*i.e.*, a class hierarchy). Operation specific behavior is modularized into a Visitor instance that implements visit methods. The accept methods are placed within the class hierarchy to implement a traversal over the structures while making calls to a visitor object's visit methods.

A Java imperative visitor interface, ImpVis, is given in listing 1.7(a). Shown in listing 1.7(b) is a functional visitor interface, FunVis, similar to

<pre>interface ImpVis{ void visit(True e); void visit(False e); void visit(Neg e); void visit(And e); void visit(Or e); }</pre>	<pre>interface FunVis<r>{ R visit(True e); R visit(False e); R visit(Neg e, R inner); R visit(And e, R lft, R rht); R visit(Or e, R lft, R rht); }</r></pre>
(a) Imperative	(b) Functional

Listing 1.7: Visitor Interfaces in Java

the presentation of Oliveira *et al.* [61]. An imperative visitor implements **void** methods that communicate using the visitor's local state. In contrast, the functional visitor is parametrized by a type R, which represents the return type of the operation to be implemented. In addition to this type parameter,

⁵Sometimes recursive calls may be to *other* functions/methods that coordinate to implement the same operation.

the functional visit methods also have more method arguments than the corresponding imperative methods. The functional visit methods for composite classes like Neg and And have extra arguments that represent recursive results of visiting corresponding subcomponents.

The final piece of the visitor puzzle is the implementation of accept methods that must be added to our BExp classes. The corresponding accept methods are shown in listing 1.8: (a) shows imperative accept methods and (b) shows the functional counterpart.⁶ False and Or cases are left out

```
// Added to BExp
                                    // Added to BExp
abstract void accept(ImpVis v);
                                    abstract <R> R accept(FuncVis<R> v);
                                    // Added to True
// Added to True
                                    <R> R accept(FuncVis<R> v)
void accept(ImpVis v)
{ v.visit(this); }
                                    { return v.visit(this); }
// Added to Neg
                                    // Added to Neg
void accept(ImpVis v){
                                    <R> R accept(FuncVis<R> v){
  inner.accept(v);
                                      return v.visit(this,
  v.visit(this);
                                                      inner.accept(v));
r
                                    }
// Added to And
                                    // Added to And
                                    <R> R accept(FuncVis<R> v){
void accept(ImpVis v){
  left.accept(v);
                                      return v.visit(this,
  right.accept(v);
                                                      left.accept(v),
  v.visit(this);
                                                      right.accept(v));
                                    }
}
      (a) Imperative Traversal
                                        (b) Functional Traversal
```

Listing 1.8: Accept methods for BExps

since they are similar to True and And, respectively. Together, the accept methods implement the *traversal* of a BExp instance. The visitor's visit methods are called at interesting points, effectively implementing *double-dispatch*. Calls to the specific visit methods are statically resolved within each class by the type of their first parameter, *e.g.*, v.visit(this, ...), since the type of this is known.⁷

With both forms of the visitor pattern in place, we can use visitors to implement Boolean expression evaluation. Using a visitor, we can now implement the operation *outside* of our BExp class definitions. Listing 1.9(a) and (b) give visitor implementations of eval in imperative and functional styles, respectively. Again, we elide the methods for False and Or since they are almost identical to those for True and And respectively. Because the imperative visitor, EvalImp, must operate via mutation, it keeps a Stack of evaluated Lit results. After the traversal of sub-expressions is complete, each accept method calls visit, passing the original BExp. Within the cor-

⁶Because the parameter types are different, these implementations can coexist in the same class hierarchy, though usually one visitor type is chosen over the other.

⁷technically the type of this cannot be known until runtime, but the Java compiler can at least determine a reasonable static bound.

```
class EvalImp implements ImpVis{
                                     class EvalFun implements FunVis<Lit>{
 Stack<Lit> stack = /*...*/;
 void visit(True e)
                                       Lit visit(True e)
 { stack.push(e); }
                                       { return e; }
  void visit(Neg e){
                                       Lit visit(Neg e, Lit inn){
    if(stack.pop().isTrue())
                                         if(inn.isTrue())
      stack.push(new False());
                                           return new False();
                                         return new True();
    else
      stack.push(new True());
                                       }
 7
 void visit(And e){
                                       Lit visit(And e, Lit lft, Lit rht){
    if(stack.pop().isTrue() &&
                                         if(lft.isTrue() && rht.isTrue())
       stack.pop().isTrue())
                                           return new lft();
      stack.push(new True());
                                         return new False();
    else
                                       }
      stack.push(new False());
 }
 Lit eval(BExp e){
                                       Lit eval(BExp e)
    e.accept(this);
                                       { return e.accept(this); }
                                     7
    return stack.pop();
 }
}
        (a) Imperative visitor
                                           (b) Functional visitor
```

Listing 1.9: Visitor-based eval implementations

responding visit method the necessary values are popped from the stack, tested, and the resulting Lit is pushed back on the stack.

The functional version, EvalFun, is implemented similarly. After subexpressions have been traversed, each accept method will call visit, passing the original BExp and the recursive accept results. Our functional version is much less complicated, since it uses the implicit call stack to manage recursion. In fact, it is almost identical to our earlier object-oriented version (listing 1.2), though it is now separated from the class definitions.

Each of the visitors also includes an eval entry point that invokes the initial accept method with **this** instance of the visitor. The imperative visitor must do a little more work. Since its return is stored in the stack, upon completion of the traversal the eval method must return the top of the stack (*i.e.*, pop()). Each of the operations can be invoked by creating a visitor instance and calling eval on a BExp:

```
new EvalImp().eval(a_bexp);
```

And similarly for EvalFun.

1.3.2.2 Visitor Limitations and Extensions

We have organized our methods this way (*i.e.*, accept and visit) so that the work done writing the accept methods (*i.e.*, the traversal) can be reused when we write new operations that follow this pattern. In theory visitors can be used to write all different kinds of operations, but in practice visitor im-

plementations have a number of limitations. Consequently, there have been many extensions to the pattern to deal with implementation challenges.

Necessary Methods The visitor implementation at a minimum requires the addition of accept methods to the relevant portions of a class hierarchy. When the programmer does not have control over the classes (*e.g.*, they are provided in binary form) this is much more difficult. When the programmer has control, writing these methods can be tedious and error prone.

Palsberg and Jay [63] introduced a special visitor, called Walkabout, that uses Java reflection to mimic double dispatch. Using reflection supports visitor extensions (*e.g.*, new visit methods) and allows the traversal to be implemented over unmodified class hierarchies. Grothoff [31] took a similar approach by compiling double-dispatch at runtime with Runabout, and the performance was greatly improved, In Aspect-Oriented Programming [41] this notion of making changes without prior knowledge is typically referred to as *obliviousness*.

Fixed Traversal Implementing a fixed traversal strategy within the class hierarchy makes writing different operations difficult, inefficient, or even impossible. For this reason most programmers simply use the visitor pattern as a way to modularize case dispatch, eliminating recursive accept calls within the class hierarchy. If, for example, we remove inner.accept(v) from Neg in the imperative case, or use inner in place of inner.accept(v) in the functional case, then the visitor can control its own traversal.

When the visitor is in charge of traversal, Buchlovsky and Thielecke [15] refer to them as *external* visitors, as the traversal is external to the datatypes. Oliveira *et al.* [61] demonstrated a functional visitor library⁸ that works with both *external* and *internal* accept implementations. Lämmel *et al.* [51, 44, 70] introduced composable strategies to define and constrain the order and depth of a traversal. Lieberherr *et al.* [52, 53] use a domain specific language to describe traversal strategies with imperative visitors.

In this dissertation we focus on a new approach that uses *external* traversals with different implementations. In the next chapter (section 2.3) we discuss *traversal control* (a simplified version of Lieberherr *et al.*'s traversal strategies) as an alternative to fixed recursion schemes.

Side-Effects Using **void** methods forces programmers to use local mutation to communicate between different parts of a structure. In practice **void** methods allow visitors to handle multiple/mutually-recursive hierarchies consistently and slightly easier to extend, since a default behavior of "*do nothing*" is always an option. However, using mutation makes imperative visitors difficult to understand, visit-order dependent, difficult to compose, and expensive to parallelize.

⁸The approach is actually more of an instance of the pattern that makes use of Scala's [59] abstract types.

Recent visitor work [61, 60] has focused on providing a functional alternative, but places added constraints on visitor extensions and return types. In particular, mutually-recursive datatypes require multiple, separate visitor definitions, and shared visitor references, which must be initialized via mutation.

In this dissertation we will use a functional approach that eliminates the need for side-effects. As a result, our traversals will be implicitly (and trivially) parallelizable.

1.3.2.3 Higher-Order Functions

Every seasoned functional programmer has witnessed the value of higherorder functions. While iteration functions like map are used extensively for predefined structures like lists, higher-order functions are also very useful with user-defined structures. One of the most common uses of higher-order functions has been to abstract traversals by creating structural recursion operators, typically called *folds* [65, 55].

Returning to our Scheme implementation of BExps, we can use our data definitions as a guide to create a function that folds BExps into a different structure, shown in listing 1.10.

Listing 1.10: Fold function for BExp structures

The comment preceding fold-bexp describes its signature. The function accepts five arguments, one for each structure definition (*i.e.*, *concrete* variants of BExp). We use A as a place-holder for the return type of our function, since it should be the same throughout. The individual functions passed to fold-bexp match the arity of the corresponding value constructors (*e.g.*, make-Neg), but instead of zero-argument functions we use values for True and False.

For each datatype case we replace the original constructor by calling the corresponding function argument with the results of recursively folding the immediate fields of the structure. We elide the case for Or, since it is almost identical to And. Using a **cond** expression to do case dispatch is analogous to the double-dispatch of our visitor's accept/visit methods.

Once we define the necessary helper functions, we can use fold-bexp to give a more succinct definition of eval, without mentioning any structural recursion. Our functions are shown in listing 1.11. For each compound

Listing 1.11: Fold-based eval implementation

constructor (*e.g.*, Not or And) we create a function that will be called on the recursive results to produce a single Lit.

Our implementation of eval has successfully been reduced to a concise, two-line function. Similar to our visitor solution, the traversal of our data structure has now been neatly separated from our operation specific implementation, and we can reuse our fold to write other functions that match this pattern of structural recursion.

1.3.2.4 Limitations and Extensions

As is common with the visitor pattern, the fold functions take many different forms, but in practice implementations suffer from a number of limitations.

Structures and Fixed Recursion How the fold is implemented is important. Deep folds where the traversal recursively walks all nested objects, as we have implemented here in fold-bexp, are more expressive than shallow (or *one-level*) folds [29], but run into the same problems as the visitor implementations since the recursion scheme is fixed.

Generalized folds [55, 65] and other forms of generic programming [12, 38, 9, 34, 54] offer alternatives that eliminate the tedium of writing folds for data structures, but again offer fixed traversals. Abstracting the recursion scheme of folds has lead to several variants of strategic and combinator approaches [45, 47, 44]

One Constructor, One Function Each constructor is handled by exactly one argument to fold-bexp. For large structures the number and order of these parameters contributes to the program's boilerplate. Sheard [65] places functions into nested tuples, and Lämmel [46] collects related func-

tions into a record. These are, however, only partial solutions, since the structure holding the functions must then be constructed and deconstructed.

Having one function per constructor also limits programmers' opportunities to abstract multiple, similar cases into a single function, or to override a more general function with a more specific case.

In the next chapter we discuss our use of function-classes over traversals, which support function extension, case abstraction, and specialization.

Return Types The signature of our fold function, fold-bexp, suggests that the types of the arguments (*e.g.*, the return type of the functions), be consistent, *e.g.*, A. The functions passed as arguments must accept and return values of this type. In a statically typed language like ML [58] or Haskell [39] this forces programmers to write several separate functions. In many cases a single return type for all parts of a structure is not flexible enough. For instance, the function map over lists typically transforms the elements of the list into values of a different type, though the list structure remains intact.

Implementations usually treat functions like map (so-called *homomorphisms* [55]) as a special case, or provide implementations for a small number of situations [48, 45]. In this dissertation, chapter 3 in particular, we show that it is possible to relax this constraint without compromising safety.

CHAPTER 2

DemeterF

The DemeterF system consists of a number of tools and libraries. In this chapter we discuss our class generator, traversal library, and generic programming tools. We begin with an overview of the structural and behavioral aspects of DemeterF-based programs, followed by an example-driven introduction to writing traversal-based functions. We conclude with a discussion of the generic and generative programming features of DemeterF.

2.1 Structures and Classes

Writing traversal-based functions begins with a description of the data structures involved and the relations between different datatypes, *i.e.*, fields or *has-a* relationships, and subtyping or *is-a* relationships. DemeterF allows programmers to separate descriptions of the structural elements of a hierarchy from their methods and behavior by merging definitions into generated Java classes. The separate structures make it convenient to describe traversals and functions, and can substantially reduce the boilerplate code mentioned in the previous chapter (*c.f.*, section 1.3.2).

As input, the DemeterF class generator accepts a *class dictionary* (CD) file [52] and a *behavior* (BEH) file. A CD describes the structures of a class hierarchy and the BEH file provides extra, class-specific definitions and methods to be placed in the body of generated source files. The format of DemeterF CDs includes a number of improvements over Lieberherr's original design. Notably, we support generic definitions with bounded parametric polymorphism, and the inclusion of other CDs.

2.1.1 Class Dictionaries

figure 2.1 describes a simplified version of DemeterF CD syntax using BNF. For the purposes of this dissertation we have left out syntactic features related to datatype generic programming, though relevant points will be discussed in section 2.7. In our BNF notation, concrete syntax is enclosed in double-quotes, *e.g.*, "include". Optional syntax is placed in square brackets,

[], and zero or more repetitions is denoted by a postfix Kleene star. The non-terminal IDENT represents valid Java identifiers and CHAR stands for a (possibly escaped) character literal. A CDFILE begins with a possibly empty

```
CDFILE ::= INCLUDE* TYPEDEF*
INCLUDE ::= "include" STRING ";"
STRING ::= """ CHAR* """
TYPEDEF ::= ["extern"] ( CLASS | INTFC)
SYNTAX ::= STRING | ANNOT
ANNOT ::= "*s" | "*1"
CLASS ::= DECL "=" [ USE ("|" USE)*] (FIELD | SYNTAX)* "."
INTFC ::= "interface" DECL "=" [ USE ("|" USE)*] "."
FIELD ::= "<" IDENT ">" USE
DECL ::= IDENT ["(" IDENT ("," IDENT)* ")"]
USE ::= IDENT ["(" USE ("," USE)* ")"]
```

Figure 2.1: Simplified Class Dictionary (CD) syntax

sequence of INCLUDE statements. The semantics of CD file inclusion is simply concatenation of the TYPEDEF sequences from each file. The body of a CDFILE is sequence of class and/or interface definitions. A CLASS is defined by declaring the class' name and type parameters. The right-hand side of a CLASS definition contains a possibly empty list of subclasses followed by a possibly empty list of FIELD and/or SYNTAX definitions, terminated by a period, ".". An INTFC is prefixed with "interface" and is defined as a possibly empty list of implementing classes. Each TYPEDEF can optionally be declared with the prefix "extern", meaning that the class has already been defined externally, *e.g.*, in another library, and should not be generated.

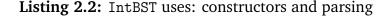
A class with a non-empty list of subclasses is termed *abstract*, and, as in Java, cannot be directly instantiated. A class definition that only contains fields and/or syntax (*i.e.*, no subtypes) is termed *concrete* and can be used to create structures at runtime. Fields can be interspersed with SYNTAX (quoted strings or printing annotations) that guide generated parsers and printers. Strings define the concrete syntax of both the input and output language for a group of class definitions. The literals ***s** and ***1** add spaces and newlines, respectively, to generated print methods that are added to the generated Java files if requested.

Listing 2.1 shows a CD representing integer binary search tree (BST) structures. The hierarchy consists of an abstract class, IntBST, with two concrete subclasses, IntNode and IntLeaf. IntNode represents BST interior tree nodes with an integer field data and left and right subtrees. IntLeaf represents a terminal/empty tree.

Listing 2.1: CD file describing functional integer BSTs

From this structural description DemeterF creates three main Java files, one for each class definition. If requested, the system will also generate a printer and parser, using the syntax inferred from the CD.¹ All generated fields are by default declared **final** and class constructors follow a functional initialization pattern, similar to that enforced by Featherweight Java [37]: each class' constructor accepts a value for each field as arguments and initializes all fields immediately.

Listing 2.2 shows the definition of three instances of IntBST. The first is



an empty IntLeaf tree, which is used to construct a tree with a root node of 2, and left and right children of 1 and 3 respectively. The second and third IntBSTs, t2 and t3, represent the same BST: t2 is created using constructor calls, and t3 using a generated (static) parse method in IntBST. In addition to parse and print methods, DemeterF is also able to generate field getters (e.g., int getData(), functional field updaters (e.g., IntNode updateData(int d)), and a number of other useful methods if requested.

2.1.2 Behavior Files

Behavior (BEH) definitions allow methods and other Java syntax (*e.g.*, comments or **static** fields) to be placed in generated classes while remaining separate from their structural definitions (*i.e.*, the CD). figure 2.2 shows our simple behavior syntax in BNF. Similar to CD files, we allow other BEH files

```
BEHFILE ::= INCLUDE* BEH*
BEH ::= IDENT "{{" TEXT "}}"
```

Figure 2.2: BEH File Syntax

¹Other so-called *datatype-generic* programming functions can also be defined. The specifics will be discussed in section 2.7.

to be included. The terminal TEXT represents any string that does not include double braces, "}}". The TEXT within the double braces is bound to the preceding IDENT. Once different TEXTs with the same bindings has been merged, the code is injected into the body of the CLASS or INTFC definition when files are generated. An example behavior file for our IntBST classes is given in listing 2.3. Each of the BEH definitions defines a method. To-

```
IntBST{{
    abstract IntBST insert(int d);
}}
IntNode{{
    IntBST insert(int d){
        if(d <= data)
            return new IntNode(data, left.insert(d), right);
        return new IntNode(data, left, right.insert(d));
    }
}
IntLeaf{{
    IntBST insert(int d){ return new IntNode(d, this, this); }
}}</pre>
```

Listing 2.3: BEH definitions for integer BST insertion

gether the methods implement the insertion of an **int** into an IntBST. The **abstract** class IntBST declares an **abstract** method, insert, that its subclasses must implement. For IntNode we use data to decide between recursive insertion into the left or right subtree, and return a new IntNode with corresponding subtree updated. For IntLeaf we construct a new IntNode with d as its data, and **this** IntLeaf as its left and right subtrees.²

When Java files are generated for our BST classes, DemeterF combines the CD and BEH definitions into Java files. Listing 2.4 shows the resulting class definition for IntNode. The generated class **extends** IntBST, which is the result of it appearing on the right-hand side of the IntBST definition. IntNode also has **protected final** fields that match its CD definition. The generated constructor accepts and initializes the instance's three fields, and a parse method is added to parse an instance from a String using the language defined by the CD. Our insert method from the BEH definitions is placed verbatim after the generated constructor and methods.

2.1.3 Parametric Polymorphism

Type parametrization is now common place, even in object-oriented communities. While ML and Haskell allow *implicit* parametric polymorphism, Java and C# support explicit parametric polymorphism in both classes

²Note that this version of insert is functional, *i.e.*, mutation free. Side-effecting versions are possible with DemeterF, but the author hopes to discourage the practice of mutable data structures, hence the **final** fields by default.

```
// IntNode.java
public class IntNode extends IntBST{
  protected final int data;
  protected final IntBST left;
  protected final IntBST left;
   /** Construct a(n) IntNode Instance */
  public IntNode(int data, IntBST left, IntBST right){
      this.data = data; this.left = left; this.right = right;
   ľ
   /** Parse an instance of IntNode from the given String */
  public static IntNode parse(String inpt){ /*...*/ }
   /*... Other generated methods ...*/
   IntBST insert(int d){
     if(d <= data)
         return new IntNode(data, left.insert(d), right);
     return new IntNode(data, left, right.insert(d));
  }
}
```

Listing 2.4: Combined CD and BEH in IntNode.java

and methods using so-called *generic* declarations.³ DemeterF allows programmers to define parametrized classes and interfaces that correspond to definitions of generic classes in Java and C#.

CD definitions can be parametrized by placing type parameters in parentheses, separated by commas (DEF and USE in figure 2.1). Explicit bounds on type parameters are supported by generating class definitions that make use of Java's **extends** syntax and C#'s **where** clauses. Our CD notation uses colons to separate a type variable from its bound.

For example, listing 2.5 shows a CD that defines classes for a generic BST implementation. We provide an **extern** definition for Java's parametrized

Listing 2.5: CD definitions for parametrized BSTs.

Comparable interface, which is used as a bound for our type parameter, D, representing the data to be stored in the tree. The type of data stored, D, must implement Comparable(D), so that nodes in the tree can be ordered to maintain a typical BST invariant.

 $^{^3} Java$ and C# do support a limited form of inference that can recover type variable annotations.

Listing 2.6 shows behavior definitions that implement an insert method for our generic BSTs. The insert methods are similar to what we imple-

```
BST{{
    abstract BST<D> insert(D d);
}}
Node{{
    BST<D> insert(D d){
        if(d.compareTo(data) <= 0)
            return new Node<D>(data, left.insert(d), right);
        return new Node<D>(data, left, right.insert(d));
    }
}}
Leaf{{
    BST<D> insert(D d){
        return new Node<D>(d, this, this);
    }
}
```

Listing 2.6: BEH definitions for generic BST insertion

mented for IntBSTs, though each now works on data of the type parameter D and returns a result of type BST<D>. Our generic BST class can be instantiated in another (or the same) CD to support parsing and printing, as shown in listing 2.7(a), with Java code using the generated classes shown in listing 2.7(b). We create two wrapper classes: one that instantiates BST to store

DoubleBST = <bst> BST(Double). CharBST = <bst> BST(Character). (a) CD use of generic BST // BST of Doubles... BST<Double> dbst = DoubleBST.parse("(1.2 (1.1 * *) (1.3 * *))") .bst.insert(1.4); // BST of Characters... BST<Character> cbst = CharBST.parse("('B' ('A' * *) ('C' * *))") .bst.insert('D');

(b) Use within Java code

Listing 2.7: Generic BST instantiation and uses

Double values, and the other which stores Characters.⁴ Our parametrization is valid, since Double and Character both **implement** Comparable for their respective types, matching our type parameter bounds. Once the wrapper/instantiation has been *parsed* we can access its field and insert a new element. In both cases the new element is placed to the right of the root's right subtree. Note that the wrapper classes are only necessary to support

⁴Java allows only *reference* types to be used as type parameters, so we use the *boxed* equivalents. In C# this is not necessary, since the language allows *value* types as parameters.

parsing and printing, since they alert DemeterF that a particular instantiation of the classes is required. Generated parametrized classes are otherwise the same as their Java equivalents.

2.1.4 Running Example

For the rest of this chapter, we return to the example data structures defined in chapter 1 (listing 1.1). Listing 2.8 shows a CD that defines the same classes using a DemeterF CD.

```
BExp = Lit | Neg | And | Or.
Lit = True | False.
True = "True".
False = "False".
Neg = "!" <inner> BExp.
And = "(&&" *s <left> BExp *s <right> BExp ")".
Or = "(||" *s <left> BExp *s <right> BExp ")".
```

Listing 2.8: CD definitions for Boolean expressions

The first line corresponds to our **abstract** class BExp, with four subclasses: Lit, Neg, And, and Or. Lit is also **abstract**, with concrete subclasses of True and False. True and False are defined only as syntax.

Other definitions are concrete classes with *recursive* fields. Neg has a single inner expression, while And and Or are binary expressions, each with two recursive fields. For completeness we give And and Or prefix operators as concrete syntax, since infix operators would make the resulting grammar non-LL(k).⁵

For the rest of this chapter we use these definitions to demonstrate the various features of writing traversal-based functions using DemeterF. When necessary we will extend our structures to illuminate different aspects of our system.

2.2 Functions and Traversals

CDs are useful for describing the structure and syntax of data, but what we eventually want to do is write functions over instances of our structures that return meaningful results. In order to write traversal-based functions, DemeterF provides classes that represent *function-classes* and traversals, that together are used to implement functions over a data structure.

⁵DemeterF currently uses JavaCC [3] to generate parsers, but does not generate any complex look-ahead decisions.

2.2.1 Function-Classes

A DemeterF function-class represents a *set* of functions using Java methods with the special name *combine*. DemeterF provides a base function-class, FC, that represents the empty set of functions. To create a new function-class, programmers can extend FC by adding specific *combine* methods for a given data structure. The *combine* methods of a function-class instance (or *function-object*) are interpreted as *fold* functions over an adaptive, generic traversal.

As a first example, listing 2.9 defines a simple function-class with the intent of converting a BExp into a String with the help of a traversal. Our

```
// Convert a BExp to a String...
class ToString extends FC{
   String combine(True t){ return "True"; }
   String combine(False f){ return "False"; }
   String combine(Neg n, String i){ return "!"+i; }
   String combine(And a, String l, String r)
   { return "(&& "+1+" "+r+")"; }
   String combine(Or o, String l, String r)
   { return "(|| "+1+" "+r+")"; }
}
```

Listing 2.9: ToString function-class

class, appropriately named ToString, **extends** the base function-class FC. It adds a *combine* method for each concrete case of our BExp data structures. In this case the *combine* methods can be identified by the type of their first argument. In each of the methods we return a String that corresponds to the concrete syntax from our original CD (listing 2.8).

2.2.2 DemeterF Traversals

In order to turn an instance of a function-class (*i.e.*, a function-object) into a function, we apply its *combine* methods over the traversal of a data structure. To do this, DemeterF provides a class, Traversal, that takes an instance of a function-class. A typical Traversal usage is shown in listing 2.10. The method toString is added to the ToString class. The method ac-

```
// Added to ToString
String toString(BExp e){
   return new Traversal(this).traverse(e);
}
```

Listing 2.10: Traversal invocation for ToString

cepts a BExp instance and traverses it in order to convert it into a String.

A new Traversal is constructed by passing **this** function-object, and the BExp is traversed. The use of **this** references the current instance of ToString (*i.e.*, the function-object), whose *combine* methods are called by the Traversal to fold together the BExp instance.

When called, the *traverse* method proceeds with a depth-first walk of the given object, in this case a BExp. After recursively traversing the fields of the current node, the Traversal selects a *combine* method from the given function-object that best matches: (1) the type of the current node, and (2) the result types of recursively traversing each of the node's fields. This is termed *multiple dispatch*, since all argument types determine the selected method. Once selected, the *combine* is then applied to the original node (as its first argument) and the traversal results of its fields.

Getting back to ToString, instances of True or False have no fields, so selecting a *combine* method is simple. The traversal selects the first or second method in ToString based on the type of the object itself. When applied to a Neg instance, *traverse* first recursively processes the object's inner field. If the result of the traversal is a String, then the third method is selected and applied. Similarly for And and Or, with both fields (left and right) being traversed before a matching method is selected. Any case for which the function-object does not have a matching *combine* method, *e.g.*, a current object of type Neg with a recursive result of type **int**, results in a runtime/dispatch exception.

As with our visitor solutions (section 1.3.2.1), our function-class and traversal can be used by creating a new function-object and calling our toString with a BExp:

```
new ToString().toString(a_bexp)
```

If the function was needed more than once, we could name a reference to the ToString instance for use with multiple calls. This style of definition could be considered *object-oriented*, since the toString method is only associated with an instance of ToString. A more global/functional implementation is also possible by making toString a **static** method that constructs a Traversal with a **new** ToString instance.

2.2.3 Case Abstraction and Specialization

As a second example of a traversal-based function we implement *strict* BExp evaluation, similar to our fold-based Scheme example (listing 1.11 in section 1.3.2.3). Listing 2.11 shows a complete function-class that implements a slightly inefficient version of BExp evaluation. Our function-class, Strict-Eval, has a number of interesting *combine* methods, each of which matches a specific case of evaluation.

The first method matches both True and False instances with their supertype, Lit, returning the literal unchanged. For Neg we match possible cases with separate *combine* methods, returning the negation of the recur-

```
// Evaluate a BExp
class StrictEval extends FC{
  Lit combine(Lit 1){ return 1; }
  Lit combine(Neg n, True t){ return new False(); }
  Lit combine(Neg n, False f){ return new True(); }
  Lit combine(And a, True 1, True r){ return 1; }
  Lit combine(Or a, False 1, False r){ return 1; }
  Lit combine(And a, Lit 1, Lit r){ return new False(); }
  Lit combine(Or a, Lit 1, Lit r){ return new True(); }
  Lit eval(BExp e)
  { return new Traversal(this).traverse(e); }
}
```

Listing 2.11: DemeterF-based strict Boolean expression evaluation

sive inner traversal result. The first two *combine* methods for And and Or match the important situations where the recursive results are both True or both False, in which case the left result, 1, can be returned. The final two cases match default cases for And and Or, where we can return False and True respectively. Again we implement a wrapper method, eval, that constructs a Traversal with **this** function-object and calls *traverse* on the given BExp.

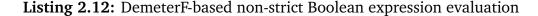
The StrictEval example demonstrates two novel features of using multiple dispatch over data structure traversal. The first is abstraction: our *combine* selection allows us to *abstract* multiple common cases into a single method. This occurs with the *combine* for Lit where we avoid mentioning separate cases for True and False, and the second/default methods for And and Or, which each handle 3 cases. The dual of abstraction is specialization: we can write a method signature that overrides a more general case with a specific result. This occurs in the first two *combine* methods for And and Or, where the specialized signature, *e.g.*, (And True True), overrides the abstracted case. In either case the traversal's multiple dispatch selects the *combine* method with the most appropriate signature. These two features help to support extensible function-classes, making the function-objects over traversals more useful.

2.3 Traversal Control

The separation of functions into function-classes and Traversal allows us to easily augment the traversal with additional features. Continuing with our BExp evaluation example, we originally used visitors (listing 1.9), higherorder functions (listing 1.11), and DemeterF traversal (listing 2.11) to implement evaluation. Although these forms of traversal eliminate the boilerplate of traversal, they were not capable of *short-cutting* the traversal. In order to implement the well-known notion of non-strict Boolean evaluation we will use DemeterF traversal control with our function-class.

DemeterF supports a version of traversal control that is a simplification of that found in Adaptive Programming *strategies* [52, 53]. The Traversal class provides a second constructor that takes a two arguments, the first is a function-object and the second is of type Control. The DemeterF class Control has creator methods that allow a programmer to describe specific fields to be *bypassed* (or skipped over) during traversal, effectively guiding the Traversal through a data structure. To make the evaluation of And and Or non-strict, we specify that their right field should be *bypass* ed.

Listing 2.12 shows a function-class that correctly implements short-cutting BExp evaluation. Our function class, Eval, is quite similar to our previous



example, StrictEval (listing 2.11). For Lit and Neg instances, the method selection is the same as StrictEval.⁶

Before describing the rest of the function set, it is important to take a closer look at the eval method. We construct our Traversal by passing **this** function-object and a Control object created using *bypass*. The string given to *bypass* represents the fields to be skipped, in this case And.right and Or.right.⁷ During the execution of traverse, when the current node is an instance of And or Or our Control tells the traversal to *skip* its right field. After the traversal of the left field is complete, a method is selected based on the type of the current node (*i.e.*, And or Or), the result type of the recursive traversal of the left field, and the type of the unchanged right field.

⁶In fact, we could have just extended StrictEval, but we save the discussion of function-class extension for section 2.5.

⁷If Java had macros we could better integrate *Control/bypass* into the language. Our implementation using Scheme provides a much more user-friendly integration [18] without exposing implementation details.

Our plan to bypass the right field is reflected in the type of the third argument of our last four *combine* methods. We use the type BExp (instead of True or False), which matches the field's original type. In the first two cases we can immediately return the result of the left traversal, True or False respectively. In the final two cases we make a recursive call to evaluate the right side of the expression. Since the right side of the expression is only traversed when necessary, we achieve our short-cutting/non-strict evaluation strategy.

2.3.1 Efficient Recursion

When a field is *bypass* ed during traversal, as with Eval in listing 2.12, it is common to hand-code a recursive call after checking some condition. In those cases it is inefficient to reconstruct an identical traversal, *e.g.*, in our eval method, for each recursive call. We can instead create and store the Traversal instance in a local variable when the function object is initialized. This initialization effectively "*ties*" the recursive "*knot*", so the same traversal can be referenced for multiple recursive calls. Listing 2.13 shows this caching strategy implemented for our Eval function-class.

Listing 2.13: Cached Traversal for efficient recursion

Depending on the size of the BExp instance that is traversed and the number of recursive calls required, this caching can save a significant amount of space, time, and more importantly, object allocations.⁸

2.4 Traversal Contexts

There are times when writing purely compositional functions will not suffice. In cases where information about the ancestors of a sub-structure is important to a method's result, programmers typically add an argument to the method definition. This argument is then passed to recursive invocations and updated when appropriate. DemeterF supports this style of traversalbased function using a notion of *traversal contexts*.

⁸Parallel execution seems to be more dependent on allocations due to Java's shared heap and garbage collection.

2.4.1 Update Methods

In addition to *combine* methods, a function-class can define *update* methods. While *combine* methods are akin to fold functions (*i.e.*, bottom-up), *update* methods are responsible for updating the traversal context at interesting points,⁹ top-down, similar to inherited attributes in Attribute Grammars [42]. The context is available to each *combine* method as its last argument. Methods can, however, ignore the context (or other later arguments) simply by declaring a shorter signature.

Methods that *update* the traversal context can accept up to three arguments that represent (1) the current node of the structure, (2) the next field to be traversed, and (3) the current node's context. The field to be traversed is encoded as an instance of a *field-class*. For each field of a CD definition, *e.g.*, left from the class And, DemeterF generates a **static** inner class whose instances represent the pending traversal of the field. Each field-type is defined as a subtype of the DemeterF class Fields.any (another inner class). Our representation has the added benefit of making field-classes in *update* methods look like field accesses, *e.g.*, And.left is the field-class of the left field of And instances.

To demonstrate traversal contexts with another BExp example, we extend our BExp structures with variable expressions and implement a traversalbased function that transforms a BExp into *negation normal* form, where the negation instances (Neg) are pushed down to the literals and variables of a Boolean expression. The modified CD definitions are shown in listing 2.14 along with classes to represent the Sign of nested negations. For brevity

// Add Var to the BExp definition
BExp = Lit | Neg | And | Or | Var.
Var = <id> ident.
// Sign of nested negations
Sign = Even | Odd.
Even = .
Odd = .

Listing 2.14: Adding Var and Sign contexts

we elide our unchanged structures. The class Var is added as a subtype of BExp. The new concrete class contains an ident, a DemeterF library class that represents identifiers.

Our strategy for implementing negation normalization is to keep track of the number of nested outer Neg expressions during the traversal as our context. We represent the nesting depth by the abstract class Sign, which is either positive, Even, or negative, Odd. Before traversal proceeds into the inner field of a Neg instance we use an *update* method to flip the Sign of the

⁹By "update" we mean *functional update*, where mutation is avoided by constructing a new, updated instance.

context for the inner subtraversal. When variables or literals are reached we return an adjusted instance based on the Sign of the context. For And and Or we follow the usual rules for And and Or under negation when the context is Odd.

Listing 2.15 shows the complete implementation of negation normalization as a function-class. The class is best explained case by case. The *update*

```
class NegNormal extends FC{
   // Flip the Sign when entering a Neg
   Sign update(Neg n, Neg.inner f, Even s){ return new Odd(); }
   Sign update(Neg n, Neg.inner f, Odd s){ return new Even(); }
   // Literals and Vars
   BExp combine(Lit 1, Even s){ return 1; }
   BExp combine(True f, Odd s){ return new False(); }
   BExp combine(False f, Odd s){ return new True();
                                                        }
   BExp combine(Var v, ident id, Even s){ return v; }
   BExp combine(Var v, ident id, Odd s){ return new Neg(v); }
   BExp combine(Neg n, BExp e){ return e; }
   // Follow De Morgan Laws...
   BExp combine(And a, BExp 1, BExp r, Even s){ return new And(l,r); }
   BExp combine(And a, BExp 1, BExp r, Odd s){ return new Or(1,r); }
BExp combine(Or o, BExp 1, BExp r, Even s){ return new Or(1,r); }
   BExp combine(Or o, BExp 1, BExp r, Odd s){ return new And(1,r); }
   // Main Entry...
   BExp normalize(BExp e)
   { return new Traversal(this).traverse(e, new Even()); }
}
```

Listing 2.15: BExp negation normalization

methods will be called when the current node is an instance of Neg, before traversing into its inner field. This is encoded by the first argument, Neg, and the second argument type of Neg.inner. For each of the context types we return the opposite Sign: Even for Odd and vice versa. For other cases the traversal automatically propagates the context unchanged.

As for the *combine* methods, the first matches after traversing a Lit instance within an Even context and returns the original literal. The next two cases match True and False instances within an Odd context, returning their negation. After normalization, only variables are negated, so the *combine* for Neg accepts just two arguments, ignoring its context, and returns the recursively normalized inner BExp.

The cases for Var return the original variable within an Even context, and its negation within an Odd context.¹⁰ The final four *combine* methods rebuild or convert And and Or instances under Even or Odd contexts respectively. The cases follow De Morgan conversion rules for conjunction/disjunc-

¹⁰Note that we reference the original Var rather than building a **new** one, though in most cases the two will be indistinguishable.

tion, e.g., $\neg(a \land b) \equiv (\neg a \lor \neg b)$, with the traversal having already propagated negations and recursively normalized the left and right fields.

The normalize method completes our implementation by creating a new Traversal and calling *traverse*. We pass two arguments to traverse: the given BExp and a root context. Since we begin with no outer Neg, our initial context is Even.

2.5 Extensible Functions

The separation of function-classes and traversal allows us to independently extend/override *combine* and *update* methods. DemeterF supports such extension using Java inheritance. As with traditional inheritance, duplicate signatures will be overridden, and other methods will be overloaded, with preferences determined from the methods' argument types by multiple dispatch.

A typical use of traversals where function-class extension is convenient is when performing *functional updates* over a particular structure, similar to map over lists.¹¹ listing 2.16 shows a class named Copy, which is used as a foundation for such a transformation over BExps. Each *combine* method

```
class Copy extends FC{
  Lit combine(Lit 1){ return 1; }
  Neg combine(Neg e, BExp in){ return new Neg(in); }
  And combine(And e, BExp 1, BExp r){ return new And(1,r); }
  Or combine(Or e, BExp 1, BExp r){ return new Or(1,r); }
  Var combine(Var e, ident id){ return new Var(id); }
}
```

Listing 2.16: Copy: functional updates for BExps

rebuilds our BExp structures during traversal by calling the individual constructors on recursive results.

As an example, we can extend Copy with specialized *combine* methods that will simplify constant (non-variable) expressions to True or False literals. Listing 2.17 shows our extended function-class, Simplify, that implements such a transformation. Our functions override Copy with specific cases where the current BExp can be simplified based on recursive results. A Neg instance can be simplified when its recursive inner result is a Lit by returning its negation, or when its recursive result is a Neg by returning the inner simplified BExp. Instances of And and Or have a number of cases that can be simplified when at least one of the recursive results is a Lit. The first case for each uses a shorter signature, ignoring the recursive result from its right field, since it is not needed. In other cases, the original And or Or can be replaced by the simplified results from its left or right field.

¹¹It is not exactly the same, since list map is shallow and our traversals are deep.

```
class Simplify extends Copy{
  Lit combine(Neg n, True t){ return new False(); }
  Lit combine(Neg n, False f){ return new True(); }
  BExp combine(Neg n, Neg e){ return e.inner; }
  Lit combine(And a, False 1){ return 1; }
  Lit combine(And a, BExp 1, False r){ return r; }
  BExp combine(And a, True 1, BExp r){ return r; }
  BExp combine(And a, BExp 1, True r){ return 1; }
  Lit combine(Or o, True 1){ return 1; }
  Lit combine(Or o, BExp 1, True r){ return r; }
  BExp combine(Or o, False 1, BExp r){ return r; }
  BExp combine(Or o, BExp 1, False r){ return r; }
  BExp combine(Or o, BExp 1, False r){ return r; }
  BExp combine(Or o, BExp 1, False r){ return r; }
  BExp simplify(BExp e)
  { return new Traversal(this).traverse(e); }
}
```

Listing 2.17: BExp simplification, using Copy

In cases where the specific *combine* methods from Simplify do not match, the methods from Copy are used to rebuild the structure. The Traversal gives us the added benefit of implicit recursion, so our transformation applies to the entire data structure. This kind of transformation is so common that DemeterF provides a function-class, named TP for *typepreserving* [45, 48], that generically implements Copy for all structures. We will discuss TP and other generic function-classes in section 2.7.

2.6 Mutual Recursion

Previously, our example data structures have only been *self recursive*, where recursive occurrences within concrete subclasses of BExp are all of type BExp. Mutually-recursive types can make processing instances more complicated, particularly when visitors [61] or folds [65] are used to implement operations. DemeterF traversals, however, handle mutual recursion just like self recursion. Since the Traversal selects the most specific matching *combine* method from the given function-object, the grouping of methods or types to which they apply is handled by our multiple dispatch.

As an example, we can extend our BExp structures to include a class that represents variable binding. Listing 2.18 shows our new structures. We add a new BExp subclass, Let, that contains a Bind and a body BExp. A binding is represented with an ident and a BExp. The types BExp and Bind are considered mutually recursive since a Let is a BExp and has a Bind, which in turn has a BExp.

We can reuse our previous example, Simplify, to handle our new structures by adding Let and Bind cases to our Copy function-class, and extending // Add Let to BExp definition
BExp = Lit | Neg | And | Or | Var | Let.
// Variable bindings
Let = "let" *s <bind> Bind *s
 "in" *s <body> BExp.
Bind = <id> ident *s "=" *s <e> BExp.

Listing 2.18: Mutually-recursive structures

Simplify.¹² Listing 2.19 shows the function-class extensions.

```
// Extend copy for Let and Bind
class Copy extends FC{
    /* ... Others from listing 2.16... */
    Let combine(Let 1, Bind b, BExp e){ return new Let(b,e); }
    Bind combine(Bind b, ident id, BExp e){ return new Bind(id,e); }
}
// Extend Simplify for Let
class SimplifyWLet extends Simplify{
    BExp combine(Let 1, Bind b, Lit e){ return e; }
}
```

Listing 2.19: Copy additions and Simplify extension for Let

Our new function-class, SimplifyWLet, adds a *combine* method for the new structure that simplifies a Let when its body can be simplified to a Lit, since the binding is unnecessary given our pure interpretation of BExps. Because each case is handled separately, the presence of mutual recursion does not affect our traversal: *combine* methods are still applied as usual. Our previous simplify method does not need to be redefined, it works as expected when called on an instance of our new class:

new SimplifyWLet().simplify(a_bexp_wlet)

And, of course, the function-class still operates on instances without our new Let and Bind structures.

2.7 Generic Programming

We have shown several examples of traversal-based functions over data structures. While we developed them for our particular BExp data structures, many of them are written with a degree of genericity. Because the traversal adapts the *combine* methods to a data structure, the function-class itself can, in many cases, avoid mentioning certain parts of the data structures. For instance, the ToString function-class from listing 2.9 relies on

¹²Multiple inheritance would be very useful in this case to extend both Copy and Simplify simultaneously.

three pieces of information: the names of the concrete classes mentioned, the *number* of parameters/fields, and the return types of their respective subtraversals. In this section we take a closer look at the generic aspects of traversal-based programming with DemeterF.

2.7.1 Generic Function-Classes

The spectrum of generic functions can (usually) be divided into two different kinds: type-unifying and type-preserving [45, 48].

2.7.1.1 Type-Unifying Functions

Type-unifying (TU) functions are those that sum a specific property over a data-structure. This category includes counting or collecting instances of a certain type within a larger data structure, or calculating the size of a structure. DemeterF supports the writing of generic TU functions with a parametrized function-class, TU<X>, that sums a property of type X over a structure. The function declares two abstract methods that the client must implement: a default *combine* method that takes no arguments, and a fold method that folds together two results of type X.

For example, listing 2.20 shows a function-class, UsedVars that collects the used variable names within a BExp instance. Our function-class **extends**

```
class UsedVars extends TU<Set<ident>>{
   Set<ident> combine()
   { return Set.<ident>create(); }
   Set<ident> fold(Set<ident> a, Set<ident> b)
   { return a.union(b); }
   Set<ident> combine(Var v){ return Set.create(v.id); }
}
```

Listing 2.20: Collect used variables in a BExp using TU

TU<Set<ident>>, in order to collect the Set of names, idents, of used variables within a BExp.¹³ We provide an implementation of a default *combine* method that returns the empty Set, and a fold method that returns the union of two Sets. The final *combine* method creates a singleton set from the id within a Var instance, *i.e.*, a *used* variable.

When an instance of UsedVars used over a traversal, the default *combine* is called whenever a leaf of the structure is reached. When a compound object is traversed, its recursive results are folded together (if necessary) into a single result by the methods inherited from TU. In the actual implementation of DemeterF we extend TU in order to collect the type definitions from the tree of included CD files.

¹³We use a functional implementation of Set from the DemeterF library, so all methods return a new Set, rather than using mutation.

2.7.1.2 Type-Preserving Functions

Type-preserving functions include transformations or functional updates to a particular part of a structure. This category includes functions like substitution or variable index calculations. DemeterF provides a class, TP, that rebuilds the data structure it traverses. Each *combine* method simply calls the corresponding constructor of its first argument. Clients implement specific *combine* methods for the part of the structure to be transformed and the rest of the methods automatically reconstruct.

Listing 2.21 shows an example function-class, Invert, that inverts True and False literals within a BExp instance. When a literal, True or False,

```
class Invert extends TP{
  False combine(True 1){ return new False(); }
  True combine(False 1){ return new True(); }
}
```

Listing 2.21: Invert True/False instances using TP

is reached, one of our *combine* methods will be called. Otherwise, the inherited methods of TP rebuild compound BExps (or Binds if we have them) using the results of recursive subtraversals to create a new instance. In the implementation of DemeterF we extend TP to implement type parameter substitution and to push global CD properties into local type definitions.

2.7.2 Generating Function-Classes

Many of our earlier functions are specific to our BExp datatypes (*e.g.*, To-String), but more general function-classes use implementations of TU and TP to generically adapt to a data structure. DemeterF allows programmers to write functions over the *structure* of CDs that generate function-classes to be used with a traversal.¹⁴ Though our implementation is complicated by parametrized types, we essentially traverse the abstract syntax tree of a CD to produce a function-class with specialized *combine* methods. In this section we give abstract specifications of our generation (*i.e.*, *compilation*) of generic function-classes from CD definitions by way of simple *rewrite* rules.

2.7.2.1 Abstract CDs

At runtime our structures are only made up of concrete classes, so generated function-classes depend only on the structure of concrete classes. Before generating function-classes, DemeterF transforms more complex CDs into a

¹⁴It is possible to write external function-classes to be loaded at runtime, but the author of this dissertation has provided a number of useful classes that are easy to use. So client extensions are rarely necessary.

simpler representation by pushing common fields from abstract classes down into concrete subtypes. For the purpose of generating function-classes it is usually enough to view a CD as a list of concrete class definitions of the form:

$$C = \langle f_1 \rangle \ T_1 \cdots \langle f_n \rangle \ T_n$$

Where each type, T_i , can be either abstract or concrete. The field names, f_i , are actually not important, but we use them to keep the names of method parameters consistent. Since fields of abstract definitions are taken into account by concrete subclasses, we view abstract classes simply as a list of bar separated subtypes:

$$A = T_1 \mid \dots \mid T_n$$

In this section we use these simplified definitions to describe rewrite rules for generating function-classes from the definitions of a particular CD.

2.7.2.2 Printing: Show

Printing in various forms has typically been a generated function in Adaptive Programming tools, *e.g.*, DemeterJ [67]. In DemeterF we define the generation of a CD-based function-class as a function from concrete definitions to *combine* methods. As an example of a print related function-class, we demonstrate the generation of Show, a common derivable type class in Haskell [35]. We will use templates to describe the format of our resulting function-classes.

The template for Show is given in listing 2.22. The template simply pro-

```
class Show extends FC{

// Convert primitives

string combine(int p){ return ""+p; }

/*... Other primitive types ... */

// Generate the rest with GenShow

\forall C \in CD.GENSHOW(C)

}
```

Listing 2.22: Show generation template

vides a class definition and *combine* methods for primitives that convert each into a String. The rest of the body of Show is generated by GENSHOW, using a simple rewrite rule mapped to each concrete definition from the CD:

```
\begin{aligned} & \operatorname{GENSHOW}(C = \langle f_1 \rangle \ T_1 \ \cdots \ \langle f_n \rangle \ T_n) \ \rightsquigarrow \\ & \operatorname{String} \ \operatorname{combine}(C \ \_h, \ \operatorname{String} \ f_1, \ \cdots, \ \operatorname{String} \ f_n) \\ & \left\{ \begin{array}{c} \operatorname{return} \ "C("+f_1+", "+\cdots+", "+f_n+")"; \end{array} \right\} \end{aligned}
```

For each concrete definition with n fields we create a *combine* method with n + 1 arguments. The first is of type C, the defined type, and the rest are of type String. During the traversal of an object using an instance of Show, the field traversals will recursively convert the fields into strings before calling the matching *combine*. Within each method, the return String is constructed by concatenating the separating the recursive field results wit commas, wrapping them in parentheses, and prefixing the String with the class name, C.

Listing 2.23 gives a portion of the generated Show function-class for our BExp CD.

```
class Show extends FC{
   /* ... */
   String combine(Neg _h, String inner)
   { return "Neg("+inner+")"; }
   String combine(And _h, String l, String r)
   { return "And("+1+","+r+")"; }
   /* ... */
}
```

Listing 2.23: Show generated for BExps

2.7.2.3 Type Unifying Functions

While the generic (reflective) TU class works for all structure, we can use the concrete class definitions in a CD to generate the equivalent function-class that does not require the use of reflection. We provide a template that is parametrized by the eventual return type, X, shown in listing 2.24. We de-

```
class TU<X> : FC{

// Methods to override

abstract X fold(X a, X b);

abstract X combine();

// Primitives call default

X combine(int p){ return combine(); }

/*... Other primitive types ...*/

// Generate the body with GenTU

\forall C \in CD.GENTU(C)}
```

Listing 2.24: TU generation template

clare the abstract methods for producing the default result (*combine()*) and folding together two recursive results, respectively. Primitive *combine* methods can be overridden, but initially return the default result. Our generation rule for concrete definitions is a generalization of that for Show:

 $\begin{aligned} & \operatorname{GENTU}(C = \langle f_1 \rangle \ T_1 \ \cdots \ \langle f_n \rangle \ T_n) \ \rightsquigarrow \\ & \operatorname{X} \ \textit{combine} \left(C \ _h, \ X \ f_1, \ \cdots, \ X \ f_n \right) \\ & \left\{ \ \operatorname{\textbf{return}} \ \operatorname{fold}(f_1, \ \operatorname{fold}(f_2, \ \cdots)); \ \right\} \end{aligned}$

Each generated *combine* method accepts n + 1 parameters: again the first of type C, but the rest are of our type parameter X. If necessary, the return result is computed by nested calls to fold. Listing 2.25 shows the resulting TU class, specialized for our Exp CD. The generated version of TU is a direct

```
class TU<X> extends FC{
   /* ... */
   X combine(Neg _h, X inner){ return inner; }
   X combine(And _h, X l, X r){ return fold(l,r); }
   /* ... */
}
```

Listing 2.25: TU generated for BExps

replacement for the generic/reflective version used in listing 2.20. The generated function-class gives us much better performance, especially when we can inline traversals [19].

2.7.2.4 Type Preserving Functions

Our last function-class generation example is probably the most useful. We use it often to do recursive functional updates and transformations over different types. Since *combine* methods are optional for primitive types we leave them out of our template, shown in listing 2.24. Our generation rule

```
class TP extends FC{ // Generate the body with GenTP \forall C \in CD. \operatorname{GENTP}(C) }
```

Listing 2.26: TP generation template

creates a *combine* method that simply reconstructs a new C instance from the recursive traversals results.

$$\begin{aligned} \operatorname{GENTP}(C &= \langle f_1 \rangle \ T_1 \ \cdots \ \langle f_n \rangle \ T_n \) &\rightsquigarrow \\ C \ \operatorname{combine}(C \ \bot, \ T_1 \ f_1, \ \cdots, \ T_n \ f_n) \\ \{ \ \operatorname{return new} \ C(f_1, \ \cdots, \ f_n); \ \} \end{aligned}$$

Because the transformation is type preserving, each field result type is the same as its defined type, T_i . The resulting generated TP class for our Exp CD is shown in figure 2.27.

```
class TP extends FC{
   /* ... */
   Neg combine(Neg _h, BExp inner)
   { return new Neg(inner); }
   And combine(Add _h, BExp 1, BExp r)
   { return new And(1, r); }
   /* ... */
}
```

Listing 2.27: TP generated for BExps

2.8 Errors and Assumptions

Having seen several examples of our DemeterF library and implemented operations, it is worth going over the assumptions that DemeterF makes and the different errors that can occur when using and writing traversal-based functions. As with any Java-based library, programmers can raise a traditional RuntimeException during the execution of a traversal and within *combine* methods. DemeterF does not attempt to interact with Java's exception mechanism, so programmer raised errors behave as expected.

DemeterF assumes a bit more about the structures that will be traversed. While class definitions generated from a CD do not (by default) support mutation, Java will still allow local mutation and mutation of handwritten classes, which allows programmers to construct cyclic instances. DemeterF assumes that traversed structures are acyclic, but traversal-based functions can be written for cyclic structures by using Control to avoid infinite recursion.¹⁵

All the function-classes presented thus far have been *type-correct* and *complete* with respect to the structures being traversed. In each case the *combine* method signatures have handled all possible cases, including recursive results. However, when this is not the case DemeterF raises a Runtime-Exception during method selection, when a suitably typed *combine* method cannot be found.

A simple example of an incomplete function-class is shown in listing 2.28. Within TypeError we have a *combine* method that handles the Lit case, but not one that handles And. Calling the error method of a TypeError:

```
new TypeError().error()
```

results in a DemeterF runtime error:

```
DemeterF: Did not find a match for:
    TypeError.combine(And, String, String)
```

Stating that a matching *combine* method for the signature (And, String, String) could not be found in the given function-object. In this case the

¹⁵The traversal of shared structures behaves as expected, though a shared instance may be traversed multiple times.

```
class TypeError extends FC{
   String combine(Lit 1){ return "Lit"; }
   String error(){
      BExp e = new And(new True(), new False());
      return new Traversal(this).traverse(e);
   }
}
```

Listing 2.28: Function-class that causes a dispatch error

problem is easy to fix by adding a new case for And, but what we want is to be certain that a Traversal will *never* raise such an error for a combination of data structure and function-class. Modeling DemeterF traversals in order to statically eliminate such dispatch errors (*i.e.*, ensuring *safety*) is the main topic of the next chapter.

Chapter 3

A Model of DemeterF

Now that we have discussed the features of our DemeterF implementation, in this chapter we formally describe the syntax and semantics of a simplified model, which we refer to as AP-F. AP-F captures the key aspects of DemeterF's CD definitions, adaptive generic traversal, and type-based multiple dispatch. We use the model to give our traversals and dispatch a precise semantics. With the given semantics we then define a type system, which guarantees that well-typed traversals are free from dispatch errors. We provide a proof of type soundness, then complete the chapter with a discussion of extensions to the model that would bring it in line with the implementation of DemeterF.

3.1 Syntax

We begin by giving a description of our minimal syntax, which embodies the key aspects of DemeterF CDs, traversals, and function-classes. Our model syntax is shown in figure 3.1. Aside from general Java features like classes and local definitions, our most notable omissions are base types and field names. Our syntactic categories are partitioned into variable names x concrete type names C and abstract type names A. An AP-F program P is a sequence of data structure definitions (abstract and concrete types) followed by an expression. Abstract and concrete types correspond to abstract (*i.e.*, no fields) and concrete classes in a DemeterF CD. Concrete type definitions mention only the types of their "fields", since functions will be used to rename structural elements during traversal.

Expressions e are either variable references, constructor calls (new), or traversals. We model the simplest form of DemeterF traversal, representing the traversal of a structure instance using a given functions-class. Function sets F and functions f represent DemeterF function-classes and *combine* methods respectively. A function set, funcset, is a sequence of functions, each of which is a sequence of type/argument pairs followed by a return and body expression in Java-like syntax. Function return types are left out, since they can be inferred from the argument types and body expression.

Figure 3.1: AP-F Model Language Syntax

3.1.1 Subtyping

Based on the definitions in a program, we define a subtype relation \leq as the reflexive, transitive closure of the immediate subtype relationship from abstract definitions. Our definition is given by three rules, shown in figure 3.2.

 $\begin{array}{c|c} [\text{S-ReFL}] & [\text{S-DeF}] \\ \hline \hline T \leq T \end{array} & \begin{array}{c} \text{abstract } A = T_0 \mid \ldots \mid T_n \in P \\ \hline \hline T_i \leq A \end{array} \\ \\ [\text{S-TRANS}] \\ \hline \hline T \leq T' & T'' \leq T' \\ \hline \hline T \leq T' \end{array}$

Figure 3.2: Subtyping Rules

The subtype relation will be used primarily to define our multiple-dispatch, but we will also use it in our type system to relate the type of a data structure to the types of possible return values, when an instance is traversed with a funcset.

3.1.2 Example

Our model does not include base types, but our basic Boolean expression structures (from chapters 1 and 2) can still be defined. The BExp CD-like definitions are shown in listing 3.1. To complete the program definition we construct a simple BExp in the body of the program representing (*true* $\land \neg false$).

Listing 3.1: Model Example: Boolean expression structures

3.2 Well-Formedness Rules

In order to avoid purely syntactic problems in our semantics, we restrict syntactically valid programs with a few *well-formedness* rules. They check the sanity of a program's definitions and allow us to focus on the key issues of our semantics.

TYPESONCE(P): Each type must only be defined once.

COMPLETETYPES(P): Each type used in the right-hand side of a definition must itself be defined.

- NOSELFSUPER(P): Each abstract type must not occur in the righthand side of its own definition.
- SINGLESUPER(*P*): Each type should occur in the right-hand side of at most one abstract definition.

The first two rules check for the existence and completeness of a program's definitions: TYPESONCE ensures that each type is *defined* only once, and COMPLETETYPES makes sure each type *use* corresponds to a defined type. The rules do not restrict recursion in the data structures or the shapes that can be defined, since they only require that a definition exists and is unique.

Our SINGLESUPER rule enforces a simplifying assumption on our type hierarchies, which restricts types to a form of single inheritance. Together with NOSELFSUPER, the rules ensure a linear supertype relation: each type may only have one supertype. Linearizing supertypes gives us a total ordering on function signatures: each abstract type can have multiple subtypes, but only one supertype. We requiring a total order on function signatures in order to simplify our dispatch semantics and avoid the usual *diamond problem* when multiple inheritance and multiple dispatch interact [57, 21].

3.3 Semantics

We use a (small-step) reduction semantics to model DemeterF traversals. We begin with a description of values v runtime expressions e and evaluation contexts E described in figure 3.3. Values are constructor calls in which all

```
\begin{array}{l} v & ::= \text{ new } C(v_1, \dots, v_n) \\ e & ::= \cdots \\ & | \text{ dispatch}(F, v_0, e_1, \dots, e_n) \\ & | \text{ apply}(f, v_0, v_1, \dots, v_n) \end{array}E & ::= [] \\ & | \text{ new } C(v \dots, E, e \dots) \\ & | \text{ traverse}(E, F) \\ & | \text{ dispatch}(F, v_0, v \dots, E, e \dots) \end{array}
```

Figure 3.3: Values, runtime expressions, and evaluation contexts

sub-expressions are also values. Runtime expressions (dispatch and apply) are not part of our surface syntax, but are used to model structural recursion and function application respectively. The use of apply is mainly cosmetic in order to avoid complicating eventual rules involving dispatch. Evaluation contexts encode our reduction strategy. Reduction can occur under the empty context, [] constructor application, the left argument of a traversal expression, or under a dispatch expression. Overall our evaluation contexts ensure that our reduction strategy is deterministic and *left-most/inner-most*.

Figure 3.4 contains definitions of our reflective meta-functions and substitution. The function *types* is used to return the concrete types of a list of sequence of values. Other functions, *argtypes* and *functions*, are simply convenient accessors for converting between abstract syntax and meta representations. We denote the substitution of a value v for a variable x within an expression e by e[v/x]. Substitution is defined over all terms, including functions and function sets. Within function definitions, substitution only occurs when the variable x is free in the function body. Since only values can be substituted, and functions are not first-class, α -conversion or renaming is not necessary to avoid capture.

Figure 3.5 completes our meta-functions with signature comparison and type-based function selection implemented by *choose*. The helper function *chooseOne* selects the most specific applicable function in a funcset, given the actual argument types. The function *possibleFs* filters the function set, returning only the functions that are *possible* to apply to the given types. The function *possible* returns true if all arguments are element-wise related, since a function may be applied to subtypes of its argument types or when actual arguments are refined from supertypes. At runtime however, the actual arguments are

```
types(\text{new } C_0(\cdots), \ldots, \text{ new } C_n(\cdots)) = (C_0 \ldots C_n)

argtypes((T_0 x_0, \ldots, T_n x_n) \{ \text{ return } e; \}) = (T_0 \ldots T_n)

functions(\text{funcset} \{ f_1 \ldots f_n \}) = (f_1 \ldots f_n)
```

x[v/x]	=	v
x'[v/x]	=	x' if $x' \neq x$
new C (e_1 , \ldots , e_n) $[v/x]$	=	new C ($e_1[v/x]$, \ldots , $e_n[v/x]$)
<code>traverse(</code> e_0 , F) $[v/x]$	=	<code>traverse(</code> $e_0[v/x]$, $F[v/x]$)
dispatch(F , v_0 , e_1 ,, e_n) $[v/x]$	=	dispatch($F[v/x]$, v_0 , $e_1[v/x]$,, $e_n[v/x]$)
<code>apply(f, v_0, v_1, \ldots, v_n)$[v/x]$</code>	=	<code>apply(</code> $f[v/x]$, v_0 , v_1 , \ldots , v_n)
$\texttt{funcset} \{ f_1 \ \dots \ f_n \ \} [v/x]$	=	$\texttt{funcset} \{ f_1[v/x] \dots f_n[v/x] \}$
($T_0 \ x_0$,) { return e ; } $[v/x]$	=	$(T_0 \ x_0, \ldots) \ \{ \texttt{return} \ e; \} \ ext{ if } x \in \overline{x_i}$
($T_0 \; x_0$,) { return e ; } $[v/x]$	=	($T_0 \ x_0$,) { return $e[v/x]$; } if $x ot\in \overline{x_i}$

Figure 3.4: Reflection and Substitution Definitions

 $choose(F, (C_0 \dots C_n)) = chooseOne(possibleFs(F, (C_0 \dots C_n)), (C_0 \dots C_n))$

 $chooseOne((), (T_0 \dots T_m)) = \text{error}$ $chooseOne((f_0 f_1 \dots f_n), (T_0 \dots T_m)) = best(f_0, (f_1 \dots f_n), (T_0 \dots T_m))$

 $best(f, (), (T_0 \dots T_m)) = f$ $best(f, (f_0 f_1 \dots f_n), (T_0 \dots T_m)) = if better(argtypes(f_0), argtypes(f))$ $then best(f_0, (f_1 \dots f_n), (T_0 \dots T_m))$ $else best(f, (f_1 \dots f_n), (T_0 \dots T_m))$

 $\begin{array}{l} better((),\,()) = \, {\tt false} \\ better((T_0 \ T_1 \ \dots \ T_n),\,(T'_0 \ T'_1 \ \dots \ T'_n)) = \ ((T_0 \not\equiv T'_0 \ \land \ T_0 \leq T'_0) \lor \\ (T_0 \equiv T'_0 \ \land \ better((T_1 \ \dots \ T_n),\,(T'_1 \ \dots \ T'_n)))) \end{array}$

 $possibleFs(F, (T_0 \dots T_n)) = filter(\lambda f. possible(argtypes(f), (T_0 \dots T_n)), functions(F))$

 $\begin{array}{l} possible((),\,()) = \, \texttt{true} \\ possible((),\,(T'_0\,\ldots\,T'_m)) = \,\texttt{false} \\ possible((T_0\,\ldots\,T_n),\,()) = \,\texttt{false} \\ possible((T_0\,T_1\,\ldots\,T_n),\,(T'_0\,T'_1\,\ldots\,T'_m)) = \,(T'_0 \leq T_0 \,\lor\, T_0 \leq T'_0) \,\land \\ possible((T_1\,\ldots\,T_n),\,(T'_1\,\ldots\,T'_m)) \end{array}$

Figure 3.5: Function Selection Meta-functions

gument types will always be **concrete** and without subtypes, so the second check $T_0 \leq T'_0$ is irrelevant. This check only becomes important when we use *possibleFs* with approximate types, as is necessary during type checking. The function *chooseOne* uses *best* to select the most specific function in the filtered set, using *better* to compare function signatures. For simplicity we compare only functions with the same number of arguments, though dispatch in our DemeterF implementation is more flexible, allowing functions to ignore later arguments.

Finally, figure 3.6 gives a relation, \rightarrow , which completes our small-step

semantics with a notion of reduction, *i.e.*, with axioms or contraction rules. The left-hand side of each rule represents a potential reducible expression,

```
\begin{split} & [\text{R-TRAV}] \\ & \text{traverse}(v_0, F) \\ & \rightarrow \text{dispatch}(F, v_0, \text{traverse}(v_1, F), \dots, \text{traverse}(v_n, F)) \\ & \text{where } v_0 = \text{new } C(v_1, \dots, v_n) \\ & [\text{R-DISPATCH}] \\ & \text{dispatch}(F, v_0, v_1, \dots, v_n) \rightarrow \text{apply}(f, v_0, v_1, \dots, v_n) & \text{if } f \neq \text{error} \\ & \text{where } f = choose(F, types(v_0 v_1 \dots v_n)) \\ & [\text{R-APPLY}] \\ & \text{apply}((T_0 x_0, \dots, T_n x_n) \{ \text{return } e; \}, v_0, v_1, \dots, v_n) \rightarrow e[\overline{v_i/x_i}] \end{split}
```

Figure 3.6: Reduction Rules

or *potential redex*. If a potential redex can be contracted then it is considered an actual redex, *i.e.*, no longer potential.

A traverse expression with a constructed value as its first argument can be contracted (R-TRAV) producing a dispatch expression. We include the function set F the original value v_0 and wrap each field of the value in a traverse expression that uses the same function set. A dispatch expression containing only values can be contracted (R-DISPATCH) to an apply expression, when the result of *choose* is not **error**. A dispatch expression that violates the side condition is considered *stuck*, *i.e.*, a potential but not actual redex. Any expression that contains a nested stuck expression is itself considered stuck, since contraction cannot occur. A stuck expression represents a runtime dispatch error from a DemeterF traversal. Our last rule (R-APPLY) is an extension of R-DISPATCH, substituting the given values for the formal parameters of the selected function. We use overbar notation, $e[v_i/x_i]$, to represent repeated substitutions: $(e[v_0/x_0] [v_1/x_1] \cdots)$.

3.3.1 From Reduction to Evaluation

Following Danvy's lecture notes at AFP'08 [23], a one-step reduction function can be defined that decomposes a non-value expression into an evaluation context E and a potential redex. If the potential redex can be contracted, then the resulting contractum can be recomposed with (plugged into) the evaluation context resulting in a reduced program. Figure 3.7 gives sketches of the functions *reduce*, *decmp*, and *recmp* that implement the one-step reduction function of our semantics.

We define *reduce* as decomposition followed by contraction and recomposition, when one of our reduction rules applies. The function *decmp* traverses an expression while accumulating an evaluation context. Expression cases

```
\begin{aligned} reduce(v) &= v \\ reduce(v) &= v \\ reduce(e) &= \mathsf{let} \langle e', E \rangle = decmp(e, []) \\ & \text{ in } recmp(e'', E) \\ & \text{ if } e' \to e'' \end{aligned}
\begin{aligned} decmp(\mathsf{new}\ C\ (v\ \dots, e_0, e\ \dots\ ), E) &= decmp(e_0, \mathsf{new}\ C\ (v\ \dots, E, e\ \dots\ )) \\ decmp(\mathsf{traverse}(e_0, F), E) &= decmp(e_0, \mathsf{traverse}(E, F)) \\ decmp(\mathsf{dispatch}(F, v\ \dots, e_0, e\ \dots\ ), E) &= decmp(e_0, \mathsf{dispatch}(F, v\ \dots, E, e\ \dots\ )) \\ decmp(e, E) &= \langle e, E \rangle \end{aligned}
\begin{aligned} recmp(e_0, \mathsf{new}\ C\ (v\ \dots, E, e\ \dots\ )) &= recmp(\mathsf{new}\ C\ (v\ \dots, e_0, e\ \dots\ ), E) \\ recmp(e_0, \mathsf{traverse}(E, F)) &= recmp(\mathsf{traverse}(e_0, F), E) \\ recmp(e_0, \mathsf{dispatch}(F, v\ \dots, E, e\ \dots\ )) &= recmp(\mathsf{dispatch}(F, v\ \dots, e_0, e\ \dots\ ), E) \end{aligned}
```

Figure 3.7: Functions for one-step reduction

that match evaluation contexts are handled explicitly by recurring on the inner, left-most non-value expression. Other expressions, *e.g.*, apply, match the final case returning a pair of the potential redex and inverted context. The function *recmp* does the reverse, building an expression and composing evaluation contexts until the empty context [] is reached.

Our one-step reduction function can be used to iteratively define an evaluation function, as shown in figure 3.8. The function *evaluate* implements

> evaluate(v) = v evaluate(e) = evaluate(reduce(e))if e is not stuck

Figure 3.8: Reduction-based Evaluation Function

the iteration of the one-step reduction function from figure 3.7. This definition can be "refocused" into an abstract machine, and further transformed resulting in a more typical big-step evaluation function [23, 24], but the version of figure 3.8 is sufficient for our purposes. For reasons of efficiency our actual DemeterF implementation is, of course, based on big-step evaluation.

3.3.2 Example

With our example definitions of listing 3.1, we can add a simple traversal and function set that implements (*strict*) BExp evaluation, shown in listing 3.2. Again, without base types, we construct an expression representing (*true* $\land \neg false$) and traverse it using a funcset. Our function set is similar to the Eval function-class from listing 2.12 in section 2.3. The traversal of the expression produces a Lit, representing a result of True or False. Similar to

Listing 3.2: Model Example: Boolean expression evaluation

the DemeterF example, multiple dispatch is used to match interesting cases during traversal. For Neg this means matching True or False and returning its negation; for And or Or this means capturing the all-true and all-false cases respectively. The other two cases for And and Or are handled by more general signatures using Lit.

3.4 Type System

Like regular Java programs, those written using our DemeterF system can raise many different kinds of errors, unrelated to traversal. Our model has been specifically designed to eliminate all but those relating to function sets, and dispatch. In order to rule out runtime errors and predict the class of values a program may return, we impose a type system on our model. Though our type system rules out standard errors like unbound variable uses, we are mostly interested in eliminating errors resulting from function selection (*choose* and *chooseOne* in figure 3.5).

For any type-correct program we obtain a typing derivation that constrains the return values of traversals and function sets based on the shape of the datatypes. Our type system is given by three mutually-recursive judgments: \vdash_e , \vdash_F , and \vdash_T ; one for each of expressions, functions, and traversals. We standard variable type environments Γ for typing expressions and functions. For traversals we use an additional environment \mathcal{X} to track the return types of recursive datatype traversals. We represent environments as a list of pairs, with syntax shown in figure 3.9.

$$\Gamma ::= \emptyset \mid \Gamma, x:T$$
$$\mathcal{X} ::= \emptyset \mid \mathcal{X}, T:T'$$

Figure 3.9: Variable and Traversal Environments

In certain typing rules we will denote the set of the left-hand sides of pairs

from Γ (also \mathcal{X}) by *dom* Γ . New pairs will be appended to environments, and lookup, denoted $\Gamma(x)$, will occur from right to left, selecting the latest binding if duplicate names exist.

3.4.1 Functions

We begin with the simplest of our typing rules. Since functions are not firstclass values, type-checking a function depends only on the type of its body expression when parameters are bound to the types given in its signature. Our rule for \vdash_F is shown in figure 3.10.

 $[\mathsf{T}\text{-}\mathsf{FUNC}] = \frac{(\Gamma, x_0: T_0, \dots, x_n: T_n) \vdash_e e_0: T}{\Gamma \vdash_F (T_0 x_0, \dots, T_n x_n) \{ \texttt{return } e_0; \}: T}$

Figure 3.10: Function Typing Rule

3.4.2 Expressions

Figure 3.11 shows our typing rules for expressions (\vdash_e). Variables must be

 $[T-VAR] [T-VAR] = \frac{x \in dom \Gamma}{\Gamma \vdash_e x : \Gamma(x)} = Concrete \ C = T_1 * \dots * T_n \in P \\ for \ i \in 1..n \quad \Gamma \vdash_e e_i : T'_i \quad T'_i \leq T_i \\ \hline \Gamma \vdash_e new \ C \ (e_1, \dots, e_n) : C \\ [T-TRAV] \\ \hline \Gamma \vdash_e e_0 : T_0 \quad \Gamma; \emptyset \vdash_T \langle T_0, F \rangle : T \\ \hline \Gamma \vdash_e traverse (e_0, F) : T \\ [T-DISPATCH] = \emptyset \vdash_e v_0 : C \\ for \ i \in 1..n \quad \Gamma \vdash_e e_i : T'_i \\ for \ f \in possible Fs(F, \ (C \ T'_1 \dots T'_n)) \quad \Gamma \vdash_F f : T_f \quad T_f \leq T \\ \hline covers(F, \ (C \ T'_1 \dots T'_n)) \\ \hline \Gamma \vdash_e dispatch(F, v_0, e_1, \dots, e_n) : T \\ [T-APPLY] \\ f = (T_0 \ x_0, \dots, T_n \ x_n) \{ \text{return } e_i \} \quad \Gamma \vdash_F f : T \\ \hline for \ i \in 0..n \quad \emptyset \vdash_e v_i : T'_i \quad T'_i \leq T_i \\ \hline \Gamma \vdash_e apply(f, v_0, v_1, \dots, v_n) : T \\ \end{cases}$

Figure 3.11: Expression Typing Rules

bound to a type in the environment (T-VAR) and value construction requires

subtypes (T-NEW) for each expression (*i.e.*, *field*) of a concrete structure. Traversal expressions (T-TRAV) delegate to a more specialized judgment, $\vdash_{\mathcal{T}}$ (presented in section 3.4.3), passing the variable environment and an empty traversal environment, $\mathcal{X} = \emptyset$. For dispatch expressions (T-DISPATCH) we use *possibleFs* to be sure all *possible* functions unify to a common supertype. Function application (T-APPLY) requires subtypes of a function's formal parameter types.

One subtle (but key) aspect of the T-DISPATCH rule is the use of the metafunction, *covers*. Its properties will be discussed in section 3.4.4, but the main idea of *covers* is to verify that a function set F contains a possible function for each possible argument sequence of concrete types that are subtypes of the given sequence. In T-DISPATCH, this means that F has at least one function that can be applied to possible *values* of the given types. The use of *covers* in this rule corresponds to our typing rules for concrete traversals, which is discussed in the next section.

3.4.3 Traversals

Traversal expressions are typed using a specific judgment $\vdash_{\mathcal{T}}$ that takes into account the types of functions in the set and the program's data structure definitions. The two rules, one for each of abstract and concrete types, are shown in figure 3.12.

```
 \begin{array}{c} [\text{T-ATRAV}] \\ \text{abstract } A = T_0 \mid \dots \mid T_n \in P \\ \text{for } i \in 1..n \quad T_i \in dom \ \mathcal{X} \ \Rightarrow \ T_i' = \mathcal{X}(T_i) \\ \text{for } i \in 1..n \quad T_i \notin dom \ \mathcal{X} \ \Rightarrow \ \Gamma; \ \mathcal{X}, \ A: T \vdash_{\mathcal{T}} \langle T_i, F \rangle : T_i' \\ \hline for \ i \in 1..n \quad T_i' \leq T \\ \hline \Gamma; \ \mathcal{X} \vdash_{\mathcal{T}} \langle A, F \rangle : T \end{array} 
 \begin{array}{c} [\text{T-CTRAV}] \\ \text{concrete } C = T_1 \ast \dots \ast T_n \in P \\ \text{for } i \in 1..n \quad T_i \in dom \ \mathcal{X} \Rightarrow \ T_i' = \mathcal{X}(T_i) \\ \text{for } i \in 1..n \quad T_i \notin dom \ \mathcal{X} \Rightarrow \ \Gamma; \ \mathcal{X}, \ C: T \vdash_{\mathcal{T}} \langle T_i, F \rangle : T_i' \\ \text{for } f \in possible Fs(F, (C \ T_1' \ \dots \ T_n')) \quad \Gamma \vdash_F f : T_f \quad T_f \leq T \\ \hline covers(F, (C \ T_1' \ \dots \ T_n')) \\ \hline \Gamma; \ \mathcal{X} \vdash_{\mathcal{T}} \langle C, F \rangle : T \end{array}
```

Figure 3.12: Traversal Typing Rules

We read $\Gamma; \mathcal{X} \vdash_{\mathcal{T}} \langle T, F \rangle : T'$ as follows :

In type environment Γ with traversal types \mathcal{X} the traversal of a value of type T with function set F returns a value of type T'.

 Γ is the standard variable type environment. \mathcal{X} is an environment of traversal return types for (possibly recursive) types that may depend on the traversal return of T. The function set F is constant for a given expression, and is passed throughout a derivation.

The typing of the traversal of an abstract type proceeds by typing each of its elements T_i separately. If a binding for T_i exists in \mathcal{X} (*i.e.*, $T_i \in dom \mathcal{X}$) then the result T'_i must be the same as the bound result type, which we denote $\mathcal{X}(T_i)$. Otherwise, we calculate the result type by adding A:T to \mathcal{X} using the same function set, F. The final line of the premise constrains the result type for the abstract type to be a common supertype of the traversal the individual elements.

The rule for concrete types is more involved, due to function selection. Similar to abstract types, for *field* types bound in \mathcal{X} , must be the same as the bound result type, *i.e.*, $T'_i = \mathcal{X}(T_i)$. For unbound field types we calculate the result type of a traversal with C:T added to \mathcal{X} using the same function set F. Using the return types T'_i of field traversals we can approximate the possible functions from F that can be called after traversing an instance of C. The final return type T is the common supertype of the *possibleFs* given the field return types. On the last line of our premise, the meta-function *covers* is used to determine whether or not the function set is *complete* with respect to all possible value sequences corresponding to subtypes of the given types. The attributes of *covers* are quite important to the type soundness of our model and deserve a special discussion that follows.

3.4.4 Function Set Coverage

Type checking DemeterF programs infers the return types of traversal expressions, but being sure that function selection always succeeds requires an analysis of function set signatures. In particular, our asymmetric multiple dispatch implemented by *choose* means that after traversing a concrete value, any of the *possible* functions may be called based on the types of sub-traversal return values. In general, we cannot know (until runtime) which concrete subtypes will be returned, so we require that all cases be handled by the function set.

In order to guarantee successful dispatch, *covers* must check all concrete subtypes of the possible argument types and ensure that a *possible* function exists. Because our type hierarchies and function signatures can be arranged into trees (or at least *directed acyclic graphs*), we call the problem *leaf-covering*. The solution involves the Cartesian product of the sequence of type hierarchies, which will be discussed thoroughly in chapter 5 (section 5.3).

The actual implementation of *covers* is not important to our soundness, we only require the specification that each concrete sequence of subtypes has a *possible* function:

 $covers(F, (T_0 T_1 \dots T_n)) \Leftrightarrow$

 $\forall C_0, C_1, \ldots, C_n \text{ with } C_i \leq T_i \cdot possibleFs(F, (C_0 C_1 \ldots C_n)) \neq ()$

As a consequence, *covers* is preserved by subtyping. If $\forall i \in 1..n \, . \, T'_i \leq T_i$, then:

 $covers(F, (T_0 T_1 \dots T_n)) \Rightarrow covers(F, (T'_0 T'_1 \dots T'_n))$

Because runtime values are made only of concrete types, *e.g.*, (Neg (True)), then function selection cannot fail as long as sub-traversals (at runtime) return subtypes of their expected types. Different implementations of *covers* will be examined in chapter 5, and the abstract problem of leaf-covering is *coNP-complete*. However, in practice the number of function arguments (*i.e.*, structure fields) tends to be small, and individual type hierarchies are usually tractable. In our DemeterF implementation the largest number of arguments is 13. With approximately 90 classes in all, the deepest subtype chain is 4 classes, *i.e.*, $C \leq A_1 \leq A_2 \leq A_3$.

3.4.5 Typing Example

Returning to our model example from listing 3.2, we can assign a type to the body of our program using the T-TRAV rule. The first argument to traverse is given the type Or by successive applications of T-NEW. Since True and False have no fields, their constructions become axioms for the derivation. The second part of T-TRAV requires the use of our traversal judgment:

$$\emptyset; \emptyset \vdash_{\mathcal{T}} \langle \operatorname{Or}, F \rangle : T$$

From the definitions in listing 3.1, Or is a concrete type, so a derivation requires the use of T-CTRAV:

$$\begin{array}{l} \texttt{concrete Or} = \texttt{BExp} * \texttt{BExp} . \in P \quad \emptyset; (\emptyset, \texttt{Or} : T_{\texttt{or}}) \vdash_{\mathcal{T}} \langle \texttt{BExp}, F \rangle : T_{\texttt{bexp}} \\ \hline \texttt{for} \ f \in \textit{possibleFs}(F, (\texttt{Or} \ T_{\texttt{bexp}} \ T_{\texttt{bexp}})) \quad \emptyset \vdash_{F} f : T_{f} \quad T_{f} \leq T_{\texttt{or}} \\ \hline \textit{covers}(F, (\texttt{Or} \ T_{\texttt{bexp}} \ T_{\texttt{bexp}})) \\ \hline \emptyset; \emptyset \vdash_{\mathcal{T}} \langle \texttt{Or}, F \rangle : T_{\texttt{or}} \end{array}$$

The traversal type derivation recursively continues to the abstract types BExp and Lit, eventually coming to the applications of T-CTRAV for True and False that do not require recursion. For these types there is only one *possible* function, which simplifies the rule further. An instance for the type True is shown below.

$$\begin{array}{l} \texttt{concrete True} = . \in P \\ \emptyset \vdash_F (\texttt{Lit 1}) \{\texttt{return 1}; \} : \texttt{Lit Lit} \leq T_{\texttt{true}} \\ \hline \\ covers(F, (\texttt{True})) \\ \hline \\ \emptyset; \mathcal{X} \vdash_T \langle \texttt{True}, F \rangle : T_{\texttt{true}} \end{array}$$

Assigning a type to the single function and checking function set coverage is then trivial. The constraints build up as we come back through the abstract

definitions of Lit and BExp. Ignoring other variants of BExp for simplicity, we have the constraints:

```
Lit \leq T_{true} Lit \leq T_{false} T_{true} \leq T_{lit} T_{false} \leq T_{lit} T_{lit} \leq T_{bexp}
```

We can make these true by setting each of the return types to Lit. Other BExp variants (Neg, And, and Or) are recursive, which causes equality constraints to be generated instead.

3.5 Type Soundness

Our type system is sound in the sense that the reduction of a well-typed AP-F program will not get *stuck*, and will result in a value of the expected type. An expression e is considered *stuck* if there does not exist an expression e' such that $e \rightarrow e'$. In particular, an expression is stuck if it is of the form:

 $E[\text{dispatch}(F, v_0, v_1, \dots, v_n)]$

and choose (figure 3.5) results in an error:

$$choose(F, types(v_0 v_1 \dots v_n)) =$$
error

We note that *choose* returns error precisely when:

$$possibleFs(F, types(v_0 v_1 \dots v_n)) = ()$$

Meaning that F does not contain a function applicable to the given arguments.

We prove our soundness result via a Wright-Felleisen style proof [73] that begins with a few AP-F specific lemmas (function and traversal specialization) then moves on to more standard soundness lemmas such as substitution and well-typed contexts. In order to prove that reduction preserves the type of a program, it is necessary to start at the dispatch level and work up to expressions. We begin by proving that *possibleFs* applied to a sequence of subtypes returns a *subset* of the functions returned by *possibleFs* applied to supertypes.

Lemma 3.5.1 (Function Specialization). As a sequence of argument types is specialized through subtyping, the set of possible functions does not increase.

```
If \forall i \in 1..n \ T'_i \leq T_i then
possibleFs(F, (T'_1 \dots T'_n)) \subseteq possibleFs(F, (T_1 \dots T_n))
```

Proof: We argue using induction on the type sequences by case analysis of the definition of *possible* form figure 3.5, used to filter the functions of F. Consider a single function $f \in F$ with formal argument types, $(T_0^f \ldots T_m^f)$. Our lemma depends on a single implication that must hold of *possible*, given our subtype sequence assumption:

$$possible((T_0^f \ldots T_m^f), (T_0' \ldots T_n')) \Rightarrow possible((T_0^f \ldots T_m^f), (T_0 \ldots T_n))$$

The three base cases of *possible* (figure 3.5) are simple, so we consider them together. If the first case applies, and then our implication follows immediately, while the two false cases are not relevant, since they only stand to decrease the set of selected functions. Proof of the lemma then hinges on showing that our implication holds for the final, inductive case of the definition. In particular, the first component of the conjunction is important. In our case this reduces to:

$$(T_0^f \le T_0') \lor (T_0' \le T_0^f) \implies (T_0^f \le T_0) \lor (T_0 \le T_0^f)$$

Which follows from reflexivity and transitivity of a program's subtype relation, \leq . Both disjunction components of the implication are immediate:

$$(T_0^f \le T_0') \Rightarrow (T_0^f \le T_0) \text{ and } (T_0' \le T_0^f) \Rightarrow (T_0 \le T_0^f)$$

In order to complete the dispatch portion of preservation, we must also show that the application of a function set within a well-typed traversal expression preserves the result type, which is the subject of lemma 3.5.2.

Lemma 3.5.2 (Traversal Specialization, or Subtype Traversals Return Subtypes). As the type of an expression that is the argument of a traversal is refined, the return type of the traversal expression itself remains a subtype of its original type.

For any well-typed traversal of a type T_0 with $\Gamma; \emptyset \vdash_{\mathcal{T}} \langle T_0, F \rangle : T$. The traversal of a type $T'_0 \leq T_0$ satisfies $\Gamma; \emptyset \vdash_{\mathcal{T}} \langle T'_0, F \rangle : T'$ for some $T' \leq T$

Proof: By induction on the traversal type derivation of Γ ; $\emptyset \vdash_{\mathcal{T}} \langle T_0, F \rangle : T$, we proceed by cases on the last rule of the derivation, which must be one of T-CTRAV or T-ATRAV, from figure 3.12.

If T-ATRAV applies (abstract $A = T_0 | \dots | T_n \in P$) then the rule requires that a traversal of an immediate subtype of T_0 return a subtype of the final result type, which applies inductively to all transitive subtypes of T_0 , including T'_0 .

If T-CTRAV applies (concrete $C = T_1 * \ldots * T_n \in P$) then T_0 can only have itself as a subtype ($T_0 \equiv T'_0$). Regardless of which function in F is actually applied at runtime, we know by the T-CTRAV derivation that each function returns a subtype, from the premises of the rule.

The final lemmas for preservation are value substitution and well-typed contexts. Substitution proves that function application preserves the type of a traversal expression:

Lemma 3.5.3 (Substitution Preserves Type). Substituting a value of a subtype for a free variable in any expression results in a subtype of the original expression's type.

Suppose $\Gamma \equiv (\Gamma', x:T_x)$. If $\Gamma \vdash_e e: T$, $\emptyset \vdash_e v: T'_x$, with $T'_x \leq T_x$ then $\Gamma' \vdash_e e[v/x]: T'$ and $T' \leq T$.

Proof: By induction on the derivation of $(\Gamma, x : T_x) \vdash_e e : T$. Traversal expressions require lemma 3.5.2, and dispatch expressions require lemma 3.5.1. We proceed by cases on the last rule used:

- **Case** T-VAR e = x'. If $x' \neq x$ then $x': T \in \Gamma'$ and $\Gamma' \vdash_e x': T$. If x' = x then e[v/x] = v and $T'_x \leq T_x$ by our assumptions.
- **Case** T-NEW e = new C (e_1, \ldots, e_n) with T = C. By the induction hypothesis, for all $i \in 1..n \ \Gamma \vdash_e e_i[v/x] : T''_i$ for some $T''_i \leq T'_i$ with $T''_i \leq T_i$ by transitivity of \leq . So $\Gamma \vdash_e \text{new } C$ ($e_1[v/x], \ldots, e_n[v/x]$) : C.
- **Case** T-TRAV $e = \text{traverse}(e_0, F)$. By the induction hypothesis, $\Gamma' \vdash_e e_0[v/x] : T'_0$ for some $T'_0 \leq T_0$. By lemma 3.5.2 the traversal result is $\Gamma; \emptyset \vdash_T \langle T'_0, F \rangle : T'$ for some $T' \leq T$, so $\Gamma' \vdash_e \text{traverse}(e_0[v/x], F[v/x]) : T'$ and $T' \leq T$.

Case T-APPLY
$$e = \operatorname{apply}(f, v_0, v_1, \ldots, v_n)$$
.
with $f = (T_0 x_0, \ldots, T_n x_n)$ { return e_0 ; }. If $x \in \overline{x_i}$ then substitution has no effect and the result is T . If $x \notin \overline{x_i}$ then by the induction hypothesis, $(\Gamma', x_0:T_0, \ldots, x_n:T_n) \vdash_e e_0[v/x]: T'$ for some $T' \leq T$.

Case T-DISPATCH $e = \text{dispatch}(F, v_0, e_1, \dots, e_n)$. By the induction hypothesis, for all $i \in 1..n$ $\Gamma \vdash_e e_i[v/x] : T''_i$ and $T''_i \leq T'_i$. By lemma 3.5.1 we know that:

 $possibleFs(F, (C T'_1 \dots T''_n)) \subseteq possibleFs(F, (C T'_1 \dots T'_n))$

So there exists a type $T' \leq T$ such that:

$$\forall f \in possibleFs(F, (C T_1'' \dots T_n'')) \ \Gamma \vdash_F f : T_f$$

with $T_f \leq T'$. The result is:

 $\Gamma \vdash_e \texttt{dispatch}(F[v/x], v_0, e_1[v/x], \ldots, e_n[v/x]): T'$

By the implication property of *covers*:

 $covers(F, (C T'_1 \dots T'_n)) \Rightarrow covers(F, (C T''_1 \dots T''_n))$

So our *covers* premise still holds.

Cases of substitution within functions/sets follow directly from our induction hypothesis.

Well-typed contexts shows that recomposition of an expression and a context also preserves the type of the outer context. The lemma and proof are similar to substitution.

Lemma 3.5.4 (Well-Typed Contexts). Substituting a closed, well-typed expression, which is a subtype of the original, into the hole of a context preserves the outer context's type.

For any closed expressions e, e', and context E, if $\emptyset \vdash_e e : T$, $\emptyset \vdash_e e' : T'$ with $T' \leq T$, and $\Gamma \vdash_e E[e] : T_0$, then $\Gamma \vdash_e E[e'] : T'_0$ for some $T'_0 \leq T_0$.

Proof: By induction on the structure of the outermost context E and the typing derivation of E[e].

- **Case** E = []. Follows from our assumptions, since $\emptyset \vdash_e e : T$, $\emptyset \vdash_e e' : T'$ and $T' \leq T$.
- **Case** $E = \text{new } C (v \dots, E', e_i \dots)$. By the induction hypothesis, replacing e with e' in E' maintains the premises of T-NEW. The result type remains C.
- **Case** E = traverse(E', F). In T-TRAV, by the induction hypothesis and lemma 3.5.2, the traversal of E'[e'] with the same function set, F, must return a subtype of the traversal result type of E'[e].
- **Case** $E = dispatch(F, v_0, v \dots, E', e_i \dots)$. In T-DISPATCH, by the induction hypothesis and lemma 3.5.1, the *possible* functions with E'[e'] instead of E'[e] remains a subset, and must unify to a common supertype, which is a subtype of that obtained with E'[e]. The premise of *covers* also holds, with proof similar to substitution.

We can now state the first half of our soundness theorem: preservation.

Theorem 1 (Preservation). *Reduction (i.e., contraction) preserves an expression's type.*

If $\Gamma \vdash_e E[e] : T$ and $E[e] \rightarrow E[e']$ then $\Gamma \vdash_e E[e'] : T'$ with $T' \leq T$.

Proof: Using lemma 3.5.4, our proof reduces to showing that our individual reductions preserve type. That is, we must show that $\emptyset \vdash_e e : T_e$ and $e \rightarrow e'$

implies $\emptyset \vdash_e e' : T'_e$ and $T'_e \leq T_e$. If we prove this implication, then by lemma 3.5.4 it is true that $\Gamma \vdash_e E[e'] : T'$ for some $T' \leq T$.

We proceed by showing the implication holds for each of our reduction rules.

Case If R-APPLY applies . Follows from substitution, lemma 3.5.3.

- **Case** If R-DISPATCH applies . Since the function selected, f, is one of the *possible* functions ($choose(F, (T_0 \dots T_n)) \in possibleFs(F, (T_0 \dots T_n))$), f is used in the premise of our typing rule (T-DISPATCH). Proof follows immediately, as the rule requires that the return types of all *possible* functions be a subtype of the assigned type.
- **Case** If R-TRAV applies. The typing derivation of the traversal expression includes both a sub-derivation for the value to be traversed, $e_0 = \text{new } C(v_1, \ldots, v_n)$, and a traversal judgment based on the definition of C. By the first sub-derivation, we know that $\emptyset \vdash_e v_i : C_i$ for some $C_i \leq T_i$ where T_i is from the definition of C. The traversal typing for each field type T_i contains as a sub-derivation a typing rule for C_i , which can be used to construct a traversal derivation for the expanded traverse term.

By lemma 3.5.1 the *possible* functions to be used in the typing derivation of the dispatch expression are a subset of those used in the traversal rule for C, and likewise unify to a common supertype (T'_e) , which is a subtype of the original, T_e . The use of *covers* in the traversal rule (T-CTRAV) for C remains the same for dispatch.

While preservation itself is interesting, as important is the preservation of function set *completeness*: if a traversal expression is well typed, then *covers* holds after traversal reduction, R-TRAV.

Corollary 1 (Preservation of covers). The reduction of a well-typed traverse expression to a dispatch expression maintains the predicate "covers".

If an expression $e = traverse(v_0, F)$ such that $\emptyset \vdash_e e : T$ reduces to $e' = dispatch(F, v_0, e_1, \ldots, e_n)$, then covers holds for the reduced expression.

The result of the corollary is that throughout (recursive) traversal reductions *covers* is preserved, so it necessarily holds when function selection is made, and a dispatch expression is contracted to apply.

Soundness rests on progress, which in turn relies on function selection succeeding. While preservation says that our *possible* functions return the right types, progress requires that there exists a possible function for well-typed traversals.

Theorem 2 (Progress). A closed, well-typed expression is either a value, or can be reduced, i.e., is never stuck.

For any expression e such that $\emptyset \vdash_e e : T$, then either e is a value, or e = E[e'] and $E[e'] \rightarrow E[e'']$.

- **Proof**: By induction on the structure *e*.
 - **Case** e = x. This case is impossible since *e* is closed.
 - **Case** $e = \text{new } C(e_1, \ldots, e_n)$. If all e_i are values, then e is also a value. Otherwise, by the induction hypothesis, we can decompose e into E[e'] with $E = \text{new } C(v \ldots, E', e_i \ldots)$, for for the first non-value and some E', and e' can be reduced.
 - **Case** $e = \text{traverse}(e_0, F)$. If e_0 is a value, then R-TRAV applies. Otherwise, by the induction hypothesis we can decompose e into E[e'] with E = traverse(E', F), for some E', and e' can be reduced.
 - **Case** $e = \text{dispatch}(F, v_0, e_1, \ldots, e_n)$. If not all e_i are values, then by the induction hypothesis we can decompose e into E[e'] with $E = \text{dispatch}(F, v_0, v \ldots, E', e_i \ldots)$, for some E', and e' can be reduced.

If all e_i are values, then R-DISPATCH applies. Because e is well-typed, it must be the case that $\emptyset \vdash_e v_0 : C_0$ and for all $i \in 1..n \ \emptyset \vdash_e e_i : C_i$. Our premises require that $covers(F, (C_0 \ C_1 \ \dots \ C_n))$, which matches our necessary property of *covers*: $possibleFs(F, (C_0 \ C_1 \ \dots \ C_n)) \neq ()$.

```
Case e = apply(f, v_0, v_1, ..., v_n).
With f = (T_0 x_0, ..., T_n x_n) { return e_0; }. R-APPLY is immediately applicable.
```

With preservation and progress we can now state and prove our soundness theorem.

Theorem 3 (Type Soundness). A closed, well-typed expression *e* is either a value, or can be reduced to another well-typed expression.

For any expression e such that $\emptyset \vdash_e e : T$, then e is either a value of type T, or $e \to e'$ and $\emptyset \vdash_e e' : T'$, with $T' \leq T$.

Proof: By PROGRESS, *e* is either a value or can be reduced. By PRESERVA-TION, if *e* reduces to *e'*, then $\emptyset \vdash_e e' : T'$ and $T' \leq T$.

Wright and Felleisen [73] refer to this theorem as *strong* soundness, since reduction is never stuck and the type of the result is correctly predicted. The standard form of type soundness is what they call *weak* soundness:

For any well-typed expression, e, if $e \rightarrow e'$, then e' is not *stuck*.

The proof of weak soundness for AP-F is immediate from Theorem 3, since a stuck dispatch expression is not a value.

CHAPTER 4 DemeterF Implementation

Having seen a number of programming examples using DemeterF and a precise model of traversal-based programming with function-objects, in this chapter we discuss the implementation of DemeterF. We first describe the overall system organization, then detail the more important and interesting pieces, and their relation to other parts of the dissertation.

We use the name DemeterF to refer collectively to the implementation of three main Java components: a generic traversal library, a class generator, and a combined type checker and inlined traversal generator.

4.1 Traversal Library

The traversal library contains classes and functions for writing dynamic traversals using function-objects. It includes base function-classes (*e.g.*, FC and TU), different implementations of Traversal, and a dynamic implementation of asymmetric multiple dispatch (*i.e.*, *choose* from figure 3.5). Both traversal and dispatch are implemented using Java reflection, which limits performance, but also shortens the development cycle of function-classes. The traversal library corresponds to an implementation of the semantic and evaluation functions from our DemeterF model (sections 3.3 and 3.3.1). Details of our dispatch/selection algorithm are described in the next chapter.

Our reflective Traversal and dispatch implementations make extensive use of a functional data structure library that was designed specifically to support programming with DemeterF. The data structures include parametrized implementations of List, Set, Map, and an ML-like Option type. Though this forces programmers to learn a new set of structures and operations, it also yields more concise programs, and data structures are described by CD, so they can be automatically parsed, printed, and traversed without handling them as special cases in our other tools.

The traversal and data structure libraries are stand-alone, but we have used them to build the other tools of the DemeterF system including the class generator, type checker and traversal inliner. The library portion of DemeterF also has been implemented in C#, though porting other parts of DemeterF to C# is an item of future work.

4.2 Class Generator

A major part of the DemeterF system is its class generator, as partially described in section 2.1. The job of the class generator is to merge together structural descriptions (in the form of a CD file) and behavioral descriptions (in the form of a BEH file) into Java source files and class definitions. The tool began as an improved version of DemeterJ [67] in order to make use of parametrized types and generic class/interface definitions. The original implementation was built using the DemeterF traversal and data structure libraries to produce the resulting Java files, while using DemeterJ to create abstract syntax trees for CD and BEH structures. The system grew quickly and was soon able to completely support its own development by generating the necessary classes, parsers and printers.

Figure 4.1 shows a high-level view of the class generator's architecture. The generator has four main components. The first performs sanity checks

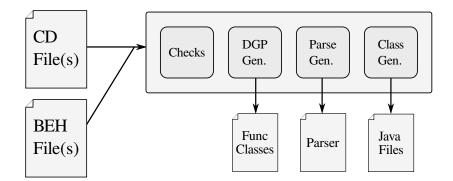


Figure 4.1: High-level view of the DemeterF class generator

on the CD definitions. The checks include making sure that every used class is defined, and that all generic uses have the correct number of type parameters. The second generates generic functions (*e.g.*, Show and TP) for the selected structures. Generic functions (so-called data-generic programming, or DGP, functions) to be created are given via the command line. The generation process is similar to the templates described in section 2.7.2, though they are implemented using traversals.¹ The third component generates a parser for the structures by producing a ".jj" file, which is later turned into Java code by JavaCC. The final component generates Java files/classes corresponding to the CD definitions. The class representations include the BEH definitions, stub methods inserted by the DGP and parser components, and several other useful methods (*e.g.*, equals).

¹User implementations can also be loaded as long as they are in the class path.

4.2.1 Traversal Usage

From the beginning the DemeterF class generator has used traversals for many different tasks. Apart from class and parser generation, DemeterF now uses traversals for everything from filtering out the syntax of CD definitions and verifying parametrized class instantiations to collecting inheritance information. The entire tool comprises approximately 25 traversals of varying complexity. Traversal control used mostly for performance, and contexts are used to keep track of local CD related information (*e.g.*, current package and generic type environment).

Each major function/operation in the class generator is placed in a separate function-class with *combine* (and *update*) methods for the particular parts of the data structure it is concerned with. Most function-classes have a helper method (similar to those discussed in section 2.2.2) that creates a Traversal and calls *traverse*, though we use traversal *factories* to allow the exact traversal implementation to be changed easily.² While the DemeterF class generator does not correspond directly to any portion of the model, it does provide us with a reasonably sized application and has proven to be a useful test and benchmark for DemeterF features and performance (see chapter 6).

4.3 Type Checking

The type system presented in the previous chapter is the basis for an implementation of a type checker and traversal inliner for DemeterF. The type checker calculates the return types for the traversal of a data structure with a given function-class, which are in turn used to generate efficient traversal and dispatch code for the specific function. While the type *checker* is quite similar to our type *system*, it also supports checking traversals with features discussed in chapter 2, namely function extension, traversal contexts, and control.

For function-class extension the type checker simply traces the function's inheritance hierarchy to collect any non-overridden *combine* and *update* methods. For traversal contexts the type checker places the context type (*e.g.*, Sign from section 2.4) as the last argument type when selecting *combine* methods (*i.e.*, *possibleFs* in T-CTRAV from figure 3.12). Similarly, for control, *bypass* ed fields cause the original field type to be used in *combine* selection, whereas the traversals of fields that are not bypassed are type checked as normal.

²Mainly for testing and measuring performance.

4.3.1 Relation to Soundness

Though our model and type system is less complex than its implementation in DemeterF, it captures the essence of our deep traversal and multiple dispatch. Because the dispatch in both cases is the same, modulo extra arguments, the meaning of type soundness in relation to our type checker and traversal implementation does not change. It is still that case that a traversal (and function-class) that satisfies the type checker will not raise any runtime dispatch errors (*c.f.*, section 2.8).

In particular, this means that when an instance of the function-class is used to traverse an instance of the data structure, the traversal will always be able to select an applicable *combine* method. In order to ensure method coverage, for each dispatch point we use the type of the current class and calculated recursive traversal types as arguments to an implementation of *covers* (from section 3.4.4). If the function-class does not cover the traversal results then the missing *combine* methods are reported to the programmer. The properties of our coverage algorithm, called *Leaf Covering*, are discussed more thoroughly in chapter 5, specifically section 5.3.

4.3.2 Traversal Inlining

The DemeterF type checker calculates the return types of a traversal with a given function-class. While showing that a specific traversal is safe is important, we can also use the traversal return types to convert our dynamic, adaptive traversals into static, more efficient code. In DemeterF, after type checking we use the traversal return types to generate a replacement class that is equivalent to Traversal specialized to the particular function-class and data structure. With the return types we calculate the possible *combine* methods for each dispatch point (*i.e.*, after the traversal of an instance of a concrete class), and the method parameter types are used to statically build a dispatch decision that implements *choose*. In the next chapter we precisely describe the algorithms involved, and the resulting performance is discussed in chapter 6.

CHAPTER 5 Algorithms

The safety and performance of DemeterF-based programs rely on the implementation of a number of algorithms including method dispatch, method coverage, and inlining. In this chapter we discuss DemeterF related algorithmic problems, their implementations, and running times.

5.1 Concepts and Notation

We begin with some useful background concepts and notation. In programming languages with inheritance and subtyping one often deals with models and meta-information representing type hierarchies. In DemeterF we are primarily concerned with single inheritance (*i.e.*, C# and Java), resulting in a *tree* (a restricted graph) of types where the parent/child relationships represent both inheritance and subtyping. Two typical examples of type hierarchies are lisp-style cons lists and simple numerical expressions. Java class definitions and their visual tree representations are shown in Figures 5.1 and 5.2.

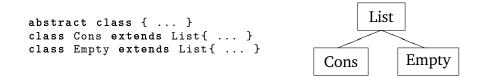


Figure 5.1: List classes and hierarchy tree

We use this more abstract, tree representation for class hierarchies in order to discuss algorithms related to multi-methods, which is particularly useful when discussing features of method selection, coverage, and static dispatch. In the rest of this section we introduce a more formal notion of trees, argument signatures, and graph Cartesian products that will be used in describing our algorithms.

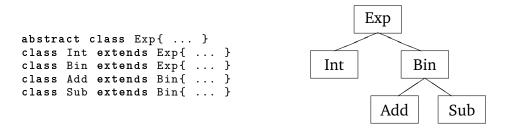


Figure 5.2: Arithmetic expression classes and hierarchy tree

5.1.1 Trees

A *tree*, $T = (\Sigma, \prec)$, is defined over an alphabet of symbols, Σ . Edges of the tree are defined by an immediate successor relation, $\prec \subseteq (\Sigma \times \Sigma)$. For two symbols $a, b \in \Sigma$, an edge exists from a to b when $b \prec a$. For simplicity we restrict the successor relation to be *injective*, modeling single inheritance. This kind of tree can also be viewed as a directed acyclic graph (DAG) where each non-root node has a unique immediate predecessor.

We use less-than, <, to denote the transitive closure of the immediate successor relation:

$$\forall a, b \in \Sigma \, . \, b < a \equiv b \prec a \lor \exists c \in \Sigma \, . \, b < c \land c < a$$

The reflexive, transitive closure of \prec is denoted by less-than-or-equal, \leq .

Given a tree $T = (\Sigma, \prec)$, we define the function leaves, to return the nodes in a tree without successors:

$$leaves(T) \equiv \{ a \in \Sigma \mid \neg \exists b \in \Sigma . b \prec a \}$$

And the function succes that returns the immediate successors of a given node in a tree:

$$\operatorname{succs}(T, b) \equiv \{ a \in \Sigma \mid b \prec a \}$$

The leaves of a tree represent the *concrete* classes in a hierarchy, and the result of succes represents a type's immediate subclasses.

When writing examples we will use a type/symbol, *e.g.*, Bin, to refer to either the symbol Bin or the tree with Bin as its root, though the meaning will be clear from context. For example, using the tree Exp from figure 5.2 we get the following results:

```
leaves(Exp) = \{ Int, Add, Sub \} \\ succs(Exp, Exp) = \{ Int, Bin \} \\ succs(Exp, Bin) = \{ Add, Sub \}
```

5.1.2 Signatures

To represent a method's formal and actual argument types we define a *signature* as a sequence of symbols. For simplicity we will use both vector (over-arrow) and sequence notations to denote signatures, depending on context, *e.g.*, $\vec{s} = (s_1, \ldots, s_n)$. Given a sequence of trees, (T_1, \ldots, T_n) , with each $T_i = (\Sigma_i, \prec)$, a signature is defined as an element of $(\Sigma_1 \times \cdots \times \Sigma_n)$. For example, using the trees from Figures 5.1 and 5.2, the signature (Add, Cons) could represent the formal parameter types of the method:

```
int combine(Add a, Cons c)
```

Or the types of actual arguments in the method call:

```
f.combine(new Add(...), new Cons(...))
```

For specific algorithms we will need to update/replace a specific element within a signature:

update(
$$\vec{s}$$
, i , a) \equiv $(s_1, \ldots, s_{i-1}, a, s_{i+1}, \ldots, s_n)$

Given a sequence \vec{s} , an integer i, and a symbol a, the function update returns a new sequence with the i^{th} component of \vec{s} replaced by a. The symbol a is assumed to be from the same tree as s_i : $s_i, a \in \Sigma_i$.

Sets of signatures will be used to model the argument types of methods in DemeterF function-classes. Given a sequence of trees, $()T_i, \ldots, T_n)$, we extend the immediate successor relation, \prec_i , from symbols to signatures to define two different comparisons: *symmetric* (\leq) and *asymmetric* (\Box). The first models method and argument applicability and the second models method selection and preference/ordering.

Symmetric Comparison Applying a method to arguments requires that the types of the arguments be subtypes of the method's formal parameter types. In comparing two signatures, each parameter is given equal, or *symmetric*, treatment. We call this relation *applicable*, and write it as \leq . Similar to symbol/tree relations, we begin by defining an immediate successor relation, \prec , on signatures using the successor relations, \prec_i , from our *n* trees:

$$\vec{c} \prec \vec{a} \equiv \exists i . c_i \prec_i a_i \land \forall j \in [1..n] . j \neq i \implies c_j = a_j$$

Two signatures are related by \prec when they differ only by their i^{th} element, and the corresponding elements are related in the i^{th} tree by \prec_i . We will use < for the transitive closure of \prec over signatures, with symmetric comparison defined as the reflexive, transitive closure of the immediate successor relation:

$$\vec{c} \leq \vec{a} \equiv \vec{c} = \vec{a} \lor \vec{c} < \vec{a}$$

We say that a signature \vec{a} is applicable to a signature \vec{c} if $\vec{c} \leq \vec{a}$, where \vec{a} and \vec{c} represent a method's formal and actual argument types respectively. This gives us a notion of methods that can be applied to a sequence of arguments, but it does not provide a total ordering. Ambiguities arise when two signatures are both applicable to the same signature, but neither is applicable to the other. For example, consider the signatures, (Int, Int), (Exp, Int), and (Exp, Int). Given our tree in figure 5.2 the following, are true:

```
(Int, Int) < (Int, Exp)
(Int, Int) < (Exp, Int)
```

With actual argument types of (Int, Int), the signatures (Exp, Int) and (Int, Exp) are both applicable, but neither is applicable to the other.¹

Asymmetric Comparison To avoid these ambiguities when a signature representing runtime argument types has multiple applicable method signatures, we define a total ordering that provides a notion of *more specific*, which we write as \Box :

$$\vec{a} \sqsubset \vec{s} \equiv \exists i \in [1..n] . (a_i < s_i) \land \forall k < i . a_k = s_k$$

The resulting relation is similar to lexicographic ordering on strings: the first element that differs defines the ordering.

Returning to our previous example, when deciding between the two applicable signatures (Exp, Int) and (Int, Exp), our asymmetric relation orders them as follows:

$$(Int, Exp) \sqsubset (Exp, Int)$$

A method signature (Int, Exp) will be chosen over (Exp, Int) when both are applicable, *i.e.*, when the actual argument types are (Int, Int).

We use this relation to model the multiple-dispatch selection that DemeterF uses to eliminate ambiguities and corresponding errors in traversals and function-objects.

5.1.3 Graph Cartesian Products

To help visualize relations over signatures and trees we will use a graph *Cartesian product* (GCP). A GCP, G = (V, E), is defined over a sequence of trees, (T_1, \ldots, T_n) , with each $T_i = (\Sigma_i, \prec_i)$. The vertices, V, of the graph are signatures and the edges, E, are defined by the immediate successor relation on signatures:

$$V = \Sigma_1 \times \dots \times \Sigma_n$$

$$E = \{ (\vec{a}, \vec{c}) \in V \times V \mid \vec{c} \prec \vec{a} \}$$

¹In most statically typed multiple-dispatch systems, *e.g.*, MultiJava [22] and Fortress [8], this results in a compile-time error.

For example, the GCP of the two earlier trees of expressions and cons-lists is shown in figure 5.3. The *root* of the GCP is the signature (Exp, List).

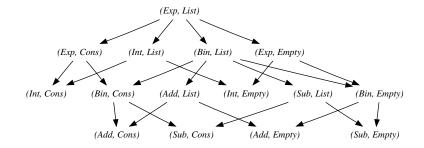


Figure 5.3: Graph Cartesian product rooted at (Exp, List).

Given our definition of a GCP, it can always be characterized as a directed acyclic graph (DAG). Reachability in a GCP is defined by the *applicable* relation on signatures, \leq , and the leaves of a GCP correspond to signatures made entirely of leaves of the corresponding trees:

$$leaves(G) \equiv leaves(T_1) \times \cdots \times leaves(T_n)$$

The leaves of the trees correspond to concrete classes, and the leaves of the GCP correspond to concrete signatures that represent the possible runtime types of arguments passed to methods.

5.1.4 Algorithm Notation

We will present algorithms in a notation similar to the functional programming language Haskell [39], with a C/Java-style calling syntax where the opening parenthesis are placed to the right of the function name and arguments are separated with commas. Our algorithms do not rely on any particular properties of an implementation (*e.g.*, lazy versus strict), just an intuition of its semantics and simple pattern matching forms.

Function Definitions Function definitions will consist of a type signature, followed by a list of equations. As an example, figure 5.4 shows a function that recursively calculates the i^{th} Fibonacci number. The function, fib, is

```
fib :: Int \rightarrow Int
fib(0) = 0
fib(1) = 1
fib(i) = fib(i-1) + fib(i-2)
```

Figure 5.4: Notation Example: Fibonacci.

declared with the type (Int \rightarrow Int): it takes a single integer and returns

an integer. The function is defined by three equations that match argument cases. 0 and 1 used in the argument position of the equations are *patterns* that match corresponding integer literals. The pattern i matches any other integer and binds it to i in the right-hand side of the equation, which proceeds by adding the results of two recursive calls. Variable bindings and uses will be typeset in italics so they are easily distinguishable.

Data Structures We assume datatypes for representing symbols (sym), trees (tree), and signatures (sig). Overloaded versions of previously defined relations and functions, *e.g.*, \prec , \sqsubset , succs, *etc.*, will be used in the right-hand side of equations when needed.

We use Haskell's list notation for type signatures, *e.g.*, [Int] is the type of integer lists, and within function definitions: the empty list is both a pattern and a value, denoted by empty square brackets, [], and a non-empty list with a head of f and a tail of R will be denoted in both patterns and expressions by (f:R).

When necessary we will define custom data structures using an intuitive notation for algebraic datatypes similar to Haskell and ML. Figure 5.5 shows an example data structure representing integer binary search trees, IntBSTs, and functions for inserting an integer into a IntBST, and collecting a list of a IntBST's elements. For simplicity we will refrain from polymorphic user-defined data structures. The type IntBST is defined by a **data** defini-

Figure 5.5: Notation Example: IntBST insertion and elements as a list.

tion with two value constructors, IntNode and IntLeaf, separated by a bar (|). In general any number of constructors can be defined. The constructor IntNode accepts three arguments, an Int and two BSTs, while IntLeaf accepts no arguments. Defined constructors are used as patterns in argument positions and as expressions. The variables within patterns, *e.g.*, *i* and *left*, are bound in the right-hand side of the equation to matching components of the structure. In the definition of insert we make use of an if-expression that decides between the recursive insertion into the *left* or *right* subtrees,

constructing a new IntNode in both cases. The definition of elements uses a helper function, append, and Haskell's infix cons-list syntax, $(d:\cdots)$. If necessary we will provide definitions for more complicated helper functions along with the algorithm(s).

With notation and background in place, we now discuss particular algorithmic problems used in the implementation of DemeterF. Each section in the remainder of this chapter will give a brief background of a problem, a concise description, an algorithmic solution, and one or more implementations including a discussion of running times.

5.2 Method Selection and Dispatch

In DemeterF, the selection of function-object methods during traversal chooses the *most specific* signature based on the runtime types of its arguments. When there is only a single applicable method, this decision can certainly be made statically. If two or more are applicable to similar traversal results then at least some of the method selection decision must be deferred to runtime. This section discusses our selection algorithms for reflective and statically computed method dispatch.

5.2.1 Reflective Selection

Before applying a *combine* method during traversal, the types of actual method arguments are known. The method signatures of the function-object used can be inspected to determine the most specific method that is *applicable* to the actual argument types.

5.2.1.1 The Problem

We describe the DemeterF runtime method selection problem as follows:

Given a non-empty signature, $\vec{c} = (c_0, c_1, \ldots, c_n)$, an implicit sequence of trees (T_0, T_1, \ldots, T_n) such that $c_i \in \text{leaves}(T_i)$, and a set of signatures, $S = \{\vec{s}_1, \ldots, \vec{s}_m\}$, compute the most specific signature, \vec{s}_i , that is applicable to \vec{c} :

$$\texttt{select}(\vec{c}, S) \equiv \vec{a} \in S \, . \, \vec{c} \leq \vec{a} \ \land \ \forall \vec{s} \in S \, . \, \vec{a} = \vec{s} \ \lor \ \vec{a} \sqsubset \vec{s}$$

The set of signatures, S, represents the formal argument types of a functionobject's *combine* methods. The signature \vec{c} represents the types of runtime arguments, with c_0 being the type of the object that was traversed and c_1, \ldots, c_n being the result types of the recursive traversal of the original object's fields.

5.2.1.2 Solution

The definition of the problem admits a direct algorithm shown in figure 5.6. We use this implementation as the definition of function-object dispatch: selecting the most specific applicable signature given runtime argument types. Our implementation is split into two functions. The function select accepts

Figure 5.6: Reflective Selection Algorithm.

a signature, \vec{c} , and a list of signatures, S, and searches for a signature that is applicable to \vec{c} . The first applicable signature is passed to best, which finds the most specific signature applicable to \vec{c} starting with the initial guess, \vec{a} .

5.2.1.3 Running Time

The comparison of signatures using \leq runs in time $O(t \cdot n)$, where t is a bound on the size of the trees and $n = |\vec{c}|$ is the number of arguments. The running time of select is as follows:

```
select(\vec{c}, S) \in O(t \cdot n \cdot |S|)
```

The implementation of select depends on the number of method signatures in the function-object. Each time a dispatch is required the list must be searched, which can dominate the running time of a data structure traversal. Rather than doing a full search we can reorganize signatures based on their argument types and reduce the number of comparisons that must be made at runtime.

5.2.2 Static Selection and Residue

Inefficiencies in select stem from two related issues: (1) the function performs a linear search through the signatures, and (2) it works independently without knowing anything about the context in which a method will be selected. When more information is available about the types of recursive traversals, the number of possibly applicable signatures can be statically reduced and a specialized decision structure can be generated.

5.2.2.1 Related Signatures

Static decisions about signature selection must deal with less information. Given a signature \vec{c} representing the static types of traversal results, it is possible at runtime to select a signature that is applicable to \vec{c} , *i.e.*, $\vec{c} \leq \vec{s}$, but selecting a more specific signature, *i.e.*, $\vec{s} \sqsubset \vec{c}$, is also possible.

Since both situations may occur, we use a broader relation, \bowtie , to describe signatures that might be selected at runtime. We define \bowtie as follows:

 $\vec{s} \bowtie \vec{c} \equiv \vec{s} \le \vec{c} \lor \vec{c} \le \vec{s}$

The signature \vec{c} represents a static approximation of traversal result types and \vec{s} represents a method signature. We call this relation *related*, since it relates two signatures that have components related in the corresponding tree. Signatures \vec{s} and \vec{c} are related if one is applicable to the other, in either order.

5.2.2.2 Residual Dispatch

With more information about the types of values to which signatures will be applied, the set S can be reduced by filtering out unrelated signatures. Because the remaining signatures are related, we can use argument subtype relationships to construct a decision tree that selects the most specific signature using a minimal number of runtime type tests. In many cases a dynamic decision is not required, when there is only one related signature. When the number of related signatures is greater than 1 we refer to the remaining dispatch decision as *residue*.

In the case of DemeterF, type checking a function-class over a data structure statically provides the approximate types of values returned from subtraversals. This can be used to determine the methods that might be applied at each point in the traversal, *i.e.*, related signatures. We use this information to generate data structure specific traversals with inlined dispatch residue to be executed at runtime. The residue takes the form of a decision tree of argument type tests, which is interpreted at runtime using \leq , or instanceof in Java.

5.2.2.3 The Problem

We describe the residual dispatch problem as follows:

Given a non-empty signature, $\vec{c} = (c_0, c_1, \ldots, c_n)$, an implicit sequence of trees (T_0, T_1, \ldots, T_n) such that $c_i \in \Sigma_i$, and a set of signatures, $S = \{\vec{s}_1, \ldots, \vec{s}_m\}$, compute a residual dispatch tree, D, that determines the most specific signature, \vec{a}_i , to be applied to a runtime signature, $\vec{a} \leq \vec{c}$.²

²There may be multiple equivalent dispatch trees corresponding to the given signatures.

The result is decision tree, D, built from two relations, *left* and *right*. Interior nodes of the decision tree are labeled with a pair, (i, t), representing a type test of the i^{th} parameter against the given symbol, t. A node's *left* and *right* children represent subdecisions for a test result of true or false, respectively. The leaves of the decision tree are labeled with signatures from S.

The signatures, S, represent the argument signatures of function-class methods, and \vec{c} represents the static types of expected traversals results for method dispatch. Our dispatch tree, D, represents a decision procedure that performs type/instance tests on the return values of subtraversals, and leaves of the tree describe the selected method's signature.

5.2.2.4 Solution

Our solution to the dispatch residue problem is shown in figure 5.7. A dis-

```
data Dec = IF(Int, sym, Dec, Dec)
             | CALL(sig)
residue :: sig \rightarrow [sig] \rightarrow Dec
residue(\vec{c}, S) = decision(1, \vec{c}, S)
decision :: Int \rightarrow sig \rightarrow [sig] \rightarrow Dec
decision(i, \vec{c}, []) = error
decision(i, \vec{c}, S) =
     if (i > |\vec{c}|) then CALL(select(\vec{c}, S))
     else let A = \operatorname{sort}(\{s_i \mid \vec{s} \in S \land \vec{s} \bowtie \vec{c}\}, <_i)
                   P = [(a_k, [a_1, \ldots, a_{k-1}]) | k \in [1..|A|]]
                   G = [(a, [\vec{s} \in S \mid s_i \bowtie a \land s_i \notin ignr]) \mid (a, ignr) \in A]
             in buildDec(i, c, G)
buildDec :: Int \rightarrow sig \rightarrow [(sym, [sig])] \rightarrow Dec
buildDec(i, \vec{c}, []) = error
buildDec(i, \vec{c}, ((a, S):G)) =
     let d = \text{decision}(i+1, \text{update}(\vec{c}, i, a), S)
     in if null(G) then d
          else IF(i, a, d, buildDec(i, \vec{c}, G))
```

Figure 5.7: Residual Selection Algorithm.

patch decision tree, Dec, is created by one of two value constructors. IF encodes the test of a particular argument position at particular type, and branches to another Dec when the test succeeds or fails. CALL represents a selected signature, once the necessary number arguments have been inspected.

The function residue constructs a Dec beginning with the first argument position, 1, given the static signature \vec{c} and a list of signatures S. If all argument types have been tested ($i > |\vec{c}|$), then the helper function decision

constructs a CALL node using select to determine most specific signature that is still applicable. Otherwise, we construct the set of symbols A from the i^{th} argument types of related signatures from S, sorted according to $<_i$. From A we construct a list of pairs, P, whose left component is the corresponding element of $A(a_i)$, and right component is a list of the previous elements from A. P represents the type to be tested for a given set of methods, and the type tests that will have failed, and so can safely be ignored, reducing useless repetitive tests for unreachable signatures.

Signatures from S are then placed into groups, G, by their i^{th} argument type. Each group consists of a symbol a from a pair in P (in order) and a list of signatures with an i^{th} argument type that is related to a (*i.e.*, $\vec{s} \in S | s_i \bowtie a \dots$), when a is also not in our list of ignored types, *ignr*. The result is a list of pairs with a symbol as their first component and a list of signatures as their second component representing a type test, and the signatures that are still possible if the test should succeed.

In buildDec the groupings are used to recursively construct a chain of decisions for the next argument position. If only one grouping exists, *i.e.*, null(G), then the decision d is returned. If there are more groupings, an IF test for argument i of type a is constructed with d as the true branch, and the rest of the groups decision as a false branch.

5.2.2.5 Running Time

Symbol comparisons, < and \bowtie , take time proportional to t, where t is a bound on the size of the trees. Signature comparisons, \leq and \bowtie , run in time $O(t \cdot n)$, where n is the length of the signature, *i.e.*, $|\vec{c}|$. The worst-case running time of residue is as follows:

residue(
$$\vec{c}$$
, S) $\in O(b^n \cdot (t \cdot n \cdot |S| + t \cdot log(t)))$

The exponential term, t^n , comes from the recursive call to decision from within buildDec, since the bound on the tree size, t, is also a bound on the length of G. The average running time of the algorithm depends on the average branching factor of the trees. If we call this factor b, then running time can be more accurately described as:

residue(
$$ec{c}$$
, S) $\in O\left(b^n \cdot (n \cdot |S| + (|S| \cdot log(|S|)))
ight)$

In most cases this term dominates the running time, since the number of signatures, |S|, is small and the size of A is typically much smaller than |S|. The running time is interesting, but more important is the size of the resulting decision tree. Since the tree will eventually be used to make dynamic selection it should be in some sense minimal. The depth of the Dec produced by residue is at worst:

$$O(t \cdot n)$$

Since we make at most t type tests for each of the n arguments, though this also requires an exponential number of methods. This is a great improvement on the runtime performance of select, which depends on the number of signatures.

5.3 Method Coverage

Multi-method languages and systems like CLOS[66], MultiJava [22], JPred [56], and DemeterF rely on selecting the most specific function for runtime argument types. DemeterF (like CLOS) uses an *asymmetric* multiple dispatch strategy where the leftmost arguments are given precedence. MultiJava and JPred employ a *symmetric* strategy where all arguments are given equal weight, and method ambiguity is not allowed at runtime. In both dispatch styles it is beneficial for the system to statically ensure that certain dispatch errors are not possible, *e.g.*, *message not understood* errors.

For DemeterF this means checking that a function-class contains an applicable signature for all possible sequences of concrete argument types, corresponding to the leaves of the GCP. For example, if a method group has the signature (Exp, List), then it suffices to check that an applicable method exists for each of the concrete combinations:

(Int, Cons) (Add, Cons) (Sub, Cons)
(Int, Empty) (Add, Empty) (Sub, Empty)

We call the task of checking signature coverage the leaf-covering problem.

5.3.1 Definition : LEAF-COVERING

Given a sequence of trees, (T_1, \ldots, T_n) , we say that a set of signatures, *S*, *covers* the trees if *S* contains an applicable signature for each signature made of leaves from each T_i :

$$\begin{array}{l} \texttt{covers}(S,\,(T_1,\,\ldots,\,T_n)) \ \equiv \\ \forall \vec{\ell} \in (\texttt{leaves}(T_1) \times \cdots \times \texttt{leaves}(T_n)) \,.\, \exists \vec{s} \in S \,.\, \vec{\ell} \leq \vec{s} \end{array}$$

Leaf-covering can also be defined in terms of a GCP: the root signature of our trees, *e.g.*, (List, Exp), becomes the root of our GCP. Leaves in the GCP are defined as the vertices of V with *out-degree* of 0:

$$leaves(G) \equiv \{ \vec{v} \in V \mid \forall \vec{u} \in V . (\vec{v}, \vec{u}) \notin E \}$$

The leaves of the GCP are the same as the signatures made up of the leaves from each of the trees, T_i . Given a GCP, the task of covers is to check that each leaf signature of the GCP has an ancestor in S.

5.3.2 LEAF-COVERING is coNP-Complete

Before describing solutions to leaf-covering, we first show that the problem is actually *coNP-Complete*. The problem is in *coNP*: to show that a set of signatures, S, does not cover all leaves we simply provide a leaf that is not covered by S. The witness can easily be chosen non-deterministically and checked in time $O(t \cdot n \cdot |S|)$. Leaf-covering can then be shown to be coNP-Complete by reduction from DNF validity, *i.e.*, *tautology* checking, to leaf-covering.³

Reducing DNF to LEAF-COVERING Consider a formula, *F*, in disjunctive normal form, where each clause consists of literals, $l_{i,j}$, which are either the positive or negative assertion of a *variable*, *e.g.*, *a* or $\neg a$:

$$F \equiv (l_{1,1} \wedge \cdots \wedge l_{1,n_1}) \vee \cdots \vee (l_{m_1} \wedge \cdots \wedge l_{m_n,n_m})$$

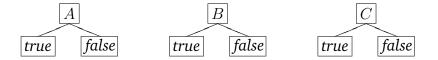
With an ordering on the variables used in F, e.g., alphabetic, we create a sequence of trees with variable names as roots and the special symbols *true* and *false* as leaves. We then encode the clauses of the formula as signatures of S containing a symbol from each of the trees in order. For each clause we encode a positive literal as *true*, a negative literal as *false*, and an unused variable as the root of its corresponding tree.

The cross product of the leaves of the trees (or the set of leaves of the GCP) contains all assignments of *true* and *false* to the variables of F. If the elements of S cover all the leaves, then all *concrete* assignments are covered by the clauses of the formula, meaning F is a tautology. If not, then one of the uncovered leaves represents an assignment that does not satisfy the formula.

As a complete example, consider the following formula:

 $F = (a \land \neg b) \lor (\neg a \land c) \lor (\neg b \land c) \lor (\neg a \land \neg c)$

To convert the validity of this formula into a leaf-covering problem, we order the variables as (a, b, c) and construct three corresponding trees:



The root of our GCP is the triple (A, B, C), and our set *S* encodes the clauses of *F* as triples:

$$S = \{ (true, false, C), (false, B, true), \\ (A, false, true), (false, B, false) \}$$

³Thanks to Yannis Smaragdakis for suggesting and detailing this reduction.

The leaf signatures (*i.e.*, leaves of the GCP) include all triple permutations of *true* and *false*. In this case the signatures, S, constructed from the formula answer in this case is *no*; the leaf signatures that are not covered, (*true*, *true*, *true*) and (*true*, *true*, *false*). The corresponding assignments to a, b, and c respectively do not satisfy F: *i.e.*, F is not valid.

5.3.3 Solutions

In this section we discuss two different solutions to leaf-covering. The first is a simple brute-force approach that directly implements the specification of the problem. The second is a more involved solution that uses tree intersections and counting.

5.3.3.1 Solution 1: Brute-Force

The definition of covers admits a straightforward solution: compute all the possible leaf signatures and check that each leaf, \vec{l} , has an applicable signature: $\exists \vec{s} \in S \ \vec{l} \leq \vec{s}$. The simple brute-force algorithm is show in figure 5.8. We first create the Cartesian-product of the leaves of each of the trees, then

```
covers :: [sig] \rightarrow [tree] \rightarrow Bool

covers(S, T_S) =

let lfs = cross(map(leaves, T_S))

in all(lfs, S)

all :: [sig] \rightarrow [sig] \rightarrow Bool

all([], S) = true

all((\vec{\ell}: lfs), S) = one(S, \vec{l}) \land all(lfs, S)

one :: [sig] \rightarrow sig \rightarrow Bool

one([], \vec{\ell}) = false

one((\vec{s}: S), \vec{\ell}) = \vec{\ell} \leq \vec{s} \lor one(S, \vec{\ell})
```

Figure 5.8: Brute-Force Leaf-Covering Algorithm.

iterate to check that all leaf signatures, $\vec{\ell},$ are covered by at least one signature in S.

Running Time For a set of signatures, S, and a sequence of trees, (T_1, \ldots, T_n) , the algorithm has the following running time:

$$\operatorname{covers}(S, (T_1, \ldots, T_n)) \in O\left(|S| \cdot \prod_{i=1}^n |\operatorname{leaves}(T_i)|\right) = O(|S| \cdot t^n)$$

Where t is a bound on the size of the trees. If a leaf signature is without a corresponding applicable signature in S then it can be used as a witness of incomplete coverage.

This solution runs in time exponential in n, *i.e.*, the number of trees, but for a fixed n the running time becomes polynomial. Problems of this type are termed *fixed-parameter tractable*, as they are only exponential in part of their input. In fact, this solution for the decision problem is polynomial (in |S|) for fixed number of trees.

5.3.3.2 Solution 2: Inclusion-Exclusion

A second solution to leaf-covering involves tree intersection and the inclusionexclusion principle. Taking a close look at the GCP example in figure 5.3 shows that multiple interior vertices have edges that reach a the same leaf signature. This overlap of signatures can be used to calculate the *size* of the union of the leaves covered by S, without having to generate the leaf signatures themselves. This is done by calculating the number of overlapping leaves of two or more signatures and using the set inclusion-exclusion principle to calculate the size of their union.

We begin by defining another version of leaves for a tree given a starting symbol:

$$leaves(T, a) \equiv \{ b \in leaves(T) \mid b \le a \}$$

Which returns the leaves of T that are also successors of a. This function can be used to compute the number of overlapping leaves of a set of signatures, $S = {\vec{s}^1, \ldots, \vec{s}^{|S|}}$, by calculating the product of the sizes of the individual (point-wise) intersections:

$$ext{overlap}(S, (T_1, \ldots, T_n)) \equiv \prod_{i=1}^n \left| igcap_{k=1}^{|S|} ext{leaves}(T_i, s_i^k)
ight|$$

The intersection of leaves is calculated independently using the i^{th} tree and the corresponding elements of each signature, s_i^k .

The total number of leaf signatures in a sequence of trees is the product of the number of leaves in the individual trees:

$$au(T_1, \ldots, T_n) \equiv \prod_{i=1}^n | extsf{leaves}(T_i) |$$

For two signatures, \vec{s} and \vec{a} , determining the number of unique leaf signatures covered can be calculated by adding the total leaves covered by each and subtracting the number of overlapping leaves:

$$\prod_{i=1}^{n} |\operatorname{leaves}(T_i, s_i)| + \prod_{i=1}^{n} |\operatorname{leaves}(T_i, s_i)| - \operatorname{overlap}(\{\vec{s}, \vec{a}\}, (T_1, \dots, T_n))$$

If this result is the same as the total number of leaves then the trees are are fully covered by the two vertices, \vec{s} and \vec{a} . If not, then an uncovered leaf signature must exist.

This provides a way to calculate the size of the union of the covered leaves directly from the number of leaves at the intersection of the signatures. For an arbitrary set of signatures, *S*, the set inclusion-exclusion principle is used to calculate the size of the union of all covered leaves using overlap:

$$\begin{aligned} \texttt{inclu}_\texttt{exclu}(S, (T_1, \dots, T_n)) \\ &\equiv \sum_{S \supseteq M \neq \emptyset} \left[(-1)^{|M|-1} \operatorname{overlap}(M, (T_1, \dots, T_n)) \right] \end{aligned}$$

The complete implementation of covers_{inex} compares the total number of leaves to the number of covered leaf signatures calculated by inclu_exclu:

$$covers_{inex}(S, (T_1, \dots, T_n)) \\ \equiv total(T_1, \dots, T_n) = inclu_exclu(S, (T_1, \dots, T_n))$$

The benefit of this second implementation is that the number of leaves covered by S is calculated over the individual trees, eliminating the need to inspect or construct the leaf signatures.

Running Time The running time of inclu_exclu relies heavily on overlap, which has the following running time:

$$\operatorname{overlap}(S, (T_1, \ldots, T_n)) \in O(t \cdot n \cdot |S|)$$

The calculation of the number of overlapping leaves for a set of signatures is efficient, since individual symbols are compared over a single tree.

The inclusion-exclusion procedure itself runs in time that is exponential in the size of *S*, rather than the number of trees:

$$\texttt{inclu}_\texttt{exclu}(S, (T_1, \dots, T_n)) \in O\left(t \cdot n \cdot \sum_{k=1}^{|S|} \binom{|S|}{k}\right) = O(t \cdot n \cdot 2^{|S|})$$

Where t is again a bound on the size of each tree. The exponential factor, $2^{|S|}$, is in contrast to the brute-force solution, where running time depends on the exponential factor t^n . Determining the best solution depends on the number of signatures versus the number trees (or the length of the signatures), which correspond to the number of methods and the number of method arguments respectively.

5.3.4 Fixed-Parameter Tractability

The running times of the two solutions to leaf-covering we have presented, *i.e.*, covers and covers_{inex}, are not exponential in all of their inputs. Both

algorithms become polynomial when part of their input is of a fixed size. If the trees, (T_1, \ldots, T_n) , are fixed then t^n is bounded by a constant, K_n . The brute-force algorithm's running time becomes:

$$covers(S, (T_1, \ldots, T_n)) \in O(|S| \cdot K_n)$$

If instead the signatures, S, are fixed, then $2^{|S|}$ is bounded by a constant, K_S and the running time of inclu_exclu becomes:

$$\operatorname{inclu}_\operatorname{exclu}(S, (T_1, \ldots, T_n)) \in O(t \cdot n \cdot K_S)$$

In the case of DemeterF, the inclusion-exclusion solution is more attractive since the set of signatures S is fixed while checking a traversal. In particular, we use the same set of signatures (*i.e.*, *combine* method signatures) to solve an instance of the leaf-covering problem for the traversal of each concrete class. Since the number of trees involved, n, (*i.e.*, the maximum number of *combine* arguments) can be different for all leaf-covering instances while type checking, fixing S is more important than fixing n.

5.3.5 Decision Versus Search

The brute-force solution to leaf-covering answers both the decision problem and the search (or *function*) problem. While we check each leaf signature, if the leaf is uncovered then we immediately have a witness.

While the inclusion-exclusion solution provides an answer to the decision problem, it does not immediately produce an uncovered leaf signature. There is a standard, well-known sequence of reductions for NP-complete problems that converts a decision solution into a search solution to decision for [64]. We are also aware of the work of Bellare and Goldwasser [11], which provides a proof and a general algorithm showing that for all NPcomplete problems, search reduces to decision ([10], Theorem 4.5). However, in this section we discuss a more efficient alternative to the standard reduction that uses the inclu_exclu implementation to determine an uncovered leaf signature.

In order to find an uncovered leaf signature, we consider edges of the GCP, represented by our successor relation, \prec . Clearly the signature, \vec{r} , made only of the roots of the trees must cover all leaves:

$$\vec{r} = (r_1, \ldots, r_n)$$
 where $r_i \in \Sigma_i \land \neg \exists a \in \Sigma_i . r_i \prec_i a$

To find an uncovered leaf, $\vec{\ell}$, if it exists, we exploit the fact that S covers fewer leaves than if S included the signature $\vec{\ell}$. In fact, if $\vec{\ell}$ is uncovered, then any predecessor of $\vec{\ell}$ can be combined with S to cover more leaves than just S:

$$\neg \operatorname{covers}(S, (T_1, \dots, T_n)) \implies \forall \vec{s} \,. \, \vec{\ell} \leq \vec{s} \\ \implies \operatorname{inclu_exclu}(S, (T_1, \dots, T_n)) \\ < \operatorname{inclu_exclu}((S \cup \{\vec{s}\}), (T_1, \dots, T_n))) \end{cases}$$

This presents us with an algorithm that uses the immediate successor relationship to explore signatures that will increase the coverage of S until we reach a leaf. Figure 5.9 shows our algorithm that searches for an uncovered leaf using inclu_exclu. We begin by calculating the number of leaves that

```
uncoveredSig :: [tree] \rightarrow [sig] \rightarrow sig

uncoveredSig(Ts, S) =

let sCov = inclu_exclu(S, Ts)

in down(sCov, roots(Ts), S, Ts)

down :: Int \rightarrow sig \rightarrow [sig] \rightarrow [tree] \rightarrow sig

down(mCov, \vec{\ell}, S, Ts) =

let ss = succs(\vec{\ell}, Ts)

in if null(ss) then \vec{\ell}

else across(sCov, ss, S, Ts)

across :: Int \rightarrow [sig] \rightarrow [sig] \rightarrow [tree] \rightarrow sig

across(mCov, [], S, Ts) = error "No Uncovered Leaf"

across(mCov, (\vec{\ell}: ss), S, Ts) =

let cov = inclu_exclu((\vec{\ell}: S), Ts)

in if cov > sCov then down(sCov, \vec{\ell}, S, Ts)

else across(sCov, ss, S, Ts)
```

Figure 5.9: Search for an uncovered leaf using inclu_exclu

S covers. We then start with the signature made up of the roots of our trees, and move down and across, in analogy to the GCP. The function down steps down the GCP to select an uncovered signature from the successors, ss, of $\vec{\ell}$. If the signature has no successors, null(ss), then it is an uncovered leaf. Otherwise, across iterates through the successors to find the first one that, when included with S, covers more leaves. If found, then we can step down the GCP and continue searching. If none of the successors is the ancestor of an uncovered leaf, then S actually covers all leaves, which we signal with an **error**.

Additionally, we can explore until we find a signature that does not overlap with *S*:

$$inclu_exclu((S \cup \{\vec{s}\}), (T_1, \dots, T_n)) = inclu_exclu(S, (T_1, \dots, T_n), S) + inclu_exclu(\{\vec{s}\}, (T_1, \dots, T_n))$$

Which provides us with the first signature that covers only uncovered leaves, *i.e.*, the ancestor of a subset of uncovered leaves, which may prove more helpful to programmers.

5.3.5.1 Running Time

The running time of our search remains polynomial in the running time of $inclu_exclu$, since the maximum number of successors of a given signature is $O(t \cdot n)$: one for each of the immediate successors in each tree. Since t is a bound on the sizes of our trees, it also bounds their depths, so the maximum number of iterations of our search is $O(t^2 \cdot n^2)$. The overall running time of *uncoveredSig* using inclu_exclu becomes:

uncoveredSig $(S, (T_1, \ldots, T_n)) \in O(t^3 \cdot n^3 \cdot 2^{|S|})$

Similar to the inclu_exclu-based decision solution, uncoveredSig is also fixed-parameter tractable. When the set of signatures, S, is fixed we have a running time that is cubic in t and n.

Chapter 6

Performance

The last component of this thesis is that function-objects over data structure traversal perform well. In this chapter we discuss the performance aspects of DemeterF, what features might inhibit performance, and how we solve these issues. We give experimental results that compare our traversal-based approach to other implementation methods.

6.1 Performance Factors

Function-classes in DemeterF-based programs modularize interesting computation. For many traversal-like functions, much of the code in a handwritten implementation is the same as for the corresponding function written using DemeterF, though it is spread throughout different classes and tangled with boilerplate code. Providing an efficient DemeterF-based implementation then reduces to efficiently producing an equivalent replacement for the boilerplate code that one would write by hand. In the case of DemeterF, the handwritten boilerplate corresponds to two particular mechanisms: the recursive traversal of a data structure, and dispatching to an appropriate *combine* method. To increase the performance of DemeterF-based functions we focus on these important aspects.

6.1.1 Traversal

The implementation of adaptive traversal in DemeterF uses Java reflection to dynamically walk a data structure. This involves inspecting the object when it is traversed and discovering its Class. From the class we get the declared fields (transitively) and recursively traversal each of the field values. Other traversal features, *i.e.*, control and contexts, can also add to the inefficiencies since they also require reflection, but there are ways to speed up reflection, like caching the the results according to the Class of the object.

Our main approach to speeding up traversals is to generate inlined code that performs the traversal for a specific function-class, control, and context type. For abstract instances we use **instanceof** checks to select between subclasses. Once the traversal of a concrete instance's fields is complete, the return results of subtraversals are used to select the appropriate *combine* method. With the traversal inlined for a particular function-class, it is then safe to use more specific implementations of dispatch.

6.1.2 Dispatch

As discussed in chapter 5, DemeterF implements two different kinds of dispatch. With our reflective traversal we use a reflective dispatch. When a Traversal is created we also reflectively collect the signatures of *combine* methods in the given function-object. When a *combine* method needs to be called, the method signatures are compared to the recursive result types using an algorithm similar to select, in section 5.2.1.

When a particular function-class and data structure are fixed, we can minimize our method selection by limiting our choices to only the related method signatures and computing a decision tree to select the correct method, similar to our algorithm residue, in section 5.2.2.

6.2 Generating Traversals

One of the major benefits of our separation of function-classes and traversals is that we can provide different (but equivalent) implementations. Our generic traversal can adapt a function-object's *combine* methods to different structures, but we can also replace reflection with static information from a specific CD.

6.2.1 Traversal Inlining

Similar to our generative descriptions in section 2.7, we describe our traversal generation using a template, which is shown in listing 6.1. As expected,

```
class Traversal{
  FC fobj;
  Traversal(FC f){ fobj = f; }
  // Generate traversal methods
  \forall A \in CD.GenTrav(A)
  \forall C \in CD.GenTrav(C)
}
```

Listing 6.1: Traversal generation template

the generated Traversal class accepts a function-object. Though only concrete classes exist at runtime, the body of the Traversal requires the CD's abstract definitions in order to decide between subclasses. Our traversal generation rule, GENTRAV, is shown below. First for abstract, then concrete definitions.

```
 \begin{array}{l} \operatorname{GenTRAV}(A=T_1\mid\cdots\mid T_n) \rightsquigarrow \\ R \ traverse < R > (A \ h) \{ \\ \quad \text{if (h instance of } T_1) \ \text{return this.} < R > traverse((T_1) \ h); \\ \quad \cdots \\ \quad \text{if (h instance of } T_n) \ \text{return this.} < R > traverse((T_n) \ h); \\ \quad \text{throw new Exception("Unknown } A \ \text{Subtype"}); \\ \} \end{array}
```

For abstract classes we create a simple chain of **if** statements that selects the appropriate recursive traverse method for the given instance.¹ In order for the Traversal to work with different function-classes/objects, we parametrize each traversal method with the return type, R. For abstract types the parameter is carries through to recursive calls.

The generation rule for concrete definitions is bit more complex:

```
 \begin{array}{l} \operatorname{GenTRAV}(\ C = \langle f_1 \rangle \ T_1 \ \cdots \ \langle f_n \rangle \ T_n \ ) \ \rightsquigarrow \\ R \ traverse \left( C \ \_h \right) \{ \\ \quad \operatorname{Object} \ f_1 \ = \ \texttt{this} . < \operatorname{Object} > traverse \left( \_h . f_1 \right); \\ \quad \cdots \\ \quad \operatorname{Object} \ f_n \ = \ \texttt{this} . < \operatorname{Object} > traverse \left( \_h . f_n \right); \\ \quad \texttt{return this} . < R > apply (\operatorname{fobj}, \operatorname{new Object}[] \{\_h, f_1, \ldots, f_n\}); \\ \} \end{array}
```

For each of a class' fields we recursively call traverse and store the result in a local variable. Since our traversal can be used with any function-object, we assume nothing about the return types by using **object**. Once all the instance's fields have been traversed we apply our function object, fobj, to an array of the results including the original object as its first element. The elided apply determines the types of the arguments and dynamically dispatches to fobj's most specific *combine* method. In our dynamic implementation we use Java reflection to implement both the selection and application of *combine* methods.² For function-classes that have several *combine* methods, this leaves much room for improvement.

¹Java will statically resolve the overloaded traverse calls because of casting.

²We use the method Class.isAssignableFrom(...) to compare the types of the formal and actual *combine* arguments, and Method.invoke(...) to call the chosen method.

6.2.2 Dispatch Inlining

When we specialize a traversal for a particular function-class, we can replace Object in our generated traversals, and apply with a calculated decision tree. For our BExp structures and Simplify function-class from section 2.5, listing 6.2 shows the generated traversal method with inlined dispatch for the Neg class. The method first recursively calls the general BExp traversal

```
BExp traverse(Neg _h){
   BExp inner = traverse(_h.inner);
   if(inner instanceof Neg)
      return fobj.combine(_h, (Neg)inner);
   else
      if(inner instanceof False)
        return fobj.combine(_h, (False)inner);
      else
        if(inner instanceof True)
        return fobj.combine(_h, (True)inner);
      else
        return fobj.combine(_h, inner);
}
```

Listing 6.2: Simplify traversal method for Neg

method on the instance's inner field, then proceeds to select the appropriate method based on the type of the recursive result.

Note that only the four *combine* methods (from listing 2.17) that could possibly apply to a Neg instance could be called. If all the tests fail, then the method with the most general signature, (Neg, BExp) is called. We also note that the declared type of the local variable, inner, matches the least upper bound of the return of the possible methods.

When mutual recursion is involved, the situation is similar, though the return types of recursive results will likely be different. Listing 6.3 shows the merged traversal method and dispatch for Let. In this case, the recur-

```
BExp traverse(Let _h){
  Bind _bind = traverse(_h.bind);
  BExp _body = traverse(_h.body);
  if(_body instanceof Lit)
    return func.combine(_h, _bind, (Lit)_body);
  else
    return func.combine(_h, _bind, _body);
}
```

Listing 6.3: Simplify traversal method for Let

sive traversals return different types of results, since Bind and BExp are not related by subtyping. The dispatch only requires a single test, since the third argument, _body, is the only difference between the two possible *code* methods from Simplify.

6.2.3 Parallel Traversal

The main benefit of separating traversals and function-objects is that we can replace our traversal without changing the results. The benefit of purely functional (*e.g.*, side-effect free) traversal-based functions is that the order in which subcomponents are traversed is irrelevant to the final result. When it may improve the performance of a particular traversal, we can also perform subtraversals in separate threads. We do this by generating a subclass of thread to perform a particular traversal in a separate thread, providing a service similar to MultiLisp's future annotation [32].

Listing 6.4 shows an **interface** Result that represents a subtraversal result of the type R. We use this interface to implement a *possibly* parallel

```
interface Result<R>{
    R result();
}
```

Listing 6.4: Traversal result interface

traversal with classes that perform a pending subtraversal either immediately, or in a separate thread.

Listing 6.5 shows ParTrav, a thread subclass that is used to implement a separate (parallel) subtraversal. ParTrav is also parametrized by the sub-

```
abstract class ParTrav<R> extends Thread implements Result<R>{
    R res = null;
    ParTrav(Traversal t){ this.start(); }
    abstract R traverse();
    public void run(){ setRes(traverse()); }
    synchronized void setRes(R r){ res = r; this.notify(); }
    synchronized R result(){
        if(res == null)this.wait();
        return res;
    }
}
```

Listing 6.5: Synchronized parallel traversal

traversal return type, and has an **abstract** method, traverse, that is responsible for executing the subtraversal. When a ParTrav instance is created, it immediately starts itself. The Java runtime will eventually begin executing the run method, which will execute the traversal and store the result in the local variable res.

For single-threaded traversals we use a simple Result implementation that wraps the subtraversal value. Listing 6.6 shows a simple class, Trav that is used to unify Results for sequential traversals. When a sequential

```
class Trav<R> implements Result<R>{
    R res;
    Trav(R r){ res = r; }
    R result(){ return res; }
}
```

Listing 6.6: Sequential traversal wrapper

traversal is performed we execute the traversal immediately and store it in a Trav instance.

In order to execute only specific subtraversals in parallel, we introduce an integer weight parameter to every traverse method. When a threshold is reached we create new ParTrav threads for subtraversals with a traverse that performs the field's subtraversal. If the threshold is not reached, then a sequential Trav is created to hold the result after it is immediately traversed. The result methods are used during instance checks for dispatch.

Listing 6.7 shows the generated traversal method for And that traverses an instance's left and right fields in different threads. We first create a

```
BExp traverse(And _h, int weight){
   final Traversal trav = this;
   Result < BExp > left = ((weight != THRESHOLD)?
       new Trav<BExp>(traverse(_h.left, weight+1)):
       new ParTrav < BExp >() {
         BExp traverse()
         { return trav.traverse(_h.left, weight+1); }
       }):
   Result < BExp > right = ((weight != THRESHOLD)?
       new Trav<BExp>(traverse(_h.right, weight+1)):
       new ParTrav <BExp >() {
        BExp traverse()
         { return trav.traverse(_h.right, weight+1); }
       });
   if(left.result() instanceof False)
   /*... The rest of dispatch ...*/
}
```

Listing 6.7: Parallel traversal method for And

final local variable, trav, which can be referenced from within our **new** anonymous classes. For each field we either create a Trav storing the sequential traversal result, or an anonymous subclass of ParTrav that implements the traverse method by calling the recursive traversal, trav, when the thread is eventually run. After the wrappers have been created, we begin dispatch by calling the result methods of the Results, which will either immediately return a result, or wait for the subtraversal to complete. In our inlined implementations we replace the local Traversal with the spe-

cific traversal we are implementing. In this way we can limit the number of threads created, but at the expense of a bit of extra allocation.

6.3 Experiments and Results

The rest of this chapter presents and discusses a performance comparison and results. We compare DemeterF-based implementations of our BExp functions to visitor and handwritten versions. Since DemeterF is implemented in DemeterF, we also compare different traversal implementations of our class generator for relative performance results.

All experiments were conducted on a Dell Optiplex GX 970 running Ubuntu Linux with two Intel Core 2 Duo 3 Ghz CPUs and 4 Gb of memory. We used Java OpenJDK Runtime (IcedTea6 1.6.1), gave each Java process 35 Mb of heap space (*i.e.*, "-Xms35M"), and disabled class garbage collection (*i.e.*, "-Xnoclassgc").

6.3.1 Boolean Expressions

In order to demonstrate the performance of traversal-based implementations using function-objects, we implemented functions from chapter 2 by hand and using visitors. The handwritten functions are in object-oriented style (*i.e.*, similar to listing 1.2). The visitors are functional, similar to those illustrated in section 1.3.2.1, but with traversal implemented in the visitor methods instead of the structures. DemeterF-based implementations use the same function-classes implemented in chapter 2 using a number of different traversals.

table 6.1 shows performance results for the first four of our seven BExp functions. Each sub-table contains the average timing results of 10 different runs. We called the given function 15 times on a large BExp instance, calling Java's garbage-collection (System.gc()) between each execution. The columns give (1) the implementation used, (2) the time in milliseconds (microseconds for Eval), and (3) the slowdown compared to handwritten methods, *i.e.*, (*time / handwritten-time*). Note that a slowdown of less than 1 is actually a *speedup*.

'Hand' stands for handwritten, 'Visitor' is a functional visitor solution with traversal implemented within the visit methods, 'Inline' is DemeterF inlined traversal and dispatch (*i.e.*, residue from figure 5.7), and 'Static Trv' is DemeterF inlined traversal with a dynamic dispatch (*i.e.*, select from figure 5.6).

Results for ToString are relatively even for all implementations, presumably because the concatenation of strings accounts for most of the running time. This is a good example for when the task to be performed by the function is more time consuming than the data structure traversal. DemeterF inlining does slightly better on average in this situation, since we can in-

ToString				StrictEval			
Hand	472 msec	1.00		Hand	832 msec	1.00	
Visitor	482 msec	1.02		Visitor	812 msec	.97	
Inline	449 msec	.95		Inline	865 msec	1.04	
Static Trv	1224 msec	2.60		Static Trv	29367 msec	35.34	
Eval				NegNormalize			
Hand	14209 μ sec	1.00		Hand	170 msec	1.00	
Visitor	19866 μ sec	1.39		Visitor	192 msec	1.13	
Inline	42230 μsec	2.97		Inline	222 msec	1.30	
Static Trv	598767 μ sec	42.14		Static Trv	23162 msec	136.25	

Table 6.1: Performance results for BExp functions (1)

line some *combine* selections rather than calling another traverse method (*e.g.*, selection for Lit can be moved one level up, since neither True nor False require subtraversals). In the handwritten and visitor solutions the leaf methods must be called separately, *e.g.*, t.accept(this), in order to differentiate instances.

StrictEval is a good test of both traversal and dispatch. Since the functionality done at each node is relatively simple, it is mainly the data structure traversal and case differentiation that are stressed, which is evident in the StaticTrv result. The visitor solution performs a bit better, presumably due to locality, and DemeterF inline. It is worth noting that the BExp instance used for StrictEval and Eval is extremely large³, so this represents a reasonable worst case for all implementations.

Eval, on the other hand, represents a best case for handwritten and visitor-based traversals, since the short-cutting recursive case can be caught inline. The DemeterF implementations must dispatch to a method in order to decide whether or not to continue. This increases the stack, in many cases doubling it, and can interfere with garbage collection, which accounts for the near 3 times slowdown. Inline generates a traversal with inlined control (*i.e.*, no tests), but StaticTrv has the additional burden of dynamically checking for bypassing fields.

NegNormalize exercises method arguments, traversal, and dispatch. The DemeterF implementations dispatch to both *combine* and update methods, which is evident in the StaticTrv case's poor performance. Visitor and DemeterF Inline implementations are a bit slower than handwritten, but within

³The BExp in the file is over 15Mb of text, and takes a few seconds to parse.

30%. The *combine* and update selections perform reasonably well, though not as well as single and double dispatch in the handwritten methods and visitors.

table 6.2 shows performance results for the rest of our BExp functions in the same format. Simplify is similar in functionality to NegNormalize, with-

Simplify					
Hand	250 msec	1.00			
Visitor	213 msec	.85			
Inline	198 msec	.79			
Static Trv	9195 msec	36.78			

UsedVars				
Hand	2372 msec	1.00		
Visitor	2427 msec	1.02		
Inline	2536 msec	1.06		
Static Trv	13069 msec	5.51		

Invert					
Hand	202 msec	1.00			
Visitor	160 msec	.79			
Inline	194 msec	.96			
Static Trv	9807 msec	48.55			

Table 6.2: Performance results for BExp functions (2)

out the need to pass and update traversal arguments (*i.e.*, context). The Visitor and DemeterF Inline implementations consistently perform better than handwritten functions on this task, though not overly so. The Visitor improvement is, again, likely due to locality. The performance of the DemeterF inlined version is due to the simpler *combine* method selection for Neg and Let, which require minimal instance checks rather than multiple method calls.

The results of UsedVars is similar to ToString, with most of the work being done in the methods, rather than exercising the data structure traversal. In each of the implementations for binary cases (e.g., And and Or) we must compute the union of two Sets. The DemeterF inlined version suffers a bit from the extra generality of its fold method. The calls to fold in the TU *combine* methods for And, Or, Bind, and Let account for the slight slowdown. The StaticTrv implementation is slower due to the number of *combine* methods in the function-class, which are eventually passed to an implementation of select (figure 5.6).

Summary The results above show that the performance of Inlined DemeterFbased functions is competitive with handwritten functions in Java. If we disregard the results for Eval due to its short running time, then we see that DemeterF inlined versions have a maximum slowdown of 30% (NegNormalize), and a maximum speedup of 21% (Simplify). As could be guessed, traversal-based implementations seem to perform best when the functionality itself requires some work, which helps reduce the ratio of traversal to computation and seems to reduce the effect of code locality on execution.

6.3.1.1 Parallel Traversals

To gauge the feasibility of parallel traversals using function-objects we ran separate tests comparing our implementations using generated multi-threaded traversals. table 6.3 shows a comparison of handwritten implementations (as before) with multi-threaded traversals for each of our BExp functions. The first column of the table is the function name, *e.g.*, ToString, and the

Function	Hand	1-Thd	SD-Hand	3-Thd	SD-Hand	SD-1-Thd
ToString	472	486	1.03	405	.86	.83
StrictEval	832	1697	2.04	1272	1.53	.75
Eval	14.2	32.7	2.30	149.4	10.51	4.57
NegNormalize	170	294	1.73	278	1.63	.95
Simplify	250	272	1.09	195	.78	.72
UsedVars	2372	2680	1.13	1731	.73	.65
Invert	202	268	1.33	254	1.26	.95

Table 6.3: Parallel performance results for BExp functions

second is the time for the handwritten Java implementation in milliseconds, the same as the first columns of tables 6.1 and 6.2. The third and fourth columns, *1-Thd* and *SD-Hand*, are the execution times for our multi-threaded traversal using a single thread, and its slowdown with respect to the handwritten version respectively. The last three columns are execution times for multi-threaded traversal with 3 threads (1 master, 2 slaves) and its slowdown as compared to handwritten implementations and the single thread versions respectively.

Our single-threaded version is relatively competitive with the handwritten implementations. The slowdown in the first *SD-Hand* column is the result of keeping track of our threshold/weight parameter and wrapping the sequential traversal results in a Trav instance, as in listing 6.7. Constant factor slowdowns of up to 2.3 is reasonable, considering the extra allocations to wrap almost all recursive subtraversals.

In the final three columns we see the different functions that are most amenable to multi-threading in this manner. Most of the *3-Thd* implementations improve on the *1-Thd* case. In particular, multi-threaded ToString, Simplify, and UsedVars versions *improve* on both the handwritten and *1*-*Trd* implementations. The functions improve handwritten implementations by 14%, 22%, and 27% while speeding up the single-thread case by 17%, 27%, and 35% respectively.

These examples show that the functions that perform the most work within their *combine* methods are the easiest to improve, though Java allocation can become a multi-threading bottleneck. Eval is an extreme case where the function is inherently sequential, and as such does not perform well with multiple threads. The Eval function itself takes such little time to complete that it's difficult for other implementations to compete, especially when extra allocations are involved.

6.3.2 DemeterF

As a final case study, in this section we discuss the performance of different components of the DemeterF class generator using different traversal implementations. As the application is too large to rewrite by hand, we compare the execution of three traversal implementations using identical functionobjects for each of the class generator's components shown in figure 4.1.

6.3.2.1 DemFGen CD Structures

Because DemeterF is implemented using the DemeterF class generator, it serves as a reasonably-sized test case for the class generator. The implementation consists of about 100 generated classes in different packages and is still one of the larger applications built using the traversal library. Table 6.4 shows results comparing running the DemeterF class generator on

	Checks	DGPs	ParseGen	ClassGen	Total
Static Trv	194.5 ms	216.5 ms	78.4 ms	151.1 ms	755.8 ms
Inline	4.31	1.39	1.62	1.45	1.64
Parallel	4.36	1.38	1.44	1.39	1.60
Par/Inln	1.01	0.99	0.89	0.96	0.97

 Table 6.4:
 DemeterF performance (speedup) generating DemeterF structures

the DemeterF CD/BEH files using different traversal implementations. The numbers represent an average of 15 runs of the generator, again on a Dell Optiplex GX 970 running Ubuntu Linux with two Intel Core 2 Duo 3 Ghz CPUs and 4 Gb of memory using Java OpenJDK Runtime (IcedTea6 1.6.1).

The columns represent the different components of the class generator (*c.f.*, figure 4.1) followed by the Total, and the first three rows represent

different traversal implementations. The first row, 'Static Trv', gives timings for each of the generator components and the total time (in milliseconds) using a static traversal with reflective dispatch. The next two rows, 'Inline' and 'Parallel', show *speedup* for inlined dispatch and parallel traversals (respectively) relative to the static traversal. The last row, 'Par/Inln', shows the speedup of the parallel traversal relative to the inlined version. Note that in this table higher numbers are better.

The results show that inlining dispatch within the DemeterF implementation greatly improves the performance. The Checks traversal in particular performs less work than the others, so the speedup is more pronounced (more than 4 times faster). The others show similar improvements (38 to 64%) but the performance of our naive implementation does not improve on the initial results of inlining. Determining the cause and improving parallel results is a item of future work.

6.3.2.2 .NET CLI Abstract Syntax

As a larger test case, we translated structures representing the Microsoft .NET Common Intermediate Language (CIL) specification into DemeterF CD/BEH files, resulting in approximately 500 generated classes. Table 6.5 shows results of generating classes using DemeterF, again comparing static

	Checks	DGPs	ParseGen	ClassGen	Total
Static Trv	484.1 ms	494.4 ms	313.4 ms	417.4 ms	1958.4 ms
Inline	3.95	0.82	1.28	1.09	1.28
Parallel	3.95	0.79	1.32	1.11	1.27
Par/Inln	1	0.96	1.03	1.02	0.99

Table 6.5: DemeterF performance (speedup) generating .NET CIL structures

traversal with dynamic dispatch, 'Static Trv', to inlined and parallel traversals.

The checking phase again performs much better with the inlined and parallel traversals (almost 4 times as fast), and the others do relatively well. The slowdown in the DGP case is due to code locality and other factors that we could not determine. Because the CD structures and function-classes are large we get an overall effect of 28% speedup when inlining both traversals and dispatch. As before the parallel performance is disappointing, but our earlier numbers (from section 6.3.1) look more promising.

Chapter 7

Related Work

7.1 Demeter Tools and Generators

Adaptive (Object-Oriented) Programming (AP) [52] combines datatype descriptions with a domain specific language that selects specific paths of an object instance, over which an imperative visitor is executed. The two major Java implementations of adaptive programming, DJ [62] and DemeterJ [67], are similar to DemeterF's dynamic/reflective and static/generated (inlined) traversals, respectively. DemeterJ uses a similar class dictionary syntax to generate Java classes, a parser, and various default visitors. Ideas from both DemeterJ and DJ have flown into the design of DemeterF, but with a purely functional flavor.

DemeterF improves on those tools with safe traversals, extensive support for generics, improved parser generation, and customizable datatypegeneric function-class generation. The functional nature of DemeterF was chosen to improve the clarity of function-classed and solutions, and to allow different parallel traversal implementations to be freely substituted. One of the major limitations of DemeterF, as compared to DemeterJ, is its simple traversal control and lack of language and tool integration. Traversal control is constructed from simpler *bypass* declarations rather than DemeterJ's from/to notation, and function-classes are not part of our BEH syntax. On the other hand, in some cases this also makes solutions more modular and improves generated traversals and development time, since our class and traversal generators are less complicated and have fewer dependencies.

XML-based generational tools like JAXB [6], XMLBeans [4], and Eclipse Modeling Framework (EMF) [5] can also be used to generate Java classes and XML parsers from data structure *schemas*. The design of the generated classes attempts to enforce good programming practices by forcing the use of factory classes and separating class implementations from interfaces. However, the tools have very little support for other generic or generative features and do not support any notion of parametrized structures. EMF has other features that allow programmers to annotate Java source files, rather than writing XML schemas and more generator-based options, but suffers from the same limitations. The DemeterF class generator is far superior in its support for parametrized structures and generic programming. It can be extended with DGP generation classes that provide syntax (input and output) in XML formats.¹ Factory classes and other features are rather simple to add to DemeterF, but since it has been designed with a smaller scale in mind than most XMLbased tools, this makes it somewhat difficult to coordinate class generation across very large teams within more complex projects.

Parser generators like JavaCC [3] and ANTLR [2] have built in support for generating code for tree-based traversals. JavaCC includes a tool JJTree that provides support for writing automatic visitor methods, and ANTLR provides similar functionality with *tree parsers*. Dispatching on the types of nodes is limited in these systems and typically must be done by the client code in an ad hoc manner. In contrast the design of DemeterF fully integrates traversal-based programming with function-object dispatch, though our support for parsing is (in general) limited to simple LL(k) grammars. Our support for DGP and parametrized structures at a high level allows programmers to focus on functionality, rather than the particulars of parsing and printing. There are features of JavaCC and ANTLR that correspond to some combination of data structures and parsing, but being specialized tools they provide much more flexible support for implementing customized parsers.

7.2 Visitors and Multi-methods

The visitor pattern [27] is most commonly used in object-oriented languages to implement functions over datatypes without requiring instance checks or casts. Typical implementations employ double dispatch as shown in chapter 1, though reflection has also been used [63, 62]. The visitor pattern has a sound type-theoretic background [15, 69], and has been at the center of discussions of extensible functions [43] and the expression problem [68, 61, 60]. There is an opinion that multi-methods [22, 20] eliminate the need for the visitor pattern, but visitors can still be used to abstract traversal code, similar to the Walkabout [63] and Runabout [31] visitors. DemeterF employs multiple dispatch to support both case abstraction and specialization within function-objects, which is not possible with traditional visitors. Our use of multiple dispatch in many ways gives us the best of both worlds (*i.e.*, mutiple-dispatch and visitors), while eliminating the boilerplate code associated with traversals.

Though we are not particularly focused on extensibility in this dissertation, DemeterF does provide support for function and data structure extensibility (particularly using our dynamic/reflective traversal). However, our type checking is not modular in the traditional sense of independent compi-

¹XML-based printing functions are already included in the standard DemeterF distribution.

lation, though it is related to work on static checking of multi-methods [57], where Millstien and Chambers are concerned with balancing modularity and expressiveness. They also focus on eliminating problems associated with multi-method overloading and subclassing across modules. The result places limitations on method and class hierarchy extensions that permit more modular type checking. The DemeterF type checker and inliner both checks and generates code for a particular traversal. Some of the ideas from multi-methods could be integrated into the build process, but the separate and external nature of function-classes means that class extensions may break previously safe traversals. This could be somewhat avoided by tightening our coverage checking, but we have chosen to provide programmers with more flexibility at the expense of a more global compilation scheme.

Agrawal *et al.* [7] focus on a simple model of dynamic dispatch and reduce the type checking problem to (1) checking the consistency of overlapping signatures, and (2) confirming that call sites are correct. Chambers and Leavens [21] eliminate overloading ambiguities by requiring that every combination of argument types have a *most specific* method signature to dispatch to. Their goal is to catch such errors at compile-time, rather than raising a runtime *method ambiguous* exception. Our type system succinctly (and formally) solves many of the same problems, though each of these projects contains useful ideas that could be applied to DemeterF in order to improve modularity and independence of type checking and traversal generation.

DemeterF dispatch is more like CLOS [66], in that we have an implicit total ordering of applicable method signatures. Our dispatch strategy has been chosen to avoid ambiguities, since we are more interested in the possible return types during traversal using an instance of a given function-class, and making sure that every case has an applicable function.

7.3 Generic and Strategic Programming

Our view of generic programming is influenced by many different projects ranging from generalized folds [65, 55], light-weight functional approaches [45, 46, 48], and visitors [43, 61] to full-fledged generic programming [38, 34], attribute grammars [42], and multi-methods [21, 7].

The notion of traversals that we use is closest to Sheard and Fegaras' work on generalized folds [65], drawing inspiration from Meijer *et al.* [55]. Though these papers mostly provide a blueprint for modeling folds, our traversal function is similar to Sheard's implementation of fold, though we group functions into a class/object, rather than passing them as argument tuples. In each case our single traverse function takes the place of a number of very complex functions, one for each value constructor. The benefits of a single traversal function become more apparent when dealing with mutually-recursive types, where fold functions can become difficult to manage. Rather than fixing calls to a particular function argument, our type-

based dispatch allows function-classes to abstract multiple cases into one *combine* method, or overload a case based on argument types.

More heavy-weight generic programming systems [54, 38] can be used to write general traversal functions for data structures of different shapes, but the level at which functions are written (*e.g.*, over a universal datatype) makes it difficult to integrate higher-level notions like traversal contexts and control. While DemeterF cannot provide all the flexibility of functions over a universal datatype, the library and code generation approaches of DemeterF provide significantly more flexibility in traversal implementations and typing. This does, however, require us to formulate soundness separately. This is partly because of our chosen implementation language, but also because we wish to provide other features, like function-class extension and multiple dispatch. We regain some (but not all) of these features through function-class generation.

Library and combinator approaches by Lämmel *et al.* [46, 45] and the *Scrap Your Boilerplate* (SYB) series of papers [48, 49, 50] support solutions to similar problems using traversal combinators and Haskell's type classes [39]. These approaches focus on two typical traversal cases: type-preserving and type-unifying functions. The base function-classes TU and TP in DemeterF perform a very similar role, though being classes, they can be extended more easily. When the typical *everywhere* traversal is not sufficient, recursion is controlled using a one-step traversal that stops at particular types. Type safety is provided by definition within their implementation language, typically Haskell. While DemeterF provides more complex features (including traversal control), the flexibility of our multiple dispatch requires an external type checker.

Strategic programming (SP) [47, 44] extends combinator approaches by using a set of basic, composable strategies to build reusable traversal schemes. Lämmel *et al.* [51] provides a good overview and comparison to AP traversal "*strategies*". While both SP and AP benefit from reusable strategy components, SP provides different forms of control that enable shortcutting and transformation ordering, while AP supports a more goal-based (or *milestone*) approach. The strategic approach has also been extended to composable visitors [70], where visitors take the place of basic strategy combinators, and are used to do in-place transformations using side-effects.

In DemeterF we have adopted a simple form of AP strategies that is less goal-based. We use a simple *bypass* ing form that allows the traversal to be short-cutting, but eliminates the need for a traversal automaton to track milestones. Our style of function-classes may fit nicely with using strategy combinators to define a traversal scheme, since our multiple dispatch is relatively independent of our traversal definition, though our current approach is more an extension of folds than strategy combinators. In practice we use very few complex instances of traversal control. For example, in the implementation of the DemeterF class generator control is mostly used to improve performance.

7.4 Attribute Grammars

DemeterF traversals, function-classes, and contexts are similar to an implementation of *attribute grammars* [42]. In Knuth's original description, each attribute is defined by functions over the productions of a context free grammar. In DemeterF CDs, **abstract** and *concrete* definitions are similar to non-terminals of a context free grammar. In DemeterF, traversing a data structure instance using a function-object corresponds to the evaluation of an attribute's functions over a derivation of the grammar.

The *combine* methods of a function-class correspond to a *synthesized* attribute, with contexts corresponding to an *inherited* attribute. Knuth mentions that attribute grammars can be used to compute arbitrary functions over a derivation of a grammar, and later papers discuss the complexity of checking attribute dependencies and evaluating functions [25]. In DemeterF functions can can be arbitrarily complex, but function-objects without hand-coded recursion correspond to *one-pass* (or *one-visit*) attribute grammars, that can be evaluated left-to-right in a single traversal [13]. Our traversal control also allows the application of functions to be limited to a particular portion of the data structure (or grammar derivation), though it may be possible, albeit very complex, to encode similar ideas within attribute functions. DemeterF can be seen as a more useful high-level implementation of single-pass attribute grammar ideas in Java, and DemeterF-based functions.

7.5 Language Models

Our model, type system, and soundness builds on simpler ideas from an earlier paper [17], with a much more detailed account in [18], and our approach has been influenced by work on aspect-oriented semantics [72]. Our type system has drawn from ideas presented in Featherweight Java (FJ) [37], though we delegate more responsibility to the implementation of our type system, in order to provide more flexibility to the programmer. Our model is relatively simple as compared to FJ and other models of Java [26] in order to capture the essence of the interaction of traversals and multiple dispatch.

Though we maintain a functional approach, our original motivations for separating traversal from other concerns stems from adaptive programming [52] and other visitor-based approaches [43, 69, 70]. More recent functional visitor approaches [61, 60] have focused on safety and modularization, but can be mainly categorized as design patterns whereas our aim is to provide a useful library and tools for writing flexible and generic traversal-based functions.

CHAPTER 8

Conclusions

The development of complex software requires the implementation of complex operations over recursively defined data structures. Complex data structures lead to an increase of boilerplate code dealing with structure access and navigation, which makes programs tedious to develop, difficult to maintain, prone to errors, and entangles important functionality resulting in a loss of clarity. This dissertation has proposed a new approach to developing structure-based functions. It is my thesis that this approach is useful, safe, and performs well.

8.1 Contributions

In support of this thesis I have developed DemeterF, a Java-based library and set of tools for writing traversal-based functions. The system supports the development of function-classes, facilities for generic programming, a type checker, and generative tools for better traversal performance.

The flexibility of function-objects over traversals, asymmetric multiple dispatch, removal of boilerplate code, and generic programming possibilities make our approach extremely useful for writing functions over data structures, both large and small. DemeterF traversals adapt function-objects to a data structure in order to implement deep, flexible folds. A single function-class/object can handle multiple and mutually-recursive structures, and can return results with limited restrictions.

DemeterF's type system and type checker allow functions and data structures to be proven free from dispatch errors, making programs safe. The type checker calculates the return types of a traversal with a specific functionclass. It uses a notion of method signature coverage to prove that our multiple dispatch algorithm will succeed for possible recursive return values.

The types of function-classes and traversals can be used to generate traversals for a specific data structure and function-class. We use the structures to generate traversal methods that implement efficient structural recursion. Where the traversal must call to the function-object, we a inline residue decision that implements our multiple dispatch. Because our approach is side-effect free, generated subtraversals can be executed in parallel. Altogether, we can replace reflective traversals with implementations that in many cases perform as well as handwritten Java functions.

8.2 Future Work

The DemeterF system is relatively complete and has been used in several courses at Northeastern, but there are several extensions and improvements for the future.

8.2.1 Improve Usability

While the DemeterF tools for generic programming and traversal generation have been used to implement DemeterF, there are some parts that are not quite ready for novice end users. In particular the generation of datatype-generic programming (DGP) functions and traversals could be integrated into the CD/BEH languages to allow clients to create traversals as part of the generated classes.¹ We have begun adding syntax to describe the DGP functions to be created for the classes defined in a CD, but the implementation requires a little more work to integrate them fully.

8.2.2 Language Implementation of AP-F

While implementing function-classes and traversals makes them portable, some features (namely traversal control and contexts) reveal our implementation to the client programmer. Implementing a language for DemeterF programs would allow us to integrate features directly and generate safe code, without relying on knowledgeable clients. A complete implementation could also improve performance and enforce side-effect free function-classes and data structures.

8.2.3 Type System Enhancements

The only notable DemeterF features missing from out AP-F model are traversal control and contexts. Finding a way to integrate them into a model would give us a more complete type system and more realistic (though probably messy) proof of type soundness. A statement of type soundness has been absent from Adaptive Programming, and describing soundness in a functional setting would certainly take us a step closer in that direction.

¹DGP functions are currently given as a command line argument, and loaded on demand. Traversals are described by a separate command and file format.

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