

CS 4770: Cryptography

CS 6750: Cryptography and  
Communication Security

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# Schedule

- HW 4
  - It is out on Piazza
  - Due on Thu 04/12
- Programming project 3
  - Out on 04/12
  - Due on 04/26 (last day it can be accepted)
  - Grading on 04/27
- Final exam
  - 04/23, 1-3pm

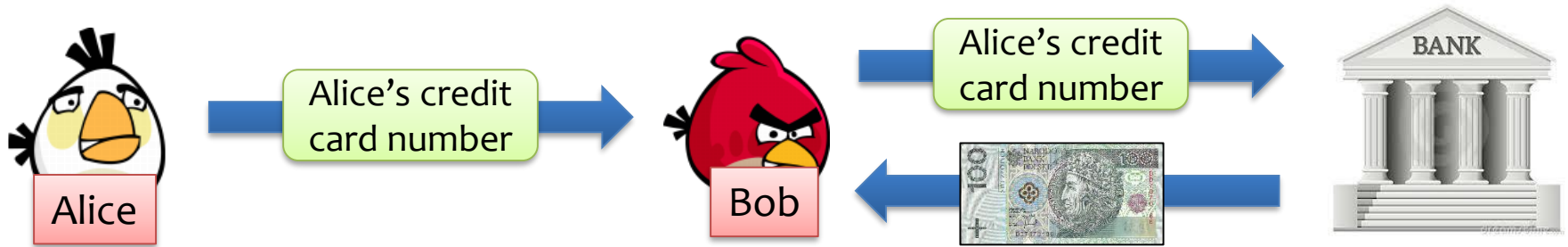
# Bitcoin

- Digital crypto currencies
  - Advantages over paper cash
- Distributed public ledger
  - Blockchain creation and distribution
  - Proof of Work (PoW)
  - Agreement and resilience to adversaries
  - Incentives for users
- Bitcoin security
- Other cryptocurrencies

# Resources

- Book: Bitcoin and Cryptocurrency Technologies
  - <http://bitcoinbook.cs.princeton.edu/>
- Bonneau et al. Research Perspectives and Challenges for Bitcoin and Cryptocurrencies.
  - <https://eprint.iacr.org/2015/261.pdf>
- Bitcoin and Cryptocurrency Technologies Course
  - <https://www.coursera.org/learn/cryptocurrency>
  - <https://piazza.com/princeton/spring2015/btctech/resources>

# Traditional ways of paying “digitally”



## **BENEFITS**

1. Convenient (pay online)
2. Highly regulated
3. Banks handle fraud
4. Cannot double-spend
5. Tax records

## **PROBLEMS**

1. **Trusted server** for each transaction
2. High **transaction fees**
3. Record of all transactions (**No anonymity/privacy**)



# Bitcoin – a “digital analogue” of the paper money



A digital currency introduced by “Satoshi Nakamoto” in 2008

- First e-cash without a centralized issuing authority
  - Store and transfer value without reliance on central banks
  - Anyone can join the system and make transactions
  - Transactions are publicly verifiable
- Built on top of an unstructured P2P system
  - Participants validate transactions and mint currency
  - System works as long as the *majority of users are honest*



Currency unit: **Bitcoin (BTC)** 1 BTC =  $10^8$  Satoshi; value  $\approx$  \$6800

# Bitcoin



in Bitcoin:

No trusted server,  
money circulates

Low fees

“Pseudonymity”

## PROBLEMS WITH DIGITAL PAYMENT

1. **Trusted server** for each transaction
2. **High transaction fees**
3. **No anonymity/privacy.**

# Bitcoin $\approx$ “real money”?

**Bitcoin** value comes from the fact that:

**“people expect that other people will accept it in the future.”**

enthusiasts:



It's like all the other currencies

sceptics:



P. Krugman



A. Greenspan



It's a Ponzi scheme





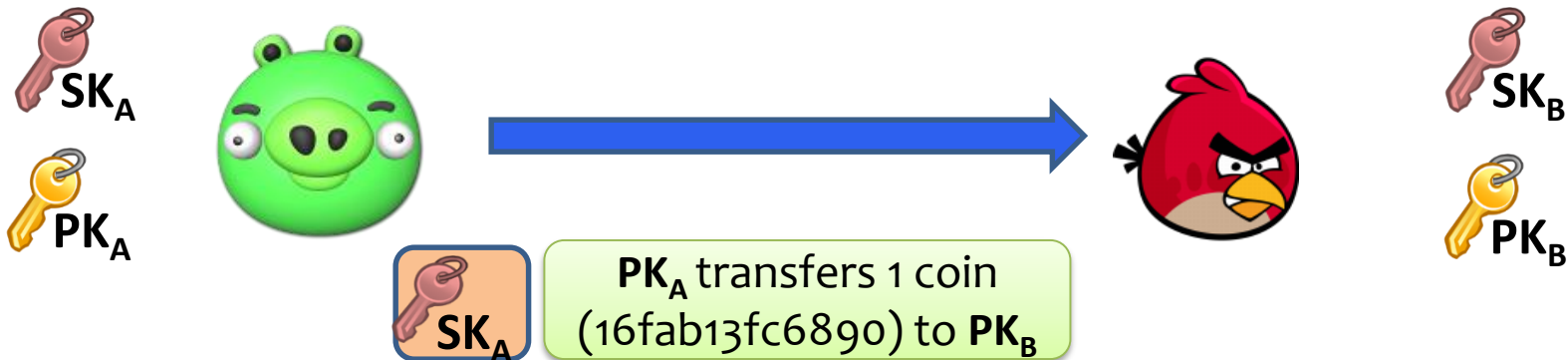
# Strawman protocol

- Alice owns a coin and wants to transfer to Bob
  - Transactions can not be forged
  - Can not be reversed
  - Spend once every coin
  - Can be spent by Bob later
- Format of coin?
  - Unique serial number (long bit string)
- What to use for identities?
  - Requirement for weak identities (no use of national ID or passport)
  - Public keys!



# Strawman protocol

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# Bitcoin Transactions



Public key 0xc7b2f68...

11-3167/1210  
01

505

STANFORD UNIVERSITY  
STANFORD, CA 94305-9045

Date 8 Mar 99

Public key 0xa8fc93875a972ea

2.56

Pay to the  
Order of

Two and



56/100

Dollars

AMERICA CALIFORNIA BANK

2390 El Camino Real • Palo Alto, CA 94306

For J. 589

Signature 0xa87g14632d452cd

⑆ 1 291 3 16 7 3 ⑆ 0 50 5 0 ⑆ 1 4 5 8 4 4 0 6 ⑆

Serial  
number

Value

Digital  
signature

The Times 03/Jan/2009 *Chancellor on  
brink of second bailout for banks.*



## Bitcoin: A Peer-to-Peer Electronic Cash System

Satoshi Nakamoto  
satoshin@gmx.com  
www.bitcoin.org

**Abstract.** A purely peer-to-peer version of electronic cash would allow online payments to be sent directly from one party to another without going through a financial institution. Digital signatures provide part of the solution, but the main benefits are lost if a trusted third party is still required to prevent double-spending. We propose a solution to the double-spending problem using a peer-to-peer network. The network timestamps transactions by hashing them into an ongoing chain of

```
bitcoin-0.1.0.rar  
bitcoin-0.1.0.tgz
```

# Main problem with the digital money

Double spending...

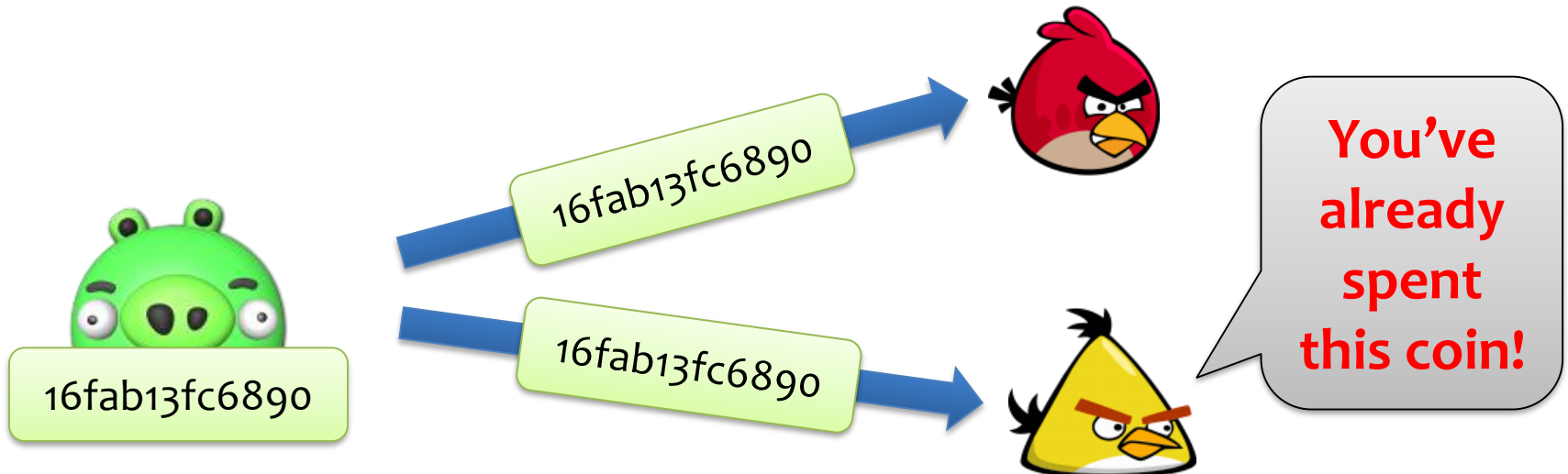
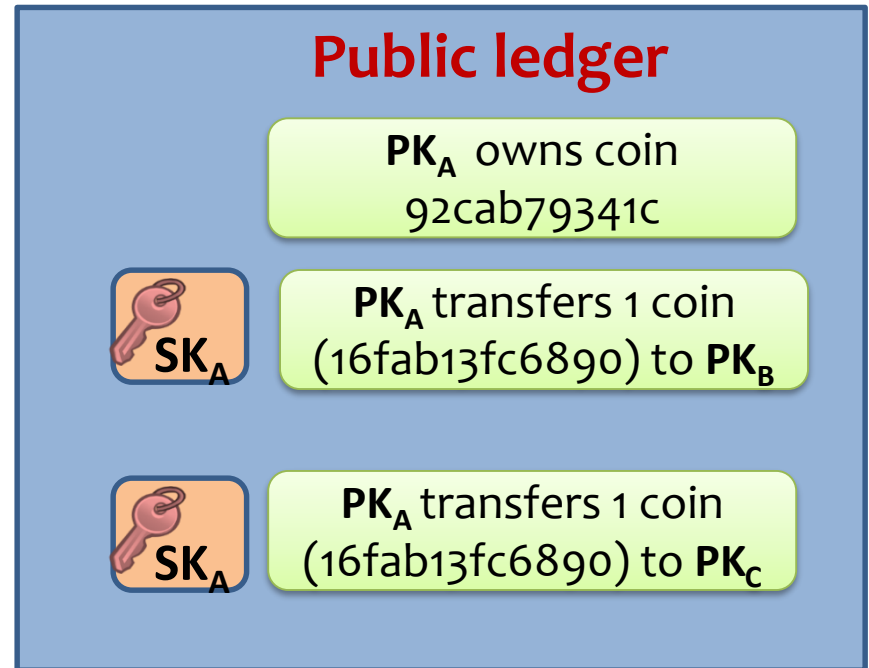


Bits are easier to copy than paper!  
Signatures alone do not prevent this

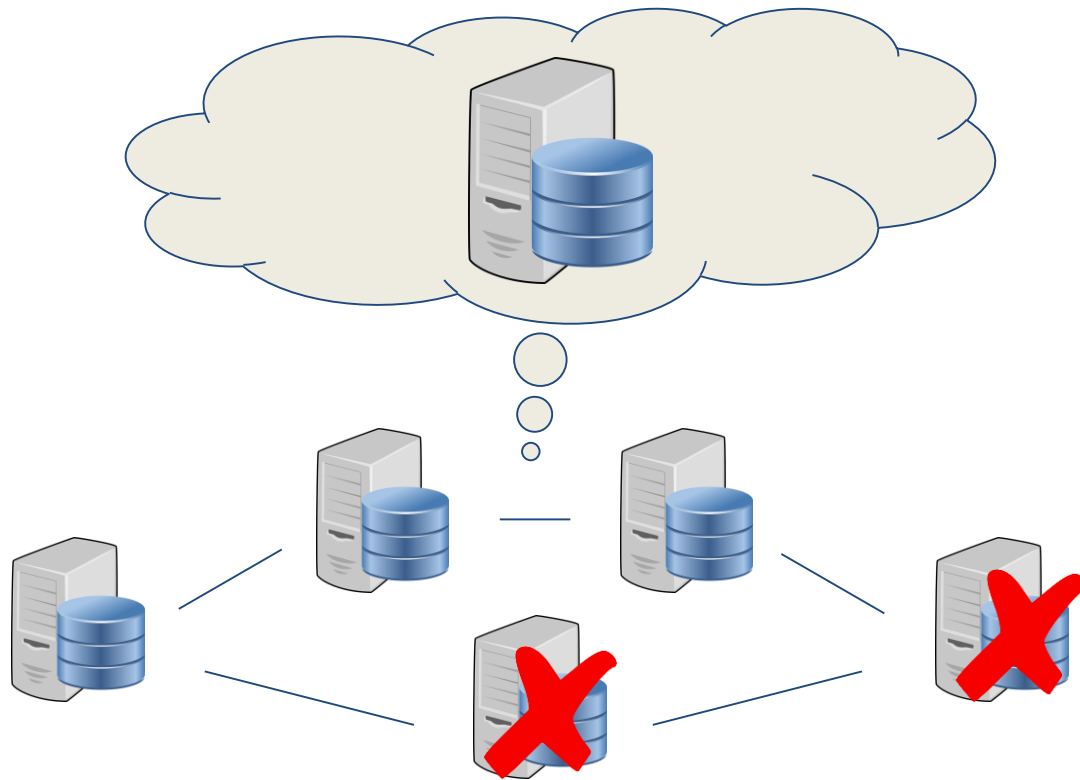
# Bitcoin idea

## Public trusted bulletin-board (public ledger or DB)

- Includes list of all transactions
- Verifiable by all users
- How to maintain it in decentralized fashion?



# A blockchain is a *Distributed System*



P2P Network

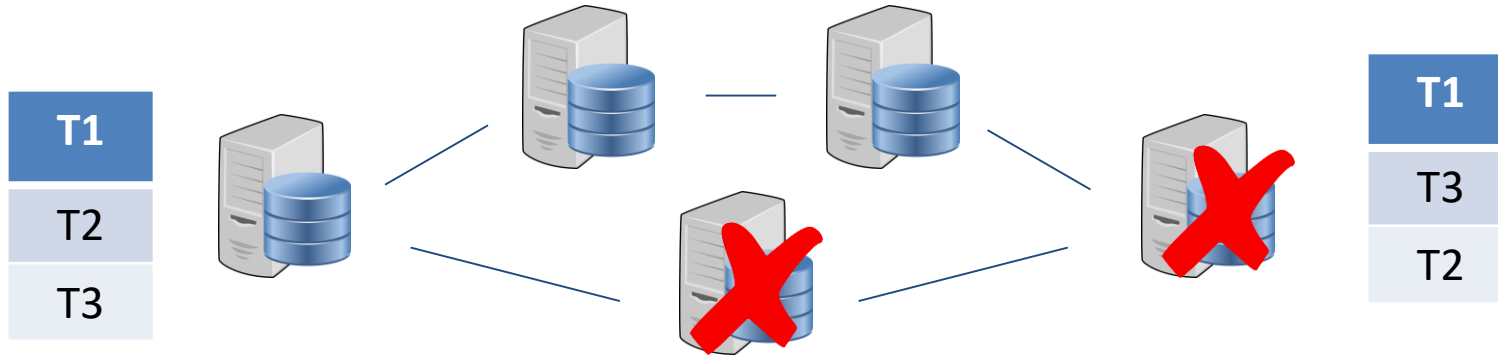
## Ordinary databases:

- Distributed within one domain
- For performance and availability

## Decentralized Ledger:

- Distributed across multiple entities
- Privacy and security against attacks
- Correctness assuming honest majority
- No single point of failure

# Challenges in designing public ledger




- **Decentralized ledger**
  - Each user maintains a list of transactions ordered across time
  - His own transactions and transactions received from other users
- **Main challenges: Obtain consensus**
  - Order of transactions is the same at all nodes
- **Attack models**
  - Network failures (messages might not be delivered timely)
  - Offline participants (nodes leave and re-connect to the network)
  - Malicious nodes (nodes try to double spend)



# Key insights

- **Decentralization through P2P network**
  - Each transaction is *broadcast* to all nodes
  - Each node keeps a tamper-evident log (local ledger) of **all** Bitcoin transactions
  - Nodes agree on list of transactions and their order (distributed consensus)
- **Consensus happens over longer periods of time**
  - Probabilistic guarantees
  - In online transactions can have some delay
- **Attack model**
  - Assumption: attacker cannot control majority computational power in the network

# Bitcoin

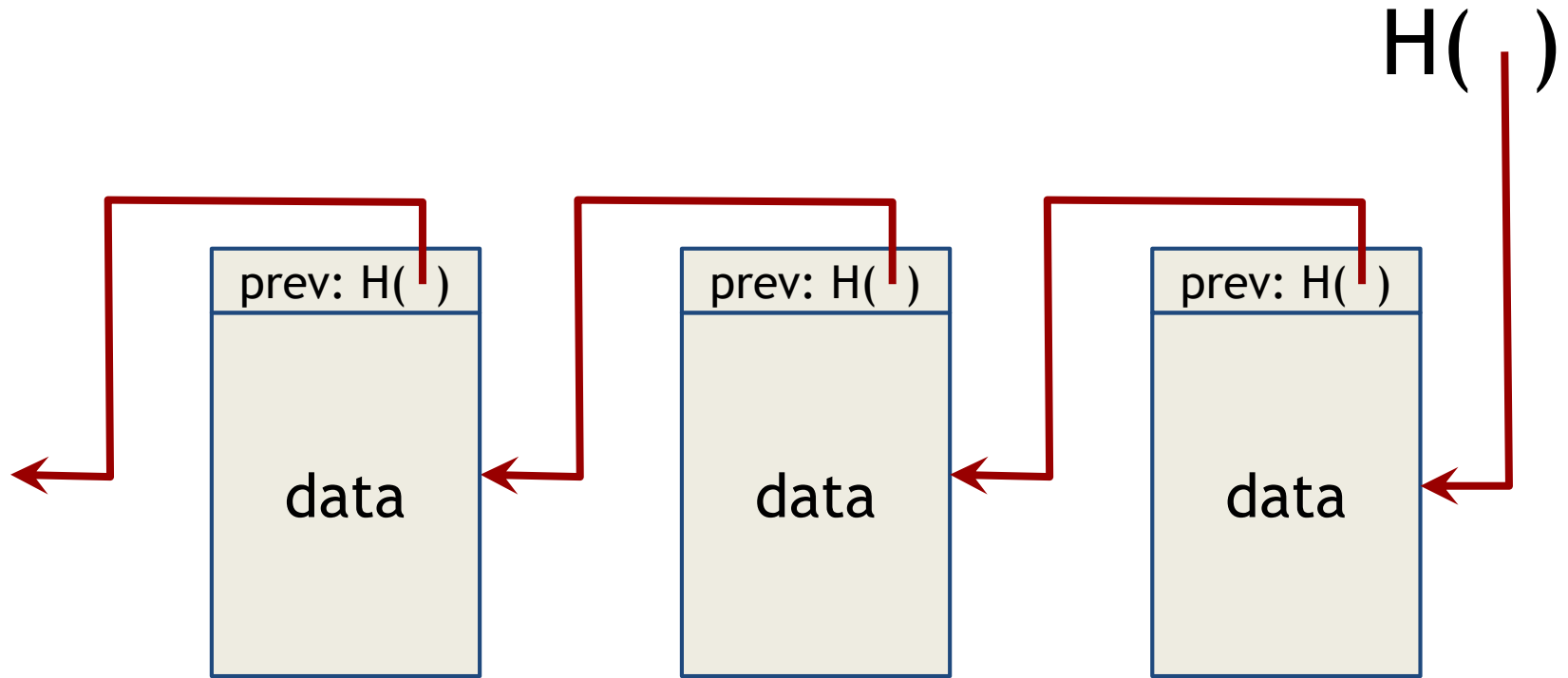
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# Public ledger

- **Tamper-evident log**
  - Record and order all transactions locally at each node
  - Valid transactions can not be modified
  - New transactions are appended after being validated
- How to design it?
  - What data structure and crypto primitives to use?
- How to prevent attackers controlling majority of transactions?
- How to incentivize users?
- How to reach agreement?

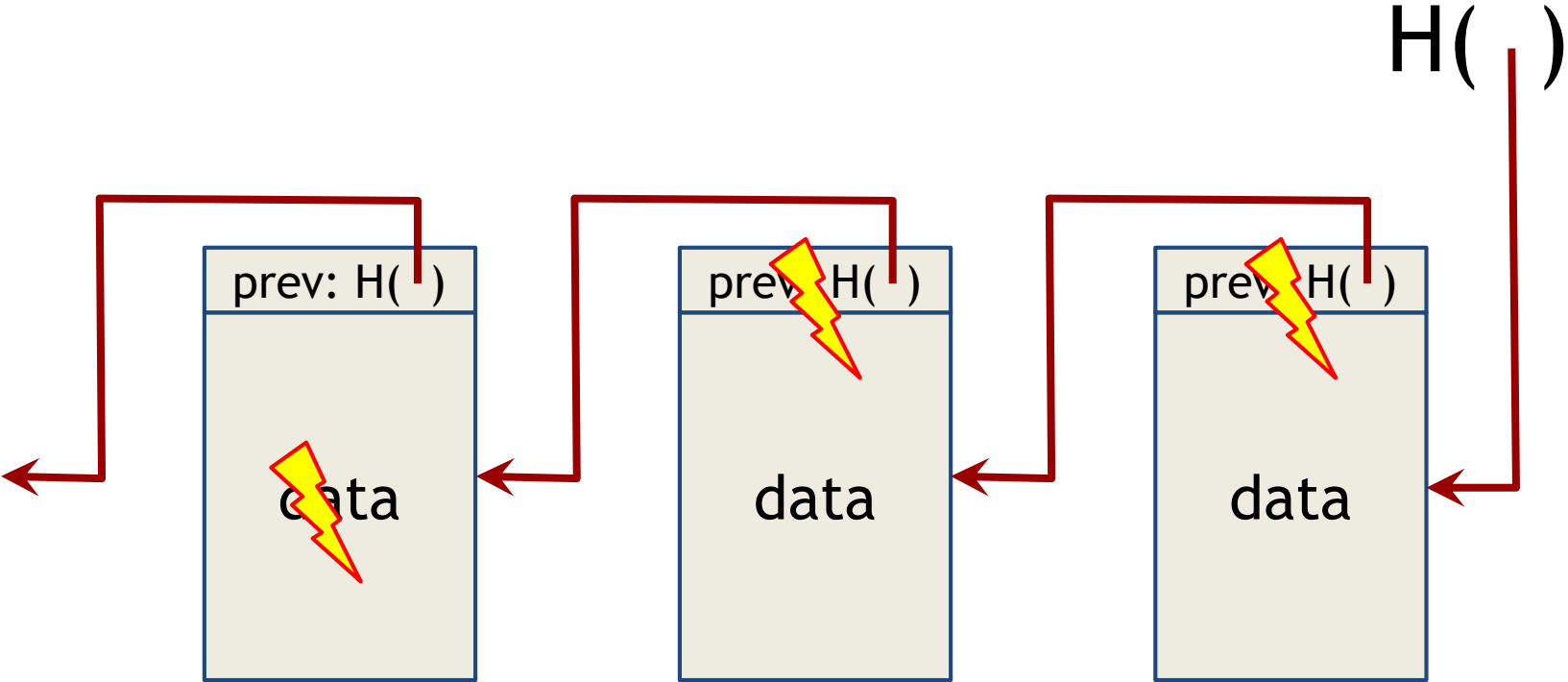
# Block chain

Linked list with hash pointers



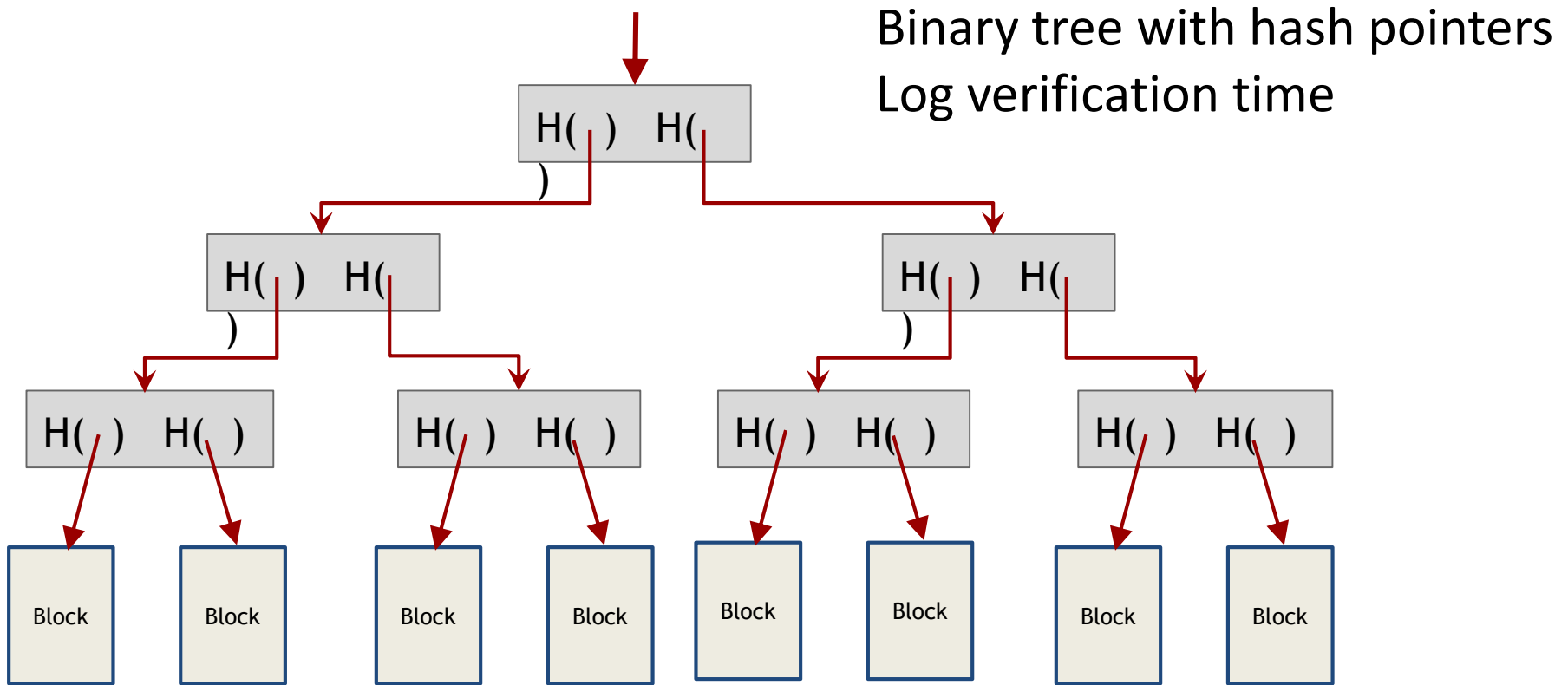
Tamper-evident log

# Detecting tampering



Tamper-evident log

# Merkle trees



	Block Hash	Prev. Block Hash	Nonce
Block		Transaction I	
		Transaction J	
		Transaction K	

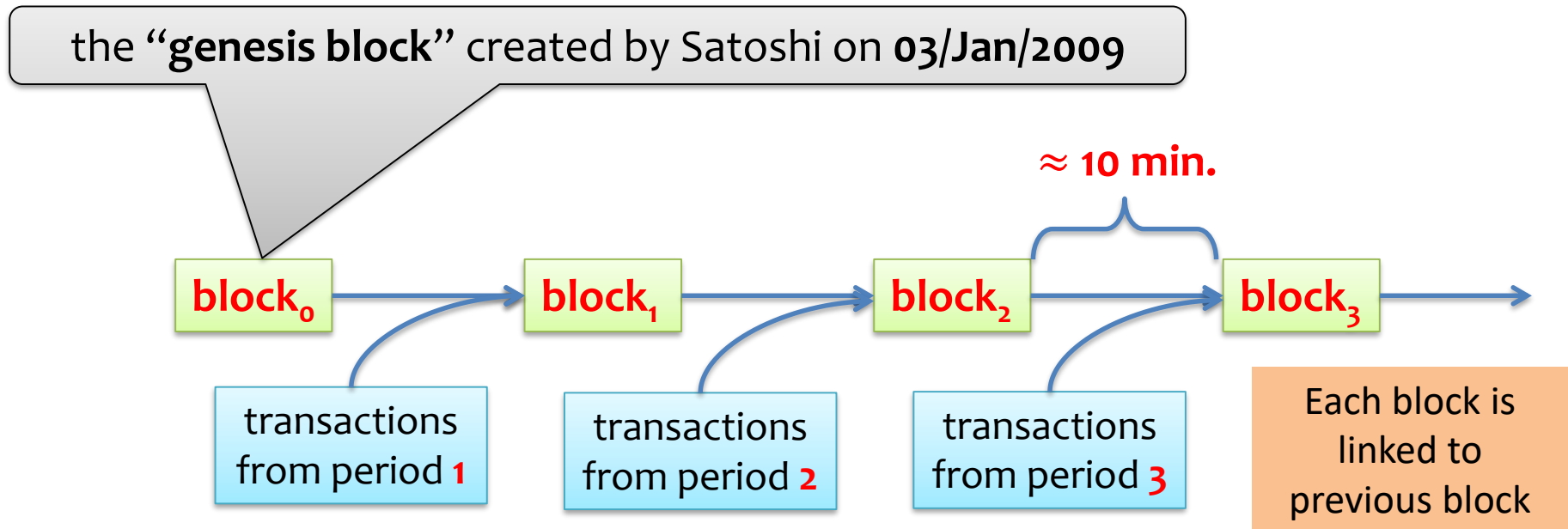
Multiple transactions for efficiency

# Block chain

The users participating in the scheme are called “miners”.



They maintain a chain of blocks (blockchain):




# Distributing transactions

- New transactions are *broadcast* to all nodes
  - P2P network
- Each node *collects new transactions* into a block
- In each round (e.g., every 10 minutes)
  - A random node *creates the next block* (includes outstanding transactions)
- Other nodes accept the block only if *all transactions in it are valid*
  - Valid signatures
  - Coins not spent before
- Nodes accept the block by including it in their local ledger



# Public ledger

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# Problem

How to define “**majority**” in  
a situation where  
**everybody can join the network?**



Sybil attacks – users create multiple identities  
Attacker can control majority!

# The Bitcoin solution

Use a resource that is hard to obtain

- In the past gold, could use national/state IDs (do not have anonymity)

Key insight: **use computational resource** (CPU power)

- Users need to present **Proofs-of-Work** to append transactions to ledger

Now creating multiple identities does not help!



# Proofs of work

Introduced by **Dwork and Naor** [Crypto 1992] as a countermeasure against spam.



## Basic idea:

Force users to do some computational work:

    solve a **moderately difficult** “puzzle”

(checking correctness of the solution has to be fast)

# Proofs of Work (PoW)

## Properties

- Cryptographic puzzles users need to solve
- Take minimum amount of CPU resources to compute
- Fast to verify
- Incentivize honest users to constantly participate in the process
  - The honest users can use their **idle CPU cycles**
  - **Nowadays**: often done on **dedicated hardware (ASIC)**
- Alleviates Sybil attacks
  - E.g. one machine pretending to be 100 Sybils doesn't magically get 100x CPU power
  - Attackers need to consume 100x computational resources
  - Implicit assumption: no single entity can control the majority of computational power

# A simple hash-based PoW

**H** -- a hash function whose computation takes time **TIME(H)**



**Prover**

finds **s** such that **H(s,x)** starts with **n** zeros (in binary)



salt

hardness parameter n

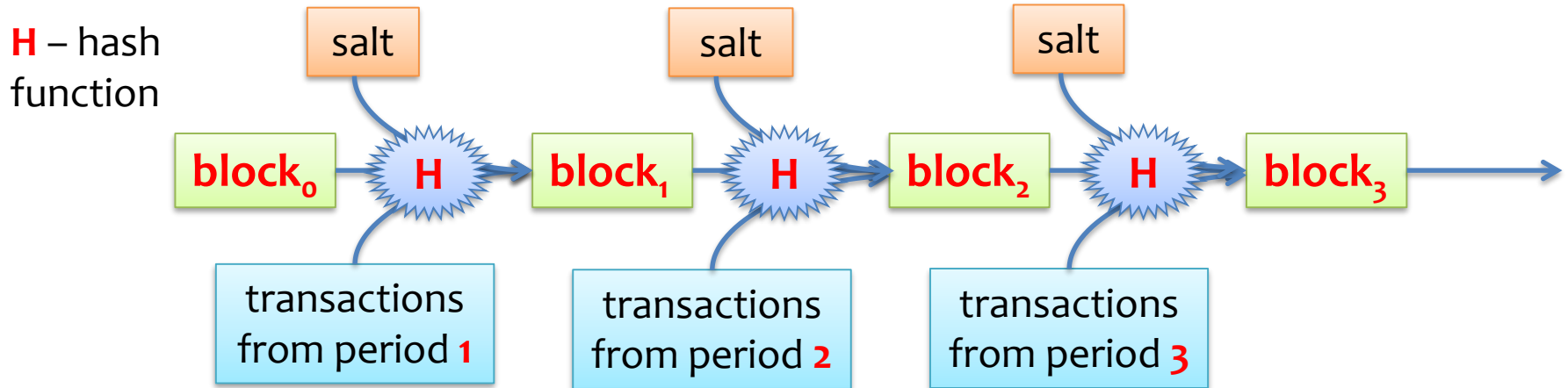
takes time  $2^n \cdot \text{TIME(H)}$

**Verifier**

checks if **H(s,x)** starts with **n** zeros

takes time **TIME(H)**

# How are the PoWs used?



**Main idea**: to extend it one needs to find **salt** such that

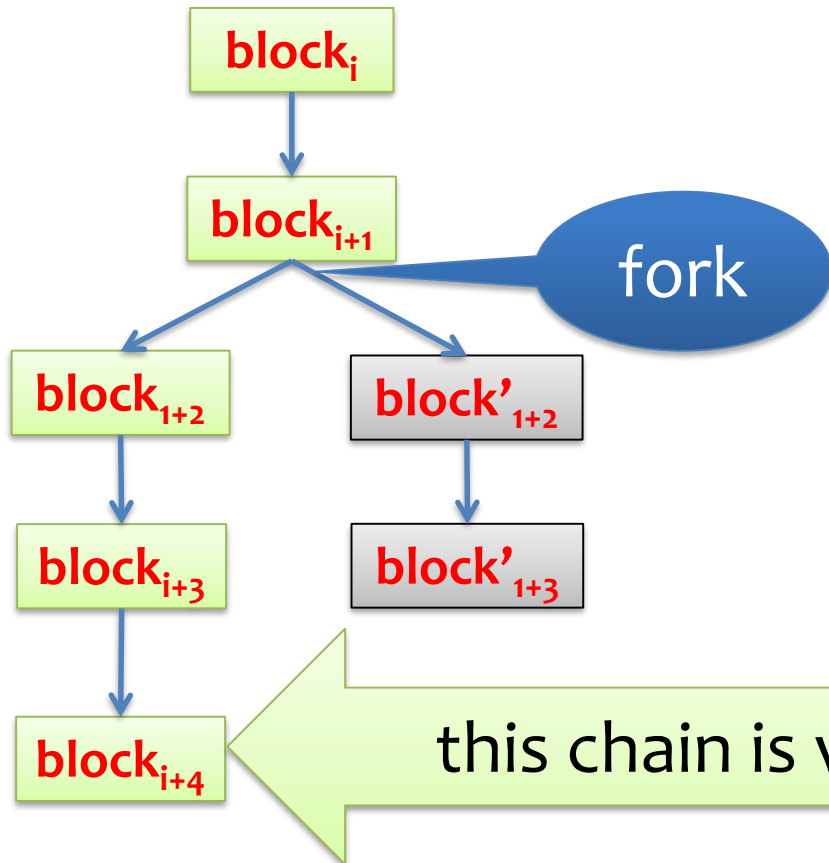
**$H(\text{salt}, \text{block}_i, \text{transactions})$**  starts with some number **n** of **zeros**

Process is called **block mining**

# Double spending: “forks”

The “**longest**” chain counts.

- It includes “more work”





# Acknowledgement

Some of the slides and slide contents are taken from

<http://www.crypto.edu.pl/Dziembowski/teaching>

and fall under the following:

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We have also used slides from Prof. Dan Boneh online cryptography course at Stanford University:

<http://crypto.stanford.edu/~dabo/courses/OnlineCrypto/>