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Analysis I  
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### **Day 17 — Summary — Completion of a vector space**

97.  $\mathbb{R}$  can be defined as the set of equivalence classes of Cauchy sequences of  $\mathbb{Q}$ . This is called the completion of  $\mathbb{Q}$ .
98. The completion of a normed vector space is defined as the set of equivalence classes of Cauchy sequences of elements in the space. The completion is a complete normed vector space.