

CS4410 : Spring 2013

Simple Code Generation

Code Generation

- Next PS: Map Fish code to MIPS code
- Issues:
 - eliminating compound expressions
 - eliminating variables
 - encoding conditionals, short-circuits, loops

Source

```
type exp =  
  Var of var  
| Int of int  
| Binop of exp * binop * exp  
| Not of exp  
| Or of exp * exp  
| And of exp * exp  
| Assign of var * exp
```

Target: MIPS

```
type label = string
```

```
type reg =
```

```
  R0 | R1 | R2 | ... | R31
```

```
type operand =
```

```
  Reg of reg
```

```
| Immed of word
```

MIPS continued

```
type inst =  
    Add of reg * reg * operand  
  | Li of reg * word  
  | Slt of reg * reg * operand  
  | Beq of reg * reg * label  
  | Bgez of reg * label  
  | J of label  
  | La of reg * label  
  | Lw of reg * reg * word  
  | Sw of reg * reg * word  
  | Label of label | ...
```

Variables

Fish only has global variables.

These can be placed in the *data segment*.

```
.data  
.align 0  
x: .word 0  
y: .word 0  
z: .word 0
```

Variable Access

To compile $x = x+1$

```
la $3, x ; load x's address
lw $2, 0($3) ; load x's value
addi $2, $2, 1 ; add 1
sw $2, 0($3) ; store value in x
```

First Problem: Nested Expr's

- Source:
 - $\text{Binop}(\text{Binop}(x, \text{Plus}, y), \text{Plus}, \text{Binop}(w, \text{Plus}, z))$
- Target:
 - `add rd, rs, rt`

What should we do?

A Simple Strategy

- Given: Binop(A,Plus,B)
- translate A so that result ends up in a particular register (e.g., \$3)
- translate B so that result ends up in a different register (e.g., \$2)
- Generate: add \$2, \$3, \$2

Problems?

Strategy Fixed:

- Invariants:
 - results always placed in \$2
- Given: Binop(A,Plus,B)
- translate A
- save \$2 somewhere
- translate B
- Restore A's value into register \$3
- Generate: add \$2, \$3, \$2

For example:

$\text{Binop}(\text{Binop}(x, \text{Plus}, y), \text{Plus}, \text{Binop}(w, \text{Plus}, z))$

1. compute $x+y$, placing result in $\$2$
2. store result in a temporary t_1
3. compute $w+z$, placing result in $\$2$
4. load temporary t_1 into a register, say $\$3$
5. add $\$2, \$3, \$2$

Expression Compilation

```
let rec exp2mips(i:exp):inst list =
  match i with
  | Int j -> [Li(R2, Word32.fromInt j)]
  | Var x -> [La(R2,x), Lw(R2,R2,zero)]
  | Binop(i1,b,i2) ->
    (let t = new_temp() in
     (exp2mips i1) @ [La(R1,t), Sw(R2,R1,zero)]
     @ (exp2mips i2) @ [La(R1,t), Lw(R1,R1,zero)]
     @ (match b with
        Plus -> [Add(R2,R2,Reg R1)]
        | ... -> ...))
  | Assign(x,e) => [exp2mips e] @
                   [La(R1,x), Sw(R2,R1,zero)]
```

Statements

```
let rec stmt2mips (s:stmt) :inst list =
  match s with
  | Exp e ->
      exp2mips e
  | Seq(s1,s2) ->
      (stmt2mips s1) @ (stmt2mips s2)
  | If(e,s1,s2) ->
      (let else_l = new_label() in
       let end_l = new_label() in
        (exp2mips b) @ [Beq(R2,R0,else_l)] @
        (stmt2mips s1) @ [J end_l,Label else_l] @
        (stmt2mips s2) @ [Label end_l])
```

Statements Continued

```
| While(e,s) ->
  (let test_l = new_label() in
   let top_l = new_label() in
    [J test_l, Label top_l] @
    (stmt2mips s) @
    [Label test_l] @
    (exp2mips b) @
    [Bne(R2,R0,top_l)])
| For(e1,e2,e3,s) ->
  stmt2mips(Seq(Exp e1,While(e2,Seq(s,Exp e3))))
```

Lots of Inefficiencies:

- Compiler takes $O(n^2)$ time due to @.
- No constant folding.
- For "**if (x == y) s1 else s2**" we do a **seq** followed by a **beq** when we could just do a **beq**.
- For "**if (b1 && b2) s1 else s2**" we could just jump to **s2** when **b1** is false.
- Lots of **la/lw** and **la/sw** for variables.
- For **e1 + e2**, we always write out **e1**'s value to memory when we could just cache it in a register.

Append:

Naïve append:

```
fun append nil y = y
  | append (h::t) y = h::(append t y)
```

Tail-recursive append:

```
fun revapp nil y = y
  | revapp (h::t) y = revapp t (h::y)
fun rev x = revapp x []
fun append x y = revapp (rev x) y
```


Accumulator-Based:

```
let rec exp2mips' (i:exp) (a:inst list):inst list =  
  match i with  
  ...
```

```
let exp2mips (i:exp) = (exp2mips' i [])
```

Constant Folding: Take 1

```
let rec exp2mips' (i:F.iexp) (a:inst list) =  
  match i with  
  | Int w -> Li(R2, Word32.fromInt w) :: a  
  | Binop(i1,Plus,Int 0) -> exp2mips' i1 a  
  | Binop(Int i1,Plus,Int i2) ->  
    exp2mips' (Int (i1+i2)) a  
  | Binop(Int i1,Minus,Int i2) ->  
    exp2mips' (Int (i1-i2)) a  
  | Binop(b,i1,i2) -> ...
```

Why isn't this great? How can we fix it?

Conditional Contexts

Consider: if ($x < y$) then S1 else S2

```
    slt    $2, $2, $3
    beq    $2, ELSE
        S1
    j     END
ELSE:
        S2
END:
```

Observation

- In most contexts, we want a value.
- But in a testing context, we jump to one place or another based on the value, and otherwise never use the value.
- In many situations, we can avoid materializing the value and thus produce better code.

For Example:

```
let rec bexp2mips (e:exp) (t:label) (f:label) =
  match e with
  | Int 0 -> [J f]
  | Int _ -> [J t]
  | Binop(e1,Eq,e2) =>
    (let t = temp()
     in
      (exp2mips e1) @
      [La (R1,t), Sw (R2,R1,zero)] @
      (exp2mips e2) @
      [La (R1,t), Lw (R1,R1,zero),
       Bne (R1,R2,f), J t])
  | _ -> (exp2mips e1) @ [ Beq (R2,R0,f), J t ]
```

Global Variables:

We treated all variables (including temps) as if they were globals:

- set aside data with a label
- to read: load address of label, then load value stored at that address.
- to write: load address of label, then store value at that address.

This is fairly inefficient:

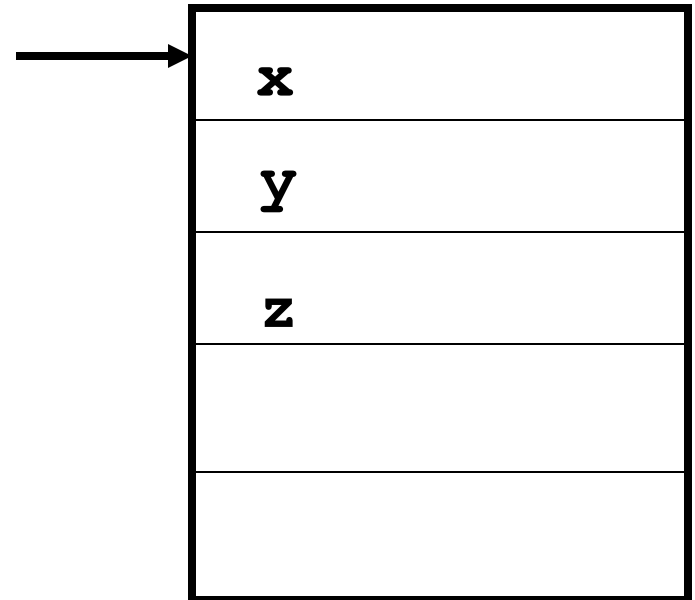
- e.g., $x+x$ involves loading x 's address twice!
- lots of memory operations.

Register Allocation:

- One option is to allocate a register to hold a variable's value:
 - Eliminates the need to load an address or do memory operations.
 - Will talk about more generally later.
 - Of course, in general, we can't avoid it when code has more (live) variables than registers.
- Can we at least avoid loading addresses?

Frames:

- Set aside one block of memory for all of the variables.
- Dedicate $\$30$ (aka $\$fp$) to hold the base address of the block.
- Assign each variable a position within the block ($x \rightarrow 0, y \rightarrow 4, z \rightarrow 8, \text{etc.}$)
- Now loads/stores can be done relative to $\$fp$:



Before and After:

`z = x+1`

```
lda $1,x
lw $2,0($1)
addi $2,$2,1
lda $1,z
sw $2,0($1)
```

```
lw $2,0($fp)
addi $2,$2,1
sw $2,8($fp)
```

Lowering

- Get rid of nested expressions before translating
 - Introduce new variables to hold intermediate results
 - Perhaps do things like constant folding
- For example, $a = (x + y) + (z + w)$ might be translated to:

```
t0 := x + y;
```

```
t1 := z + w;
```

```
a := t0 + t1;
```

12 instructions (9 memory)

```
t0 := x + y;      lw $v0, <xoff>($fp)
                  lw $v1, <yoff>($fp)
                  add $v0, $v0, $v1
                  sw $v0, <t0off>($fp)
t1 := z + w;      lw $v0, <zoff>($fp)
                  lw $v1, <woff>($fp)
                  add $v0, $v0, $v1
                  sw $v0, <t1off>($fp)
a := t0 + t1;    lw $v0, <t0off>($fp)
                  lw $v1, <t1off>($fp)
                  add $v0, $v0, $v1
                  sw $v0, <aoff>($fp)
```

Still...

We're doing a lot of stupid loads and stores.

- We shouldn't need to load/store from temps!
- (Nor variables, but we'll deal with them later...)

So another idea is to use registers to hold the intermediate values instead of variables.

- Of course, we can only use registers to hold some number of temps (say k).
- Maybe use registers to hold first k temps?

For example:

```
t0 := x;           # load variable
t1 := y;           # load variable
t2 := t0 + t1;     # add
t3 := z;           # load variable
t4 := w;           # load variable
t5 := t3 + t4;     # add
t6 := t2 + t5;     # add
a := t6;           # store result
```

Then: 8 instructions (5 mem!)

- Notice that each little statement can be directly translated to MIPS instructions:

```
t0 := x;          --> lw $t0,<xoff>($fp)
t1 := y;          --> lw $t1,<yoff>($fp)
t2 := t0 + t1;    --> add $t2,$t0,$t1
t3 := z;          --> lw $t3,<zoff>($fp)
t4 := w;          --> lw $t4,<woff>($fp)
t5 := t3 + t4;    --> add $t5,$t3,$t4
t6 := t2 + t5;    --> add $t6,$t2,$t5
a := t6;          --> sw $t6,<aoff>($fp)
```

Recycling:

- Sometimes we can recycle a temp:

<code>t0 := x;</code>	<code>t0 taken</code>
<code>t1 := y;</code>	<code>t0, t1 taken</code>
<code>t2 := t0 + t1;</code>	<code>t2 taken (t0, t1 free)</code>
<code>t3 := z;</code>	<code>t2, t3 taken</code>
<code>t4 := w;</code>	<code>t2, t3, t4 taken</code>
<code>t5 := t3 + t4;</code>	<code>t2, t5 taken (t3, t4 free)</code>
<code>t6 := t2 + t5;</code>	<code>t6 taken (t2, t5 free)</code>
<code>a := t6;</code>	<code>(t6 free)</code>

Tracking Available Temps:

Hmmm. Looks a lot like a stack...

<code>t0 := x;</code>	<code>t0</code>
<code>t1 := y;</code>	<code>t1, t0</code>
<code>t0 := t0 + t1;</code>	<code>t0</code>
<code>t1 := z;</code>	<code>t1, t0</code>
<code>t2 := w;</code>	<code>t2, t1, t0</code>
<code>t1 := t1 + t2;</code>	<code>t1, t0</code>
<code>t1 := t0 + t1;</code>	<code>t1</code>
<code>a := t1;</code>	<code><empty></code>

Finally, consider:

$(x+y) * x$

```
t0 := x;           # loads x
t1 := y;
t0 := x+y
t1 := x;           # loads x again!
t0 := t0*t1;
```

Good Compilers: (not this proj!)

Introduces temps as described earlier:

- It lowers the code to something close to assembly, where the number of resources (i.e., registers) is made explicit.
- Ideally, we have a 1-to-1 mapping between the lowered intermediate code and assembly code.

Performs an analysis to calculate the *live range* of each temp:

- A temp t is live at a program point if there is a subsequent read (use) of t along some control-flow path, without an intervening write (definition).
- The problem is simplified for *functional* code since variables are never re-defined.

Interference Graphs:

From the live-range information for each temp, we calculate an *interference graph*.

- Temps **t1** and **t2** *interfere* if there is some program point where they are both live.
- We build a graph where the nodes are temps and the edges represent interference.
- If two temps interfere, then we cannot allocate them to the same register.
- Conversely, if **t1** and **t2** do not interfere, we can use the same register to hold their values.

Register Coloring

- Assign each node (temp) a register such that if t_1 interferes with t_2 , then they are given distinct colors.
 - Similar to trying to "color" a map so that adjacent countries have different colors.
 - In general, this problem is NP complete, so we must use heuristics.
- Problem: given k registers and $n > k$ nodes, the graph might not be colorable.
 - Solution: spill a node to the stack.
 - Reconstruct interference graph & try coloring again.
 - Trick: spill temps that are used infrequently and/or have high interference degree.

Example:

$a := (x+y) * (x+z)$

$t_0 := x$

$t_1 := y$

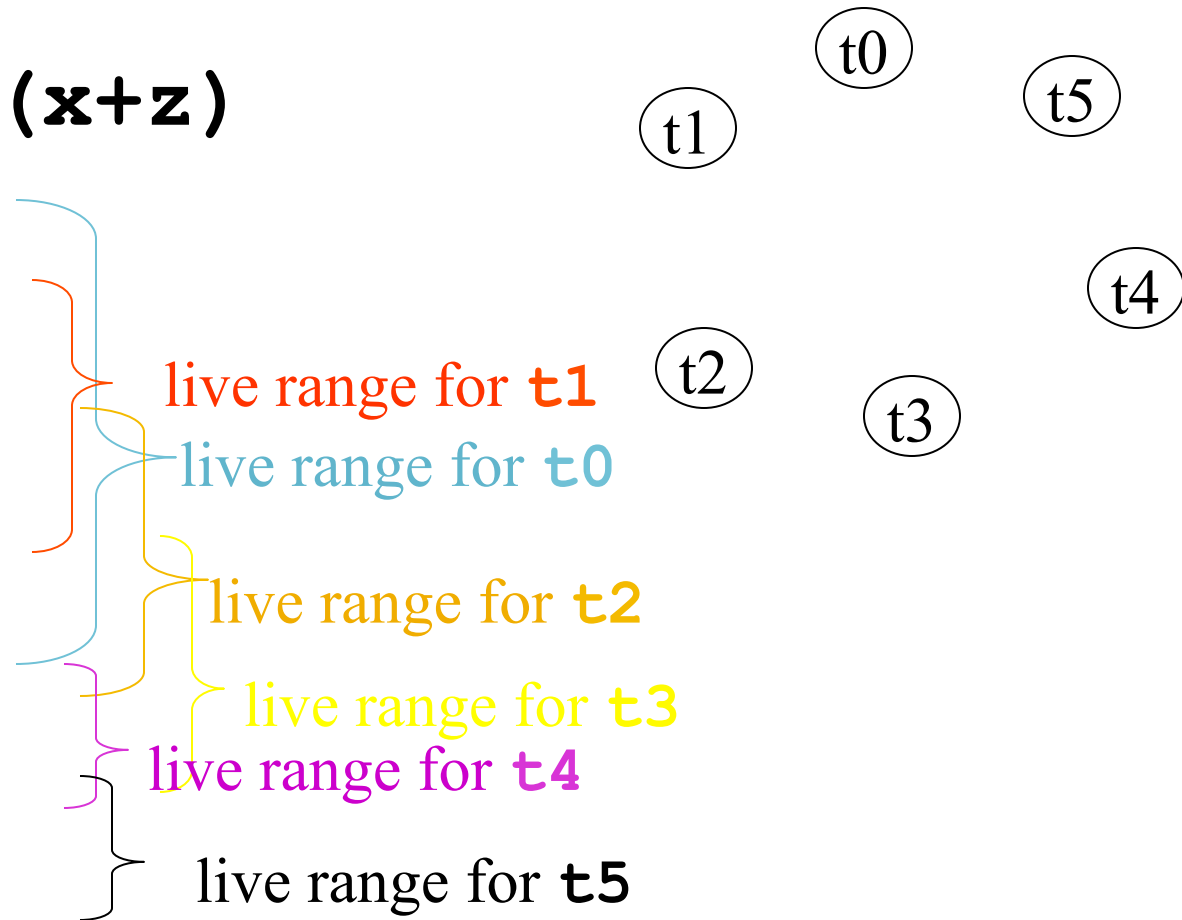
$t_2 := z$

$t_3 := t_0 + t_1$

$t_4 := t_0 + t_2$

$t_5 := t_3 * t_4$

$a := t_5$



Graph:

$a := (x+y) * (x+z)$

$t_0 := x$

$t_1 := y$

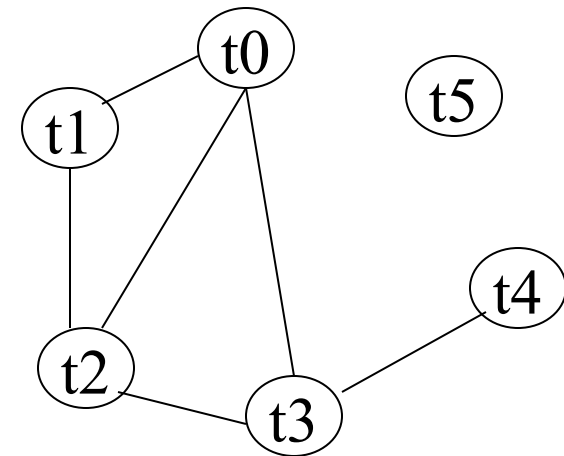
$t_2 := z$

$t_3 := t_0 + t_1$

$t_4 := t_0 + t_2$

$t_5 := t_3 * t_4$

$a := t_5$



Coloring:

$a := (x+y) * (x+z)$

$t_0 := x$

$t_1 := y$

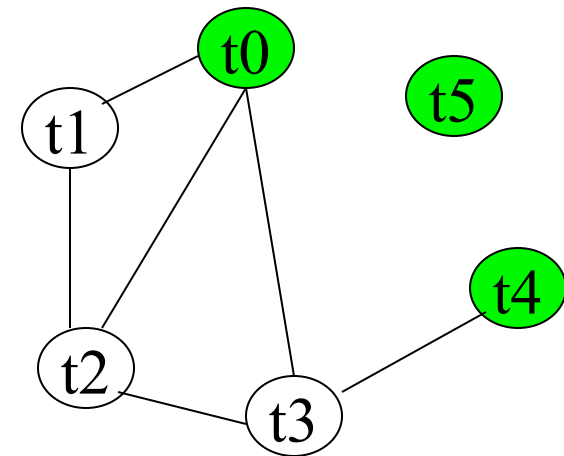
$t_2 := z$

$t_3 := t_0 + t_1$

$t_4 := t_0 + t_2$

$t_5 := t_3 * t_4$

$a := t_5$



Coloring:

$a := (x+y) * (x+z)$

$t_0 := x$

$t_1 := y$

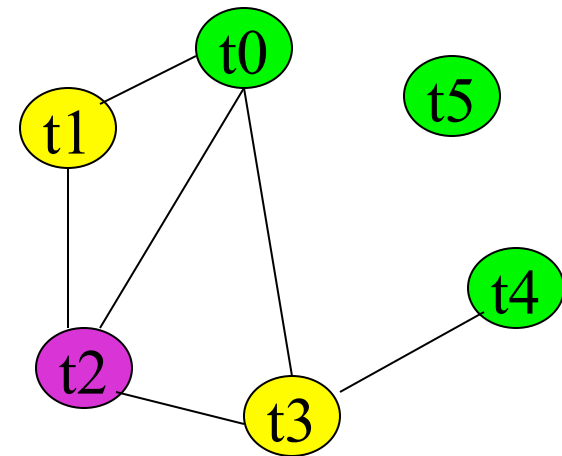
$t_2 := z$

$t_3 := t_0 + t_1$

$t_4 := t_0 + t_2$

$t_5 := t_3 * t_4$

$a := t_5$



Assignment:

$a := (x+y) * (x+z)$

$t0 := x$

$t1 := y$

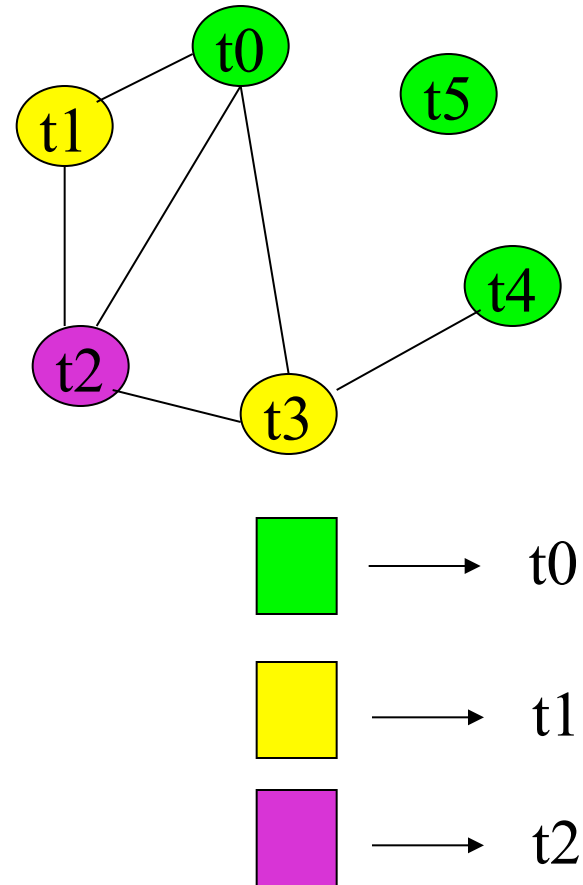
$t2 := z$

$t3 := t0+t1$

$t4 := t0+t2$

$t5 := t3*t4$

$a := t5$



Rewrite:

$a := (x+y) * (x+z)$

$t0 := x$

$t1 := y$

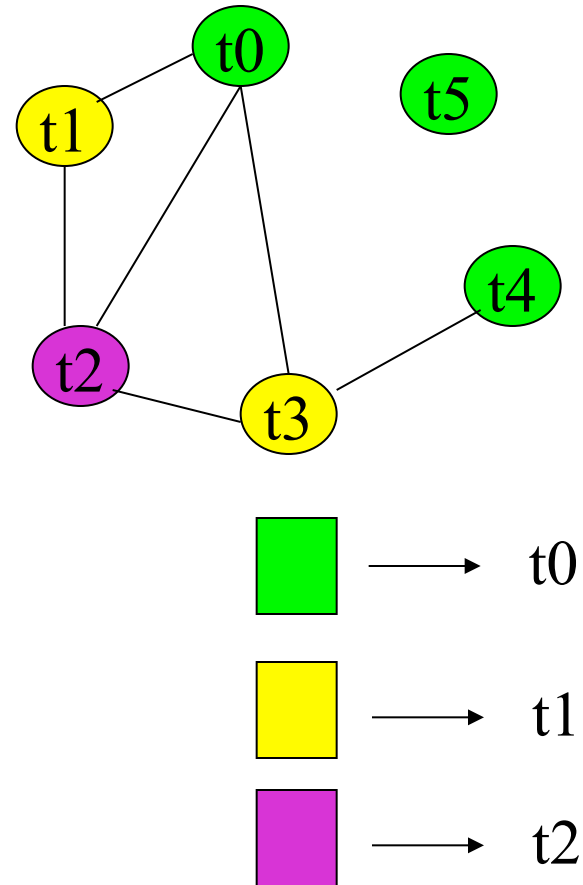
$t2 := z$

$t3 := t0+t1$

$t0 := t0+t2$

$t0 := t3*t0$

$a := t0$



Generate Code

`a := (x+y) * (x+z)`

```
t0 := x      --> lw $t0,<xoff>($fp)
t1 := y      --> lw $t1,<yoff>($fp)
t2 := z      --> lw $t2,<zoff>($fp)
t3 := t0+t1  --> add $t3,$t0,$t1
t0 := t0+t2  --> add $t0,$t0,$t2
t0 := t3*t0  --> mul $t0,$t3,$t2
a := t0      --> sw $t0,<aoff>($fp)
```